

Training Machines to See What You See

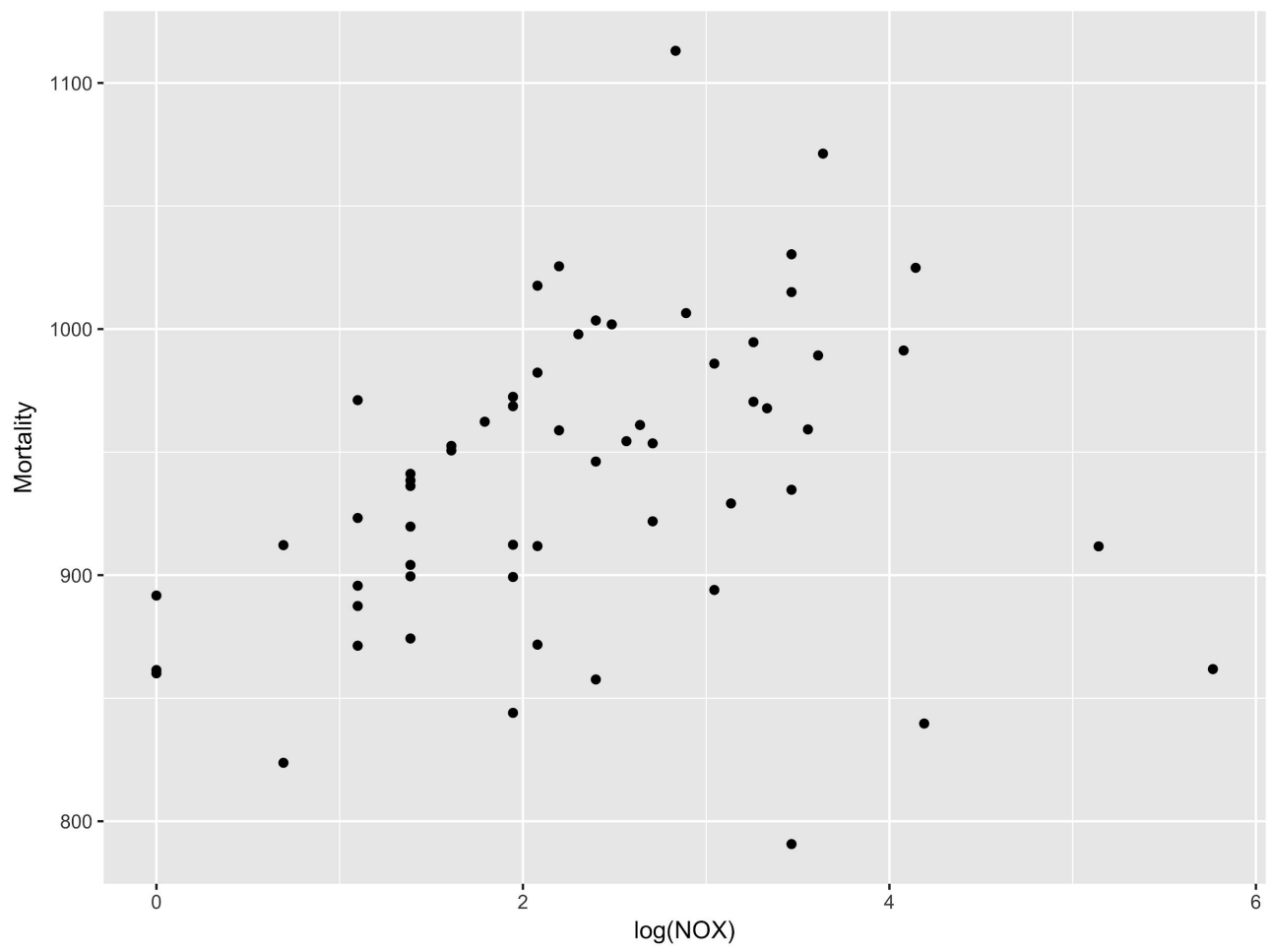
Let's start with some data

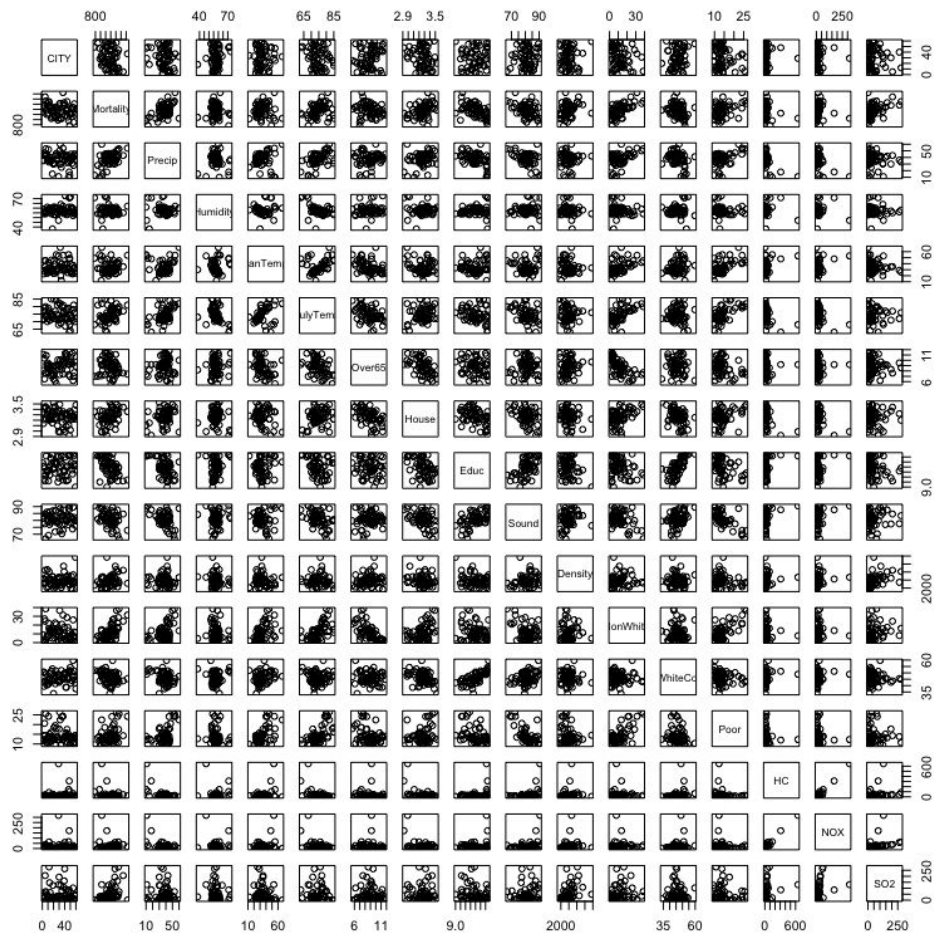
How does air pollution affect mortality?



Data set with both pollution and socioeconomic data for 5 Standard Metropolitan Statistical Areas in the U.S between 1959–1961.

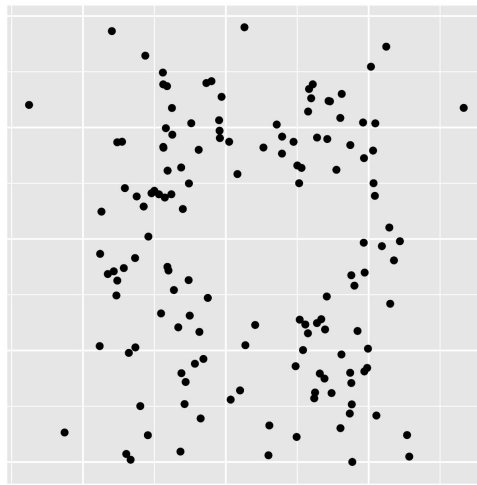
60 observations of 17 variables.





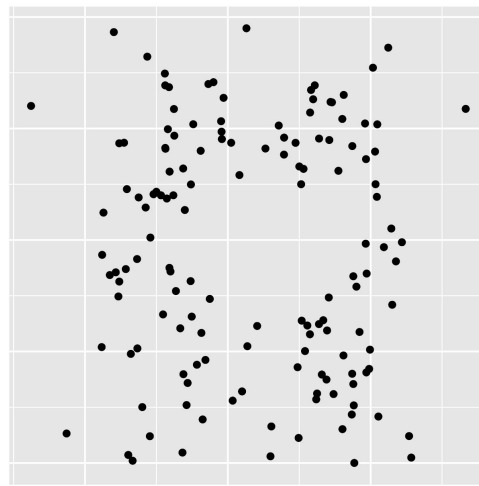
Can we train a computer to
detect patterns more effectively
and efficiently than humans?

Summary Statistics



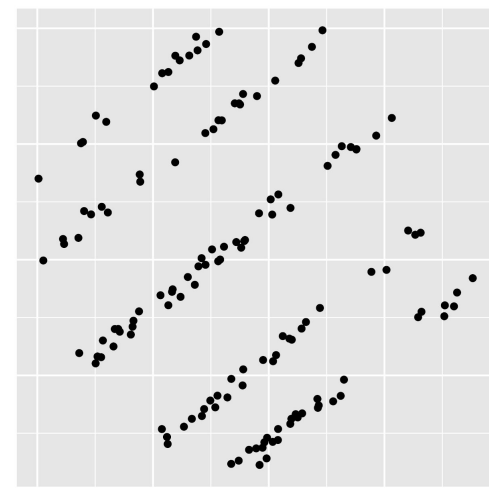
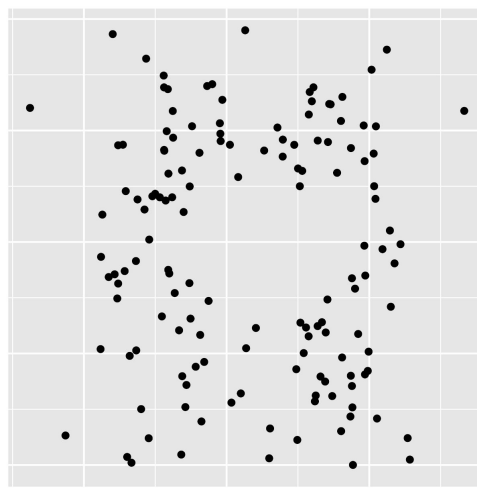
Summary Statistics

Mean(X)	54.26
Mean(Y)	47.83
Std.Dev(X)	16.76
Std.Dev(Y)	26.93
Correlation	-0.06



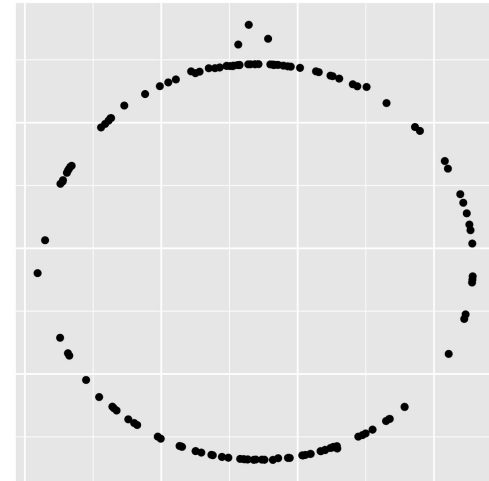
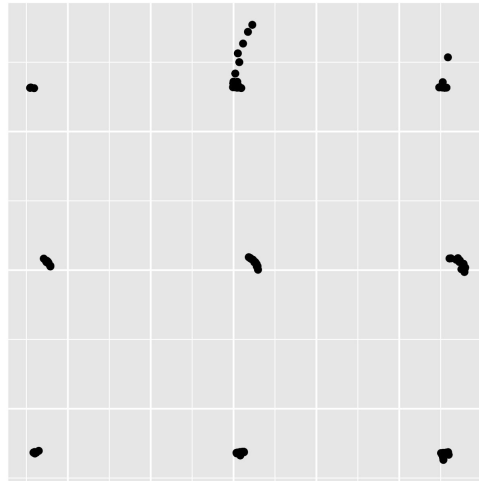
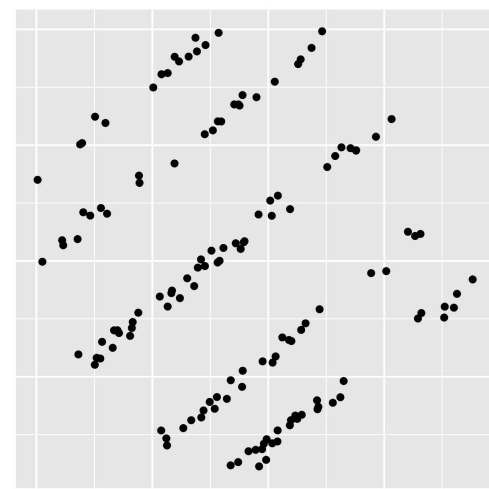
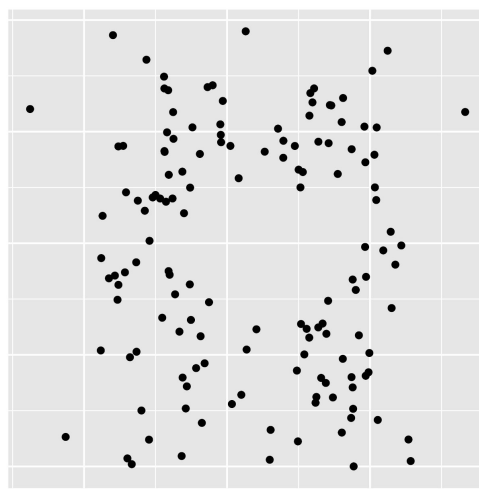
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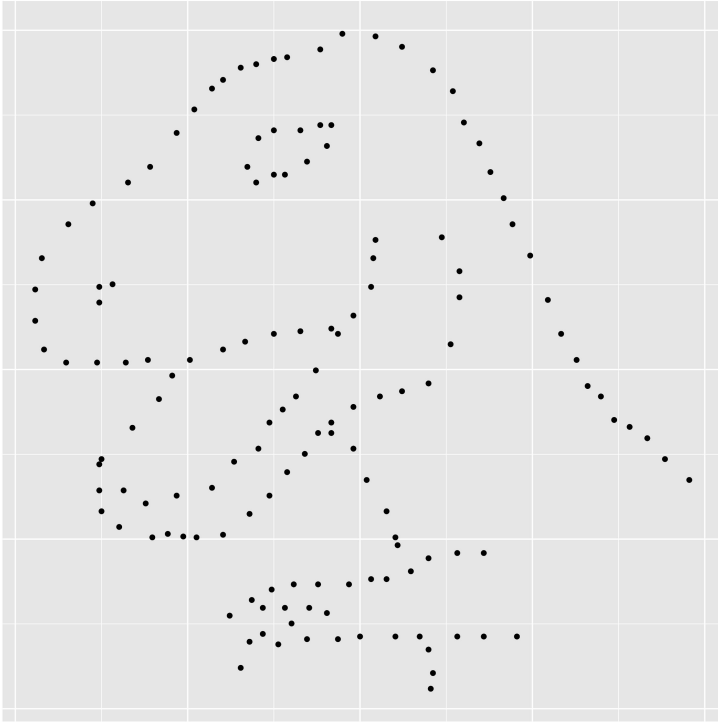


Summary Statistics

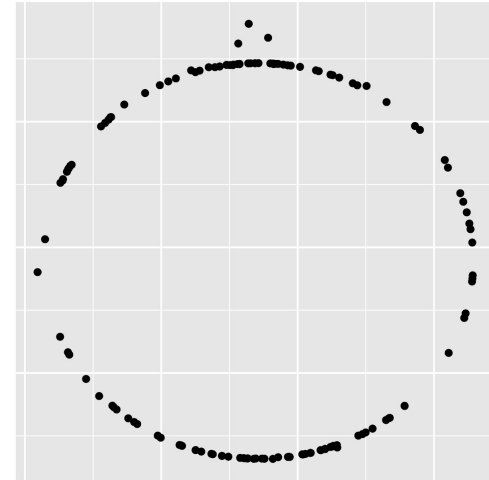
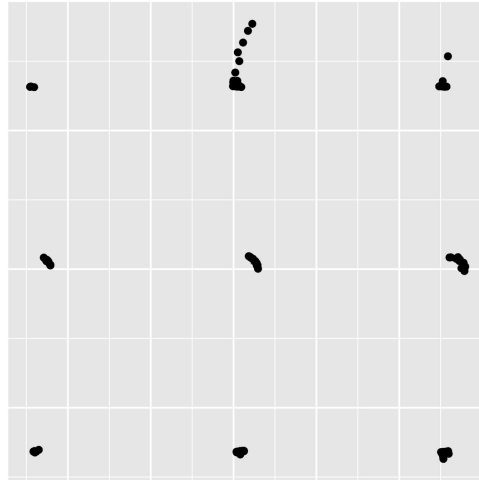
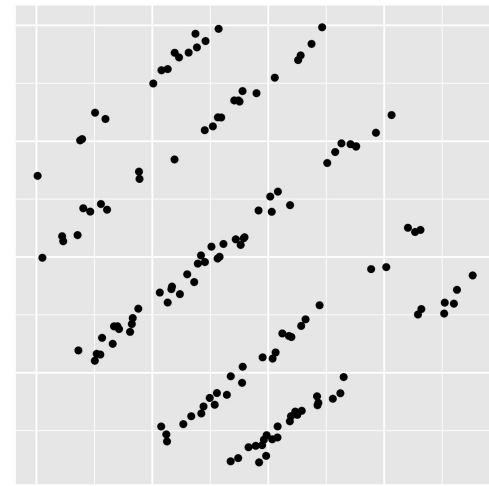
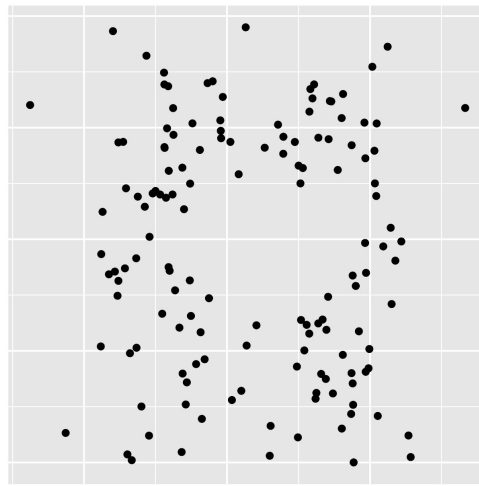
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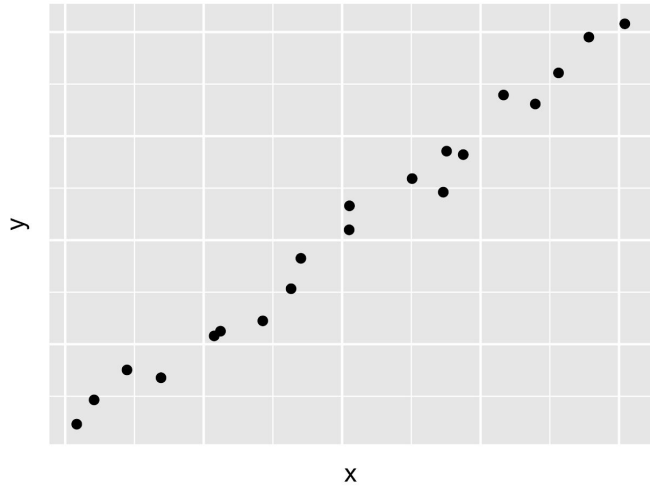


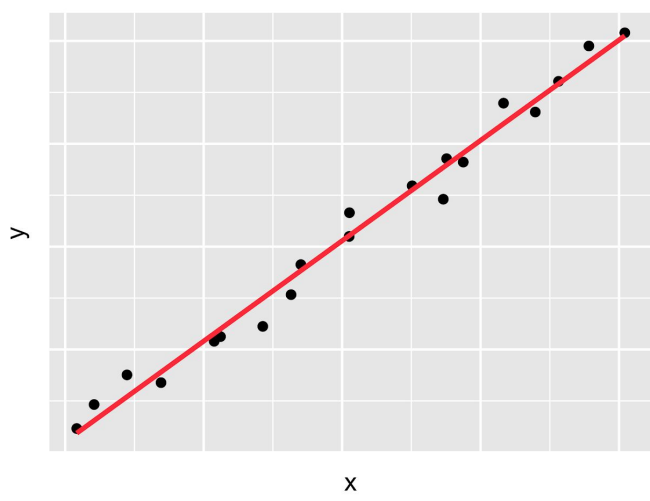
Summary Statistics

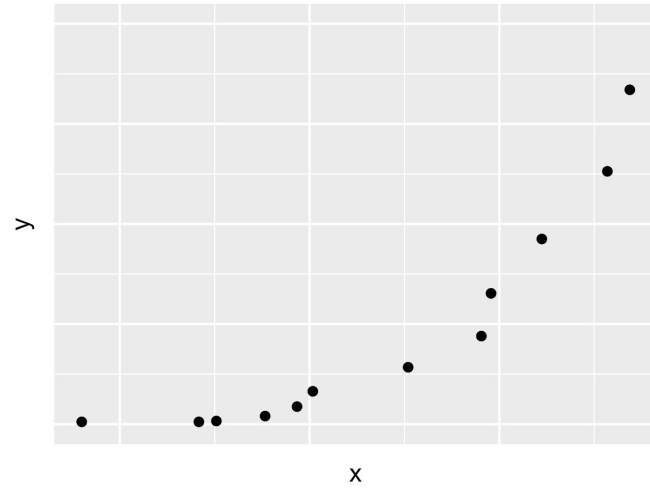
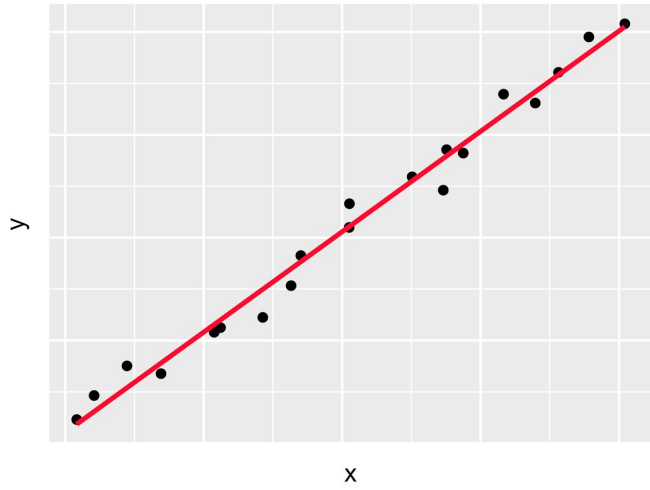


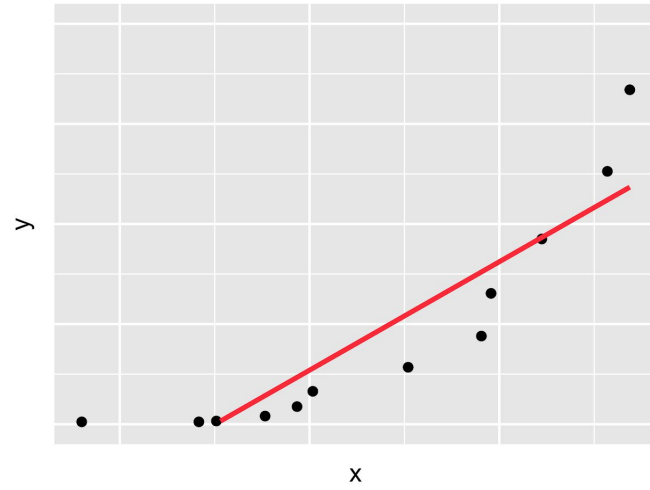
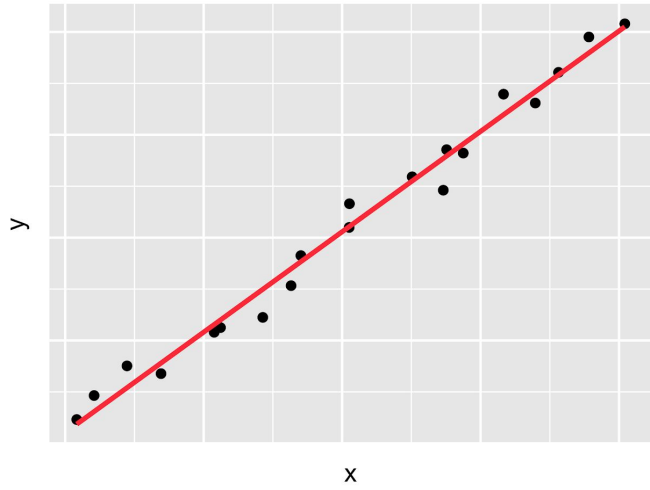
Datasaurus Dozen, Alberto Cairo

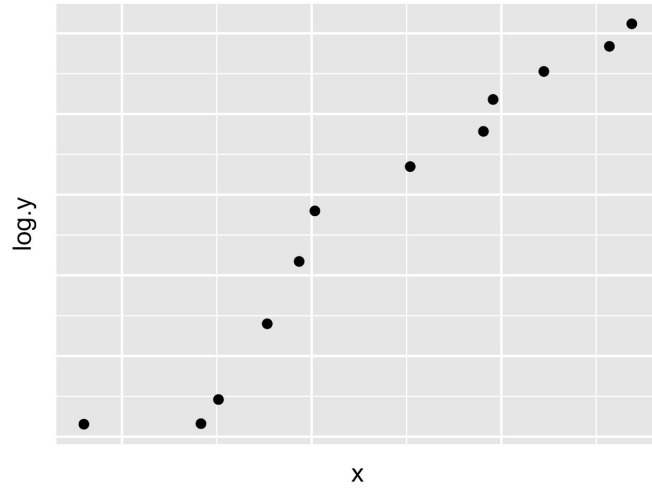
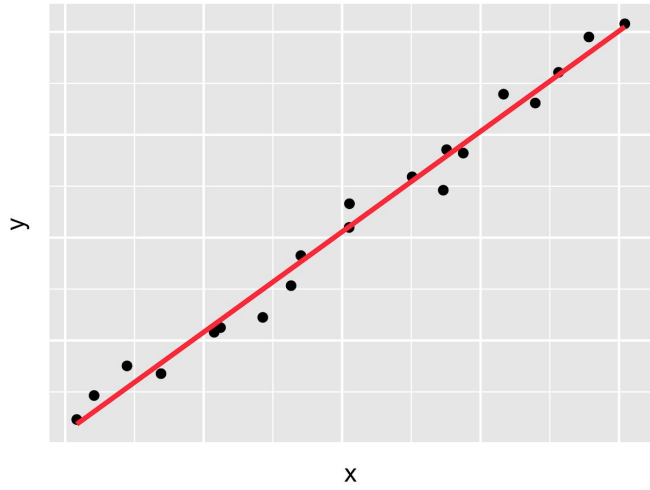


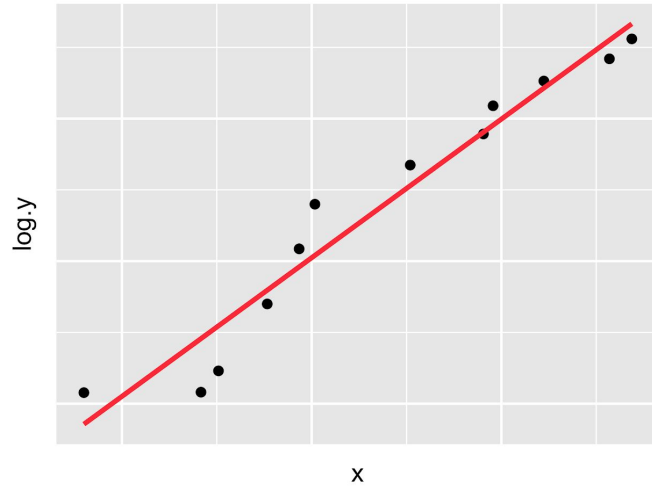
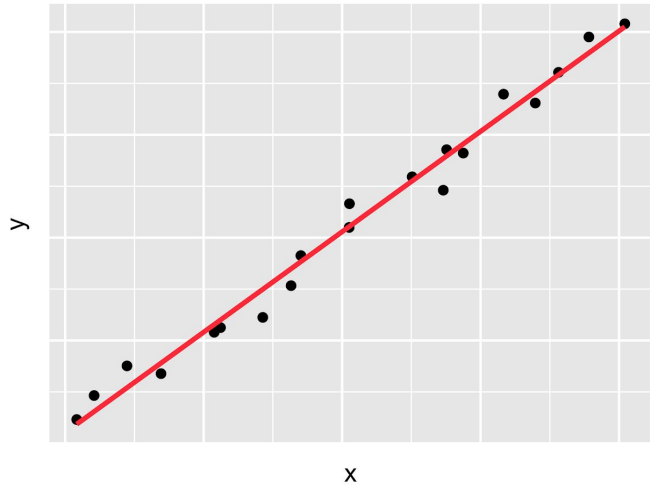


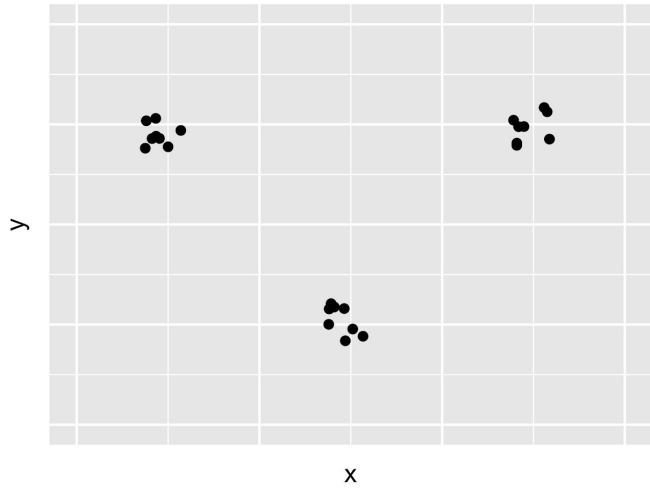
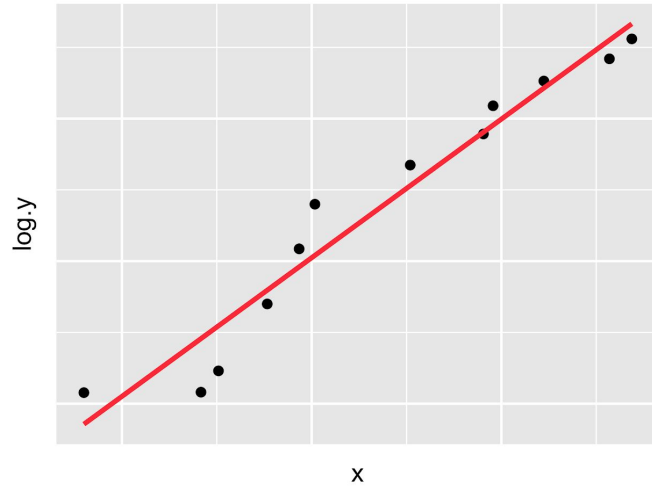
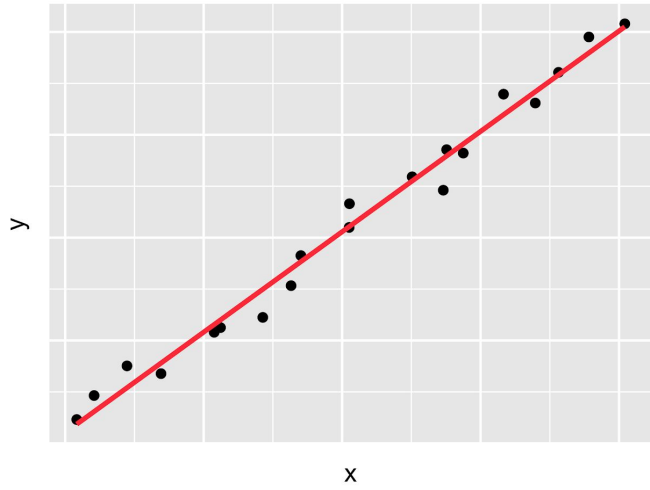


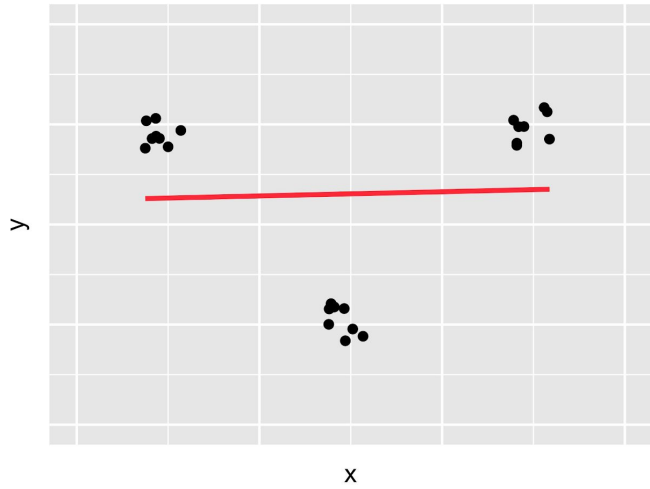
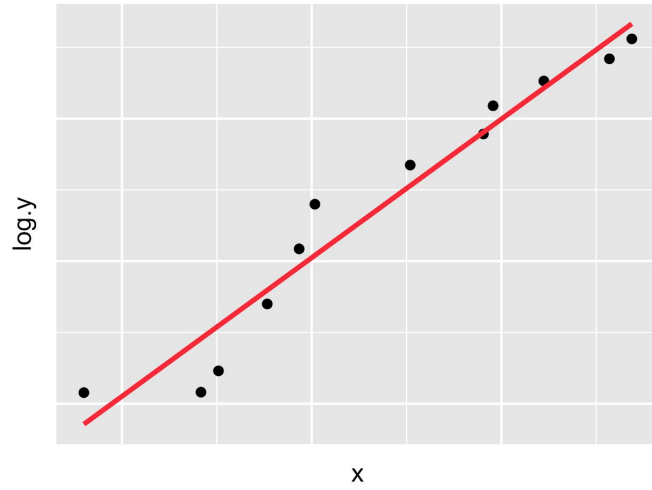
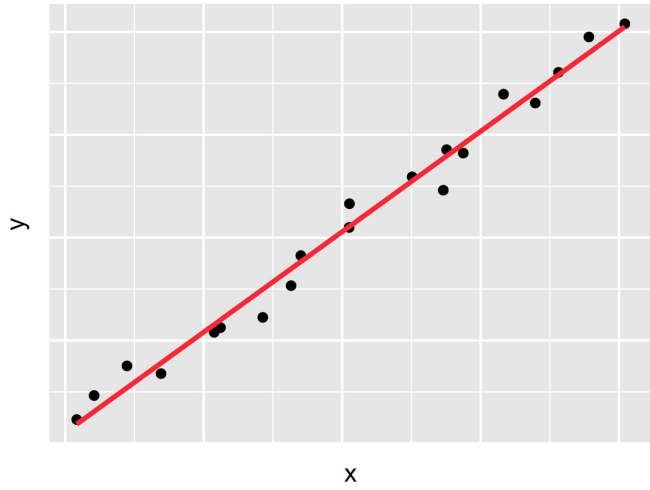


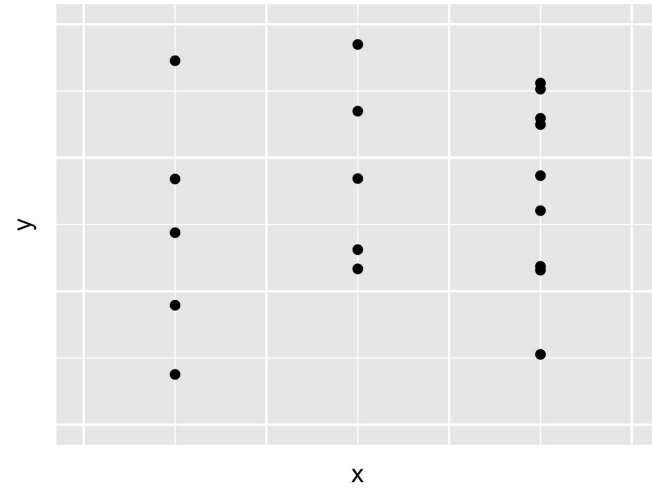
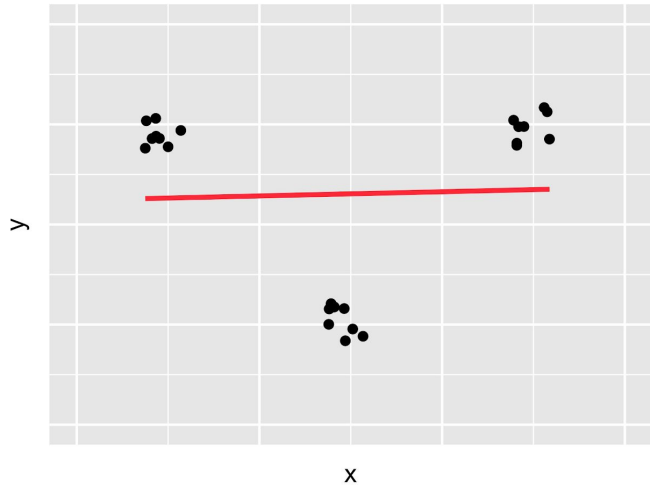
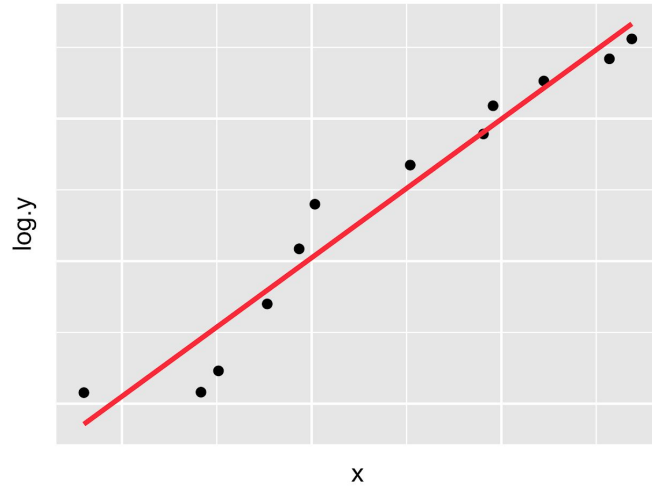
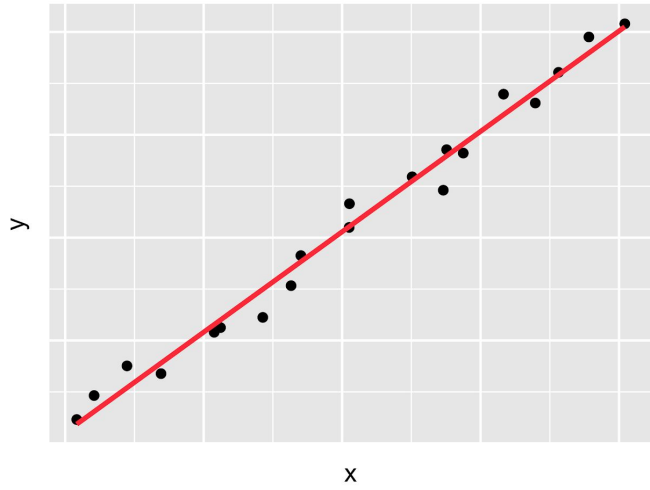


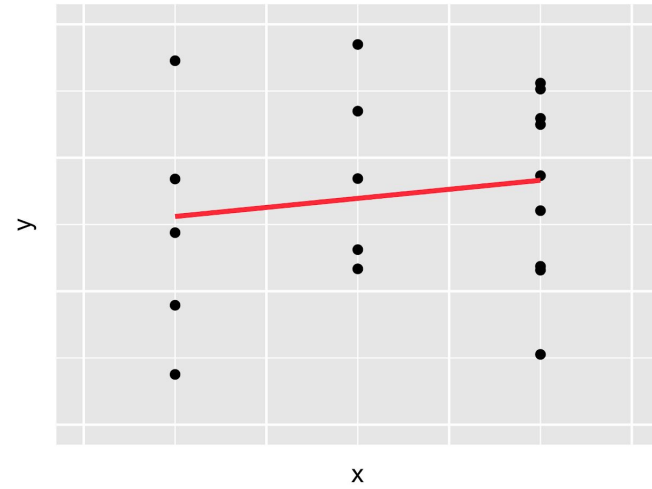
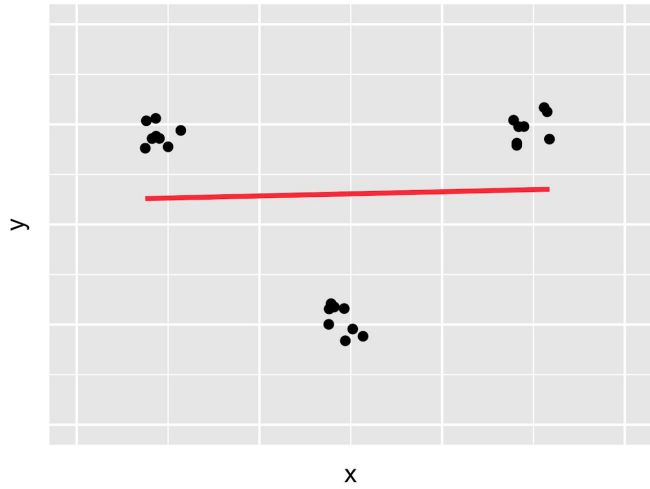
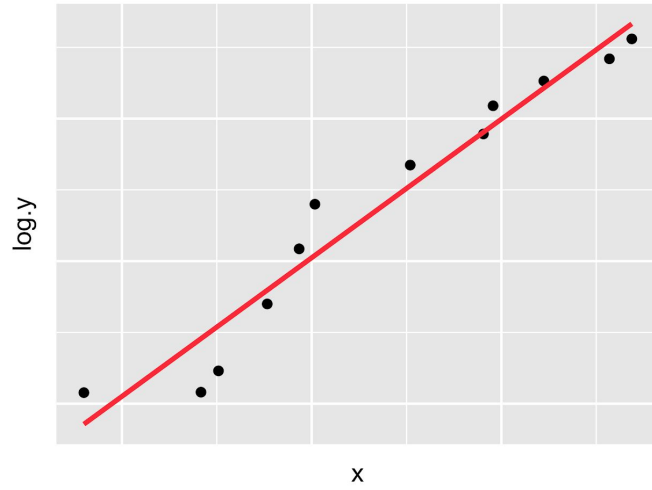
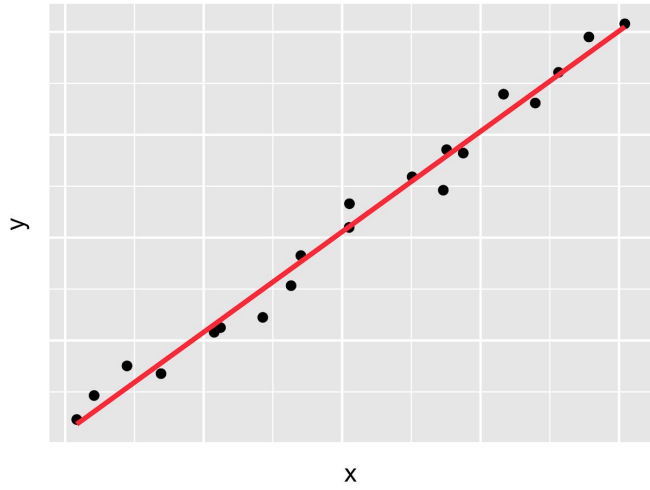




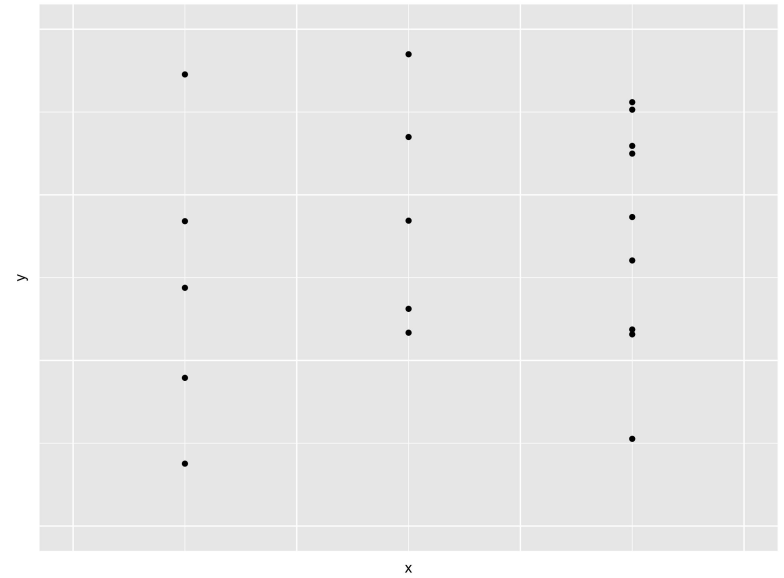
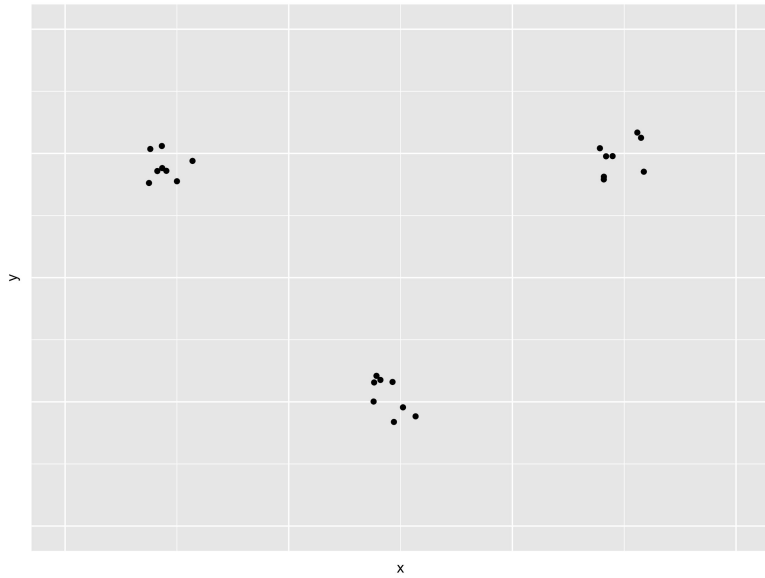






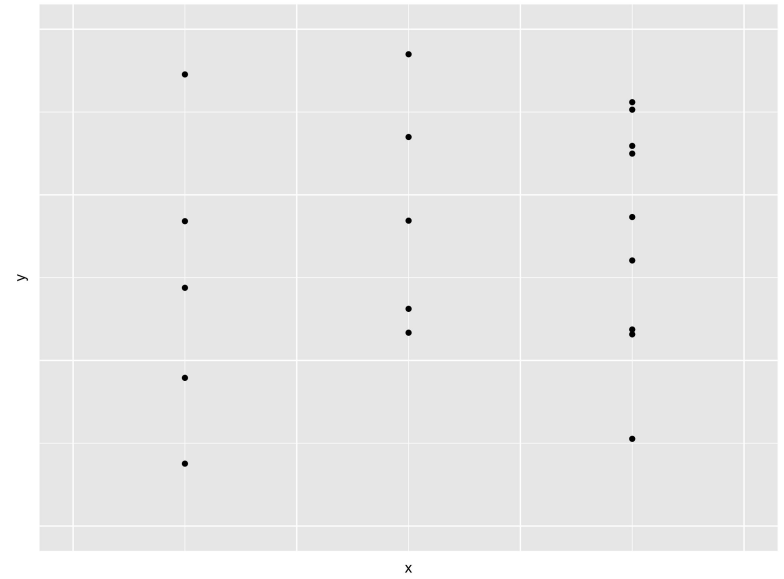
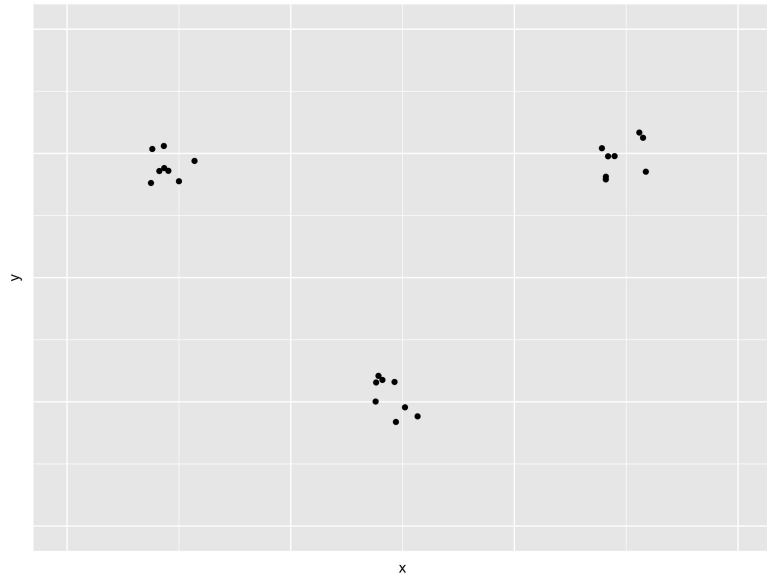


How would you approach this problem?



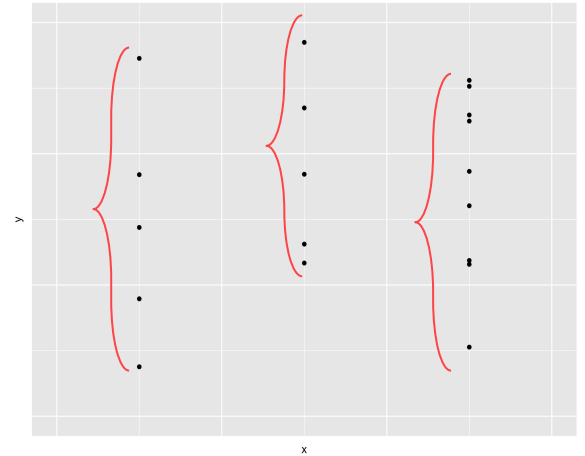
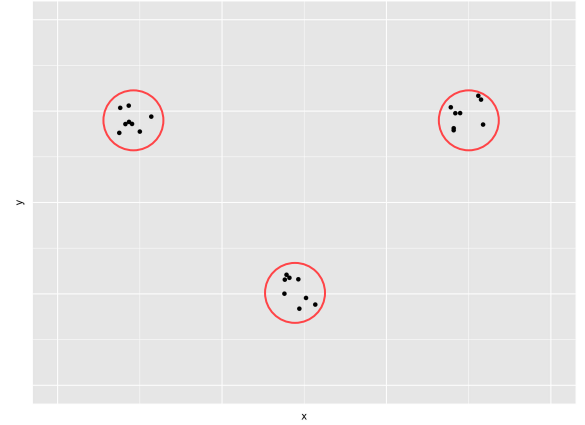
Scatterplot Diagnostics

Patterns



Scagnostics

- Tukey and Tukey (1985) coined “scagnostics” - scatterplot diagnostics
- Further defined by Wilkinson, Anand, and Grossman (2005, 2008)



Graphs

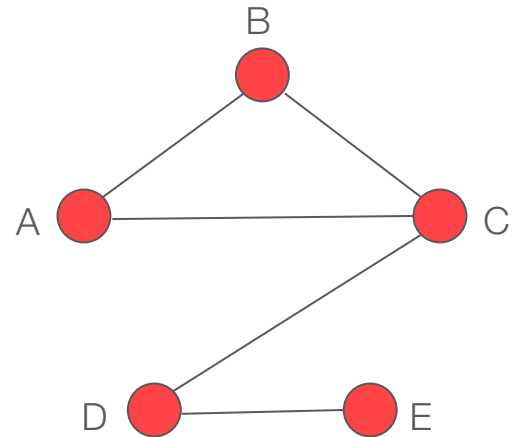
What is a geometric graph?

- A *graph* is a set of vertices V which are related by edges $e(v,w)$ in E and v,w in V
- *Geometric graphs* can be represented as points and lines in a metric space S

$$V = \{A,B,C,D,E\}$$

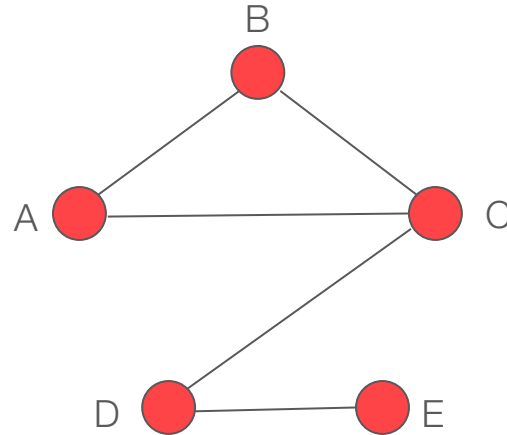
$$E = \{(A,B), (A,C), (B,C), (C,D), (D,E)\}$$

$S = 2$ dimensional space



Graphs for Scagnostics

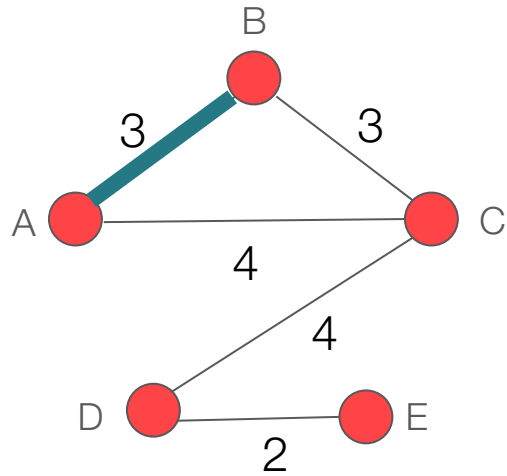
- Undirected
- Simple
- Planar
- Straight
- Finite



Graph Feature Measures

$Length(e)$ is the Euclidean distance between the vertices of an edge e

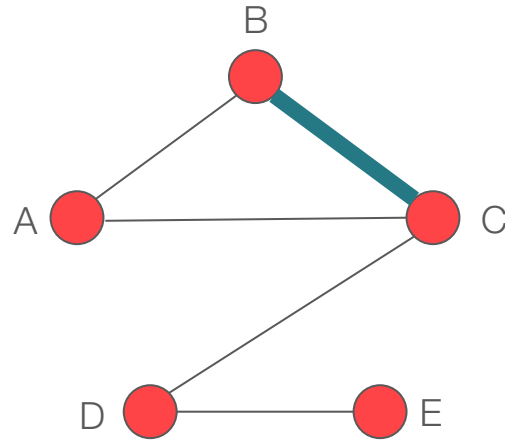
$Length(G)$ is the total length of all edges of a graph G



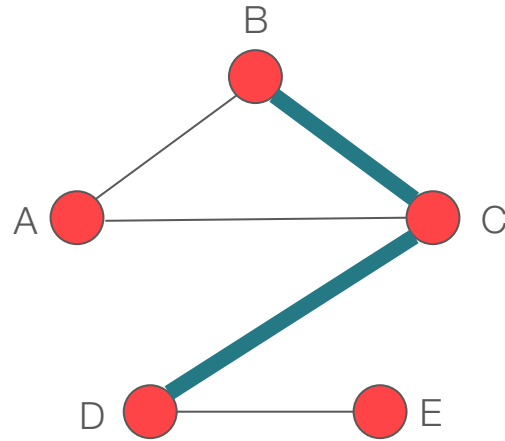
$$Length(AB) = 3$$

$$Length(G) = 3 + 3 + 4 + 4 + 2 = 16$$

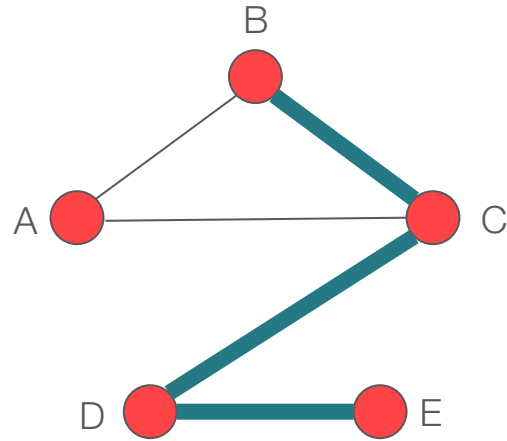
A *path* is a list of vertices such that all successive pairs are an edge



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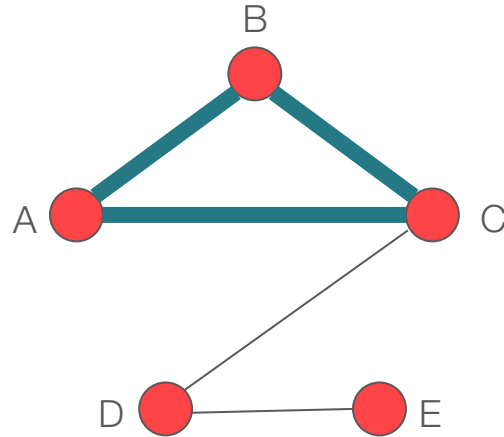


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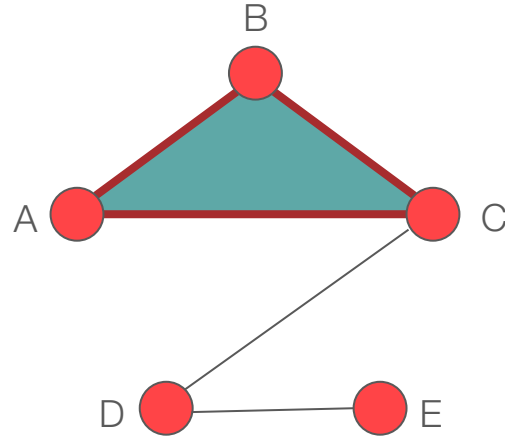
A path is *closed* if its first and last vertices are the same

A *polygon* is the boundary of a closed path



$Area(P)$ is the area of polygon P

$Perimeter(P)$ is the length of the boundary of polygon P .

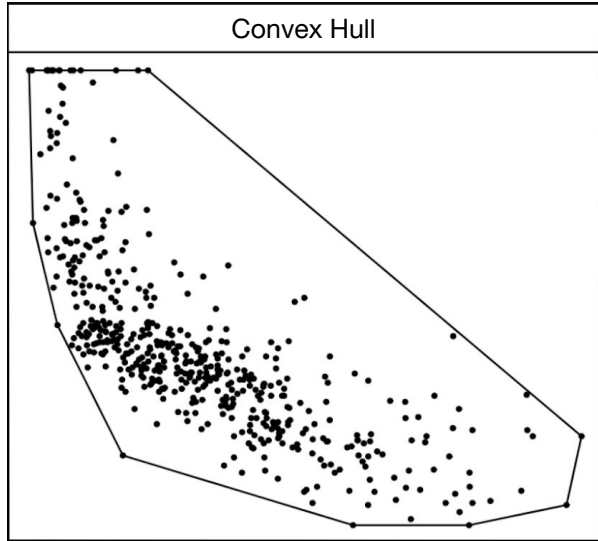


Geometric Graphs of Interest

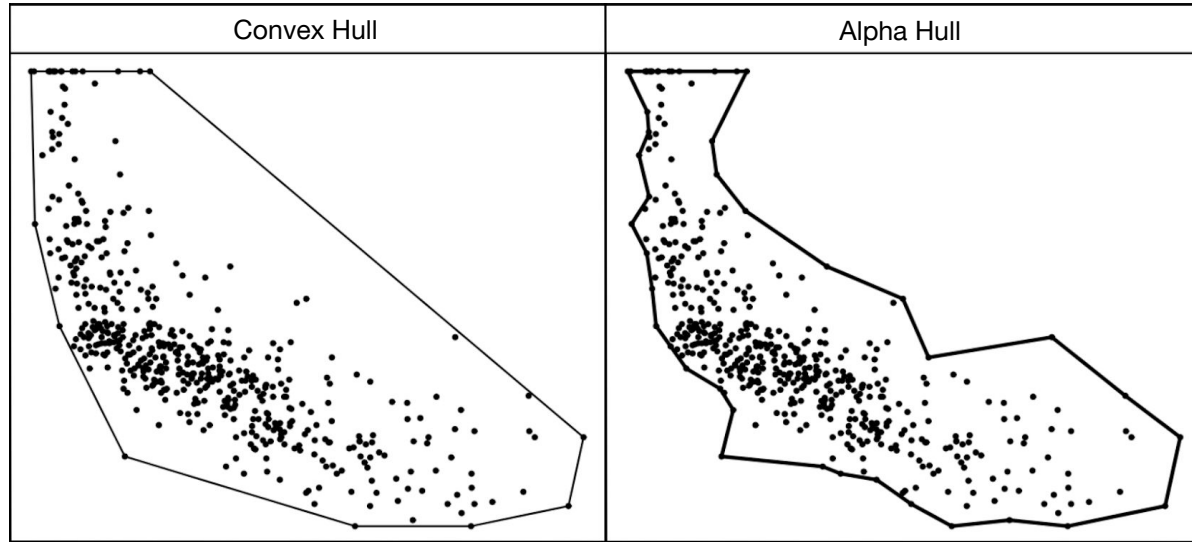
- Convex Hull
- Alpha Hull
- Minimum Spanning Tree



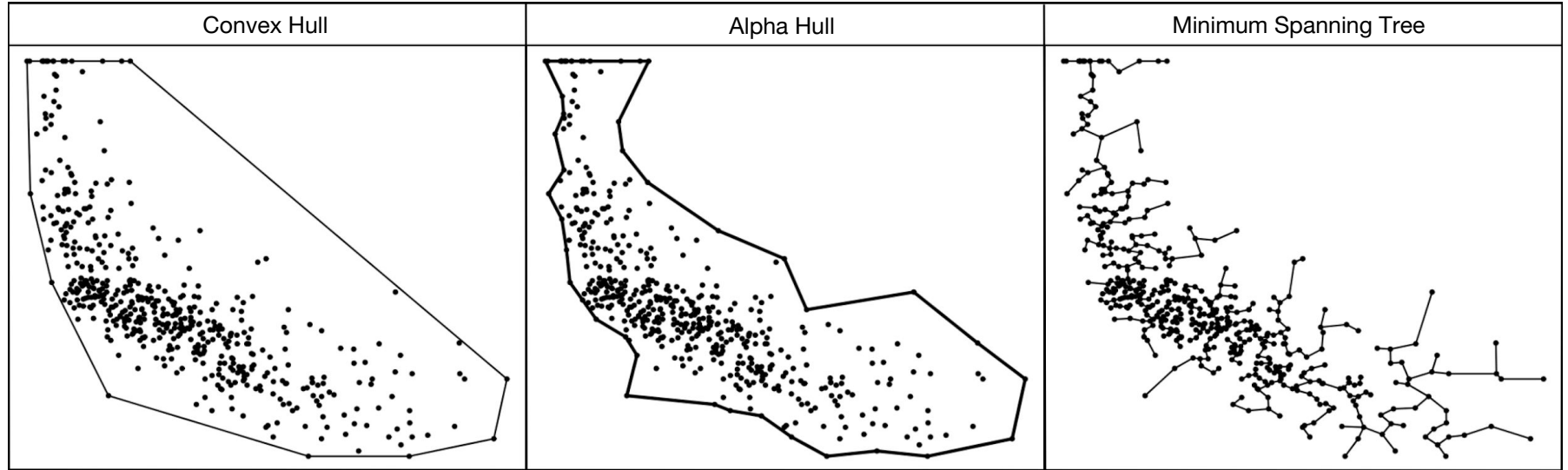
Convex Hull



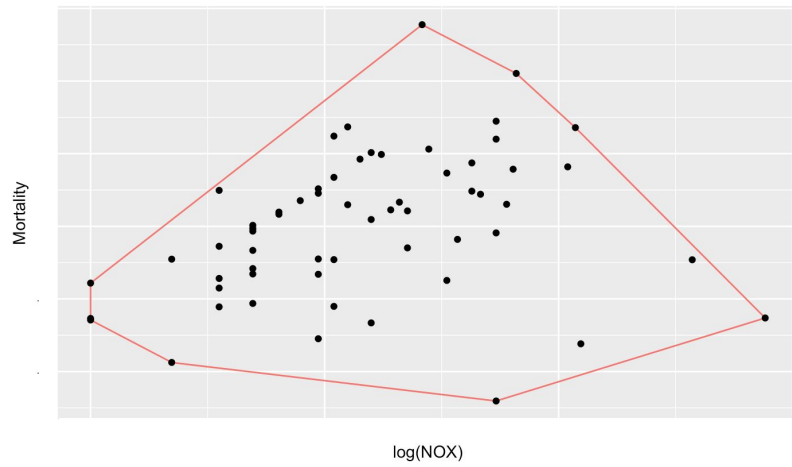
Alpha Hull



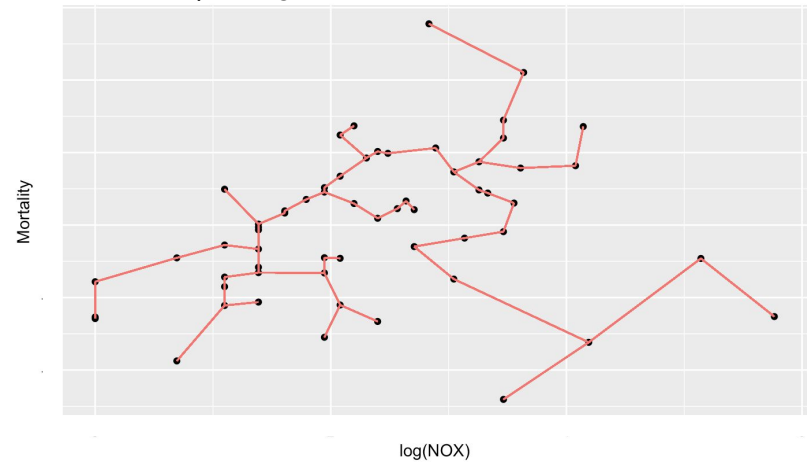
Minimum Spanning Tree



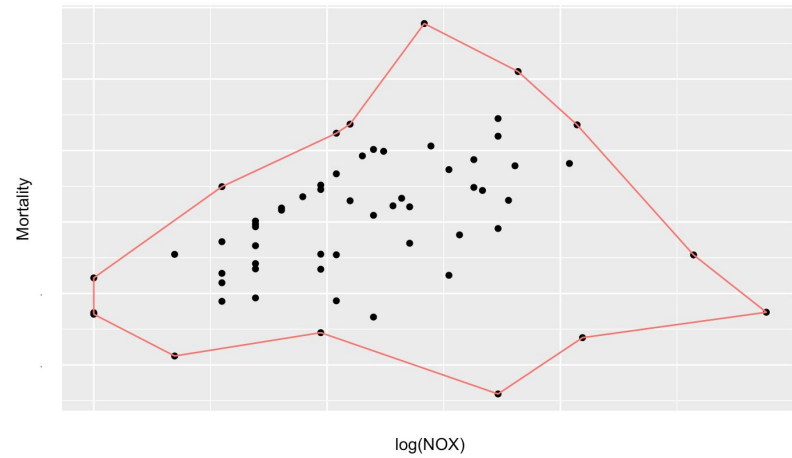
Convex Hull



Minimum Spanning Tree

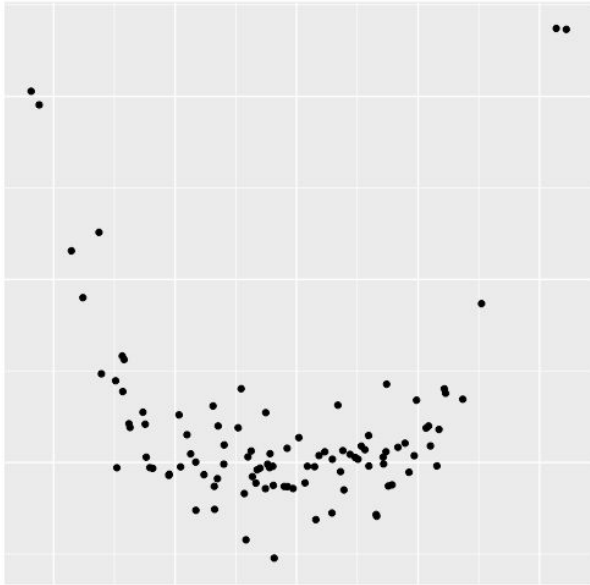


Alpha Hull

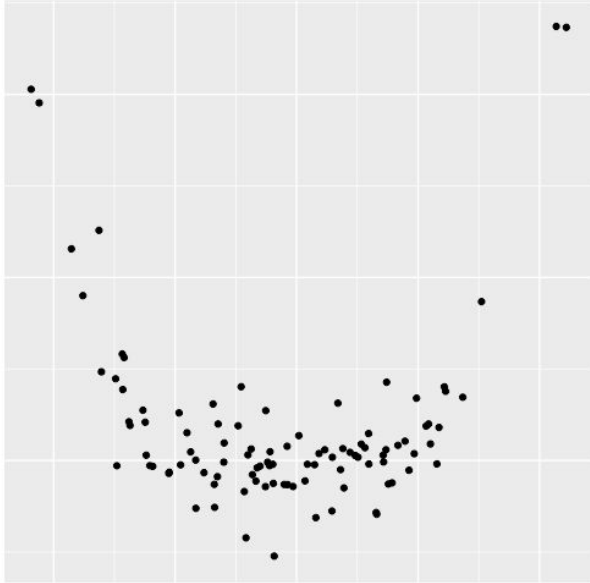


Calculating Scagnostics

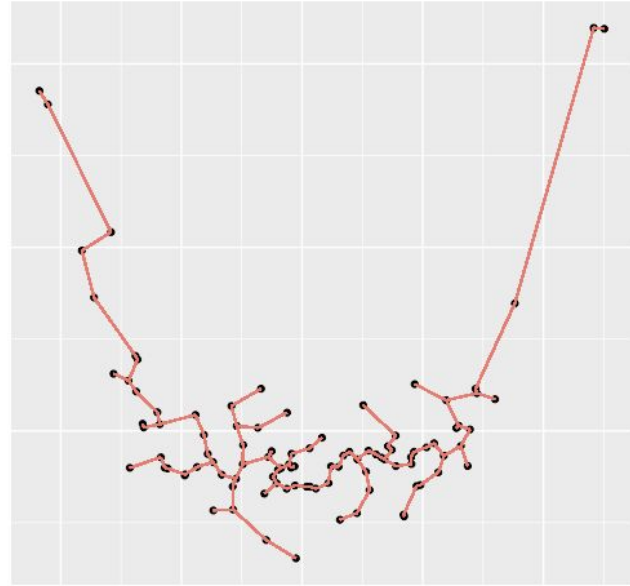
How do we quantify patterns?



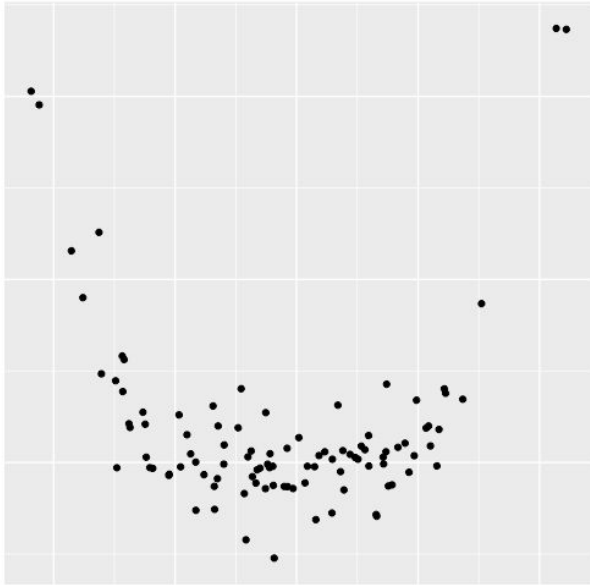
Suppose we want to measure how “stringy” a plot is



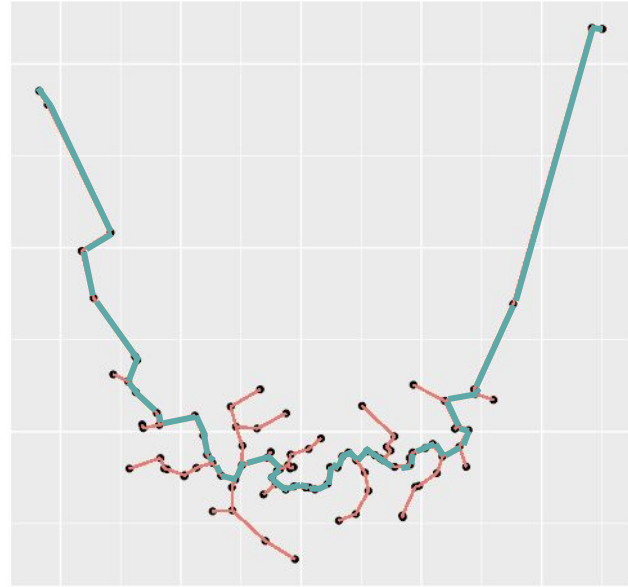
Minimum Spanning Tree



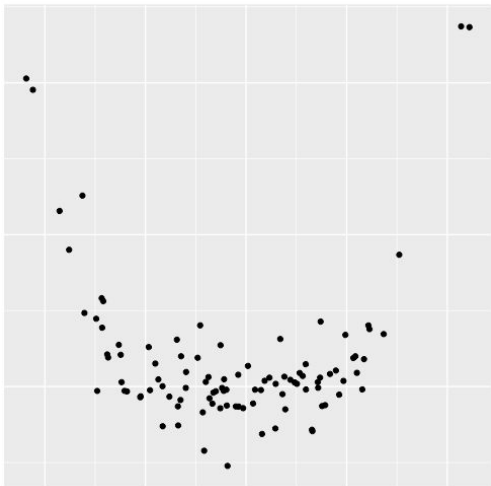
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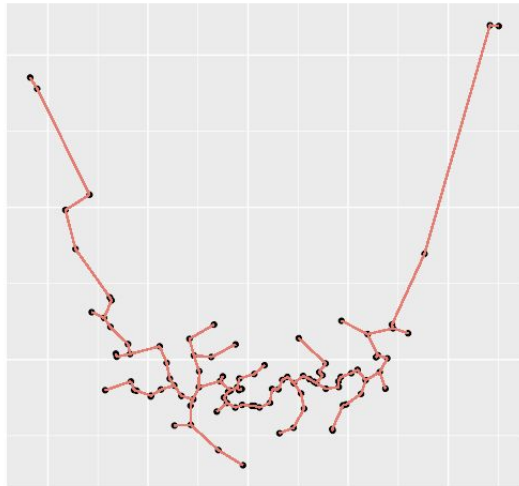
Minimum Spanning Tree



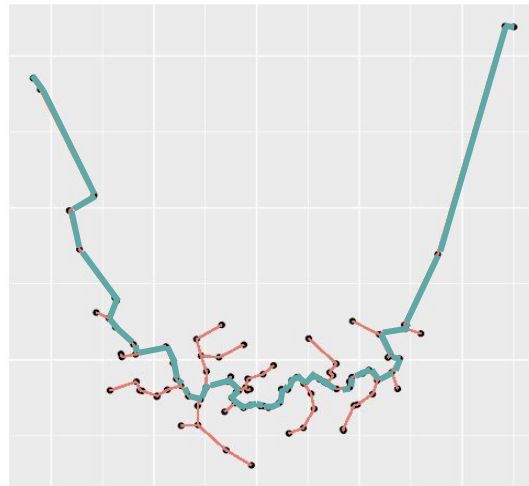
$$C_{stringy} = \frac{\text{diameter}(T)}{\text{length}(T)}$$



Minimum Spanning Tree



Diameter



Scagnostic Measures

Shape

- Stringy
- Convex
- Skinny
- Clumpy
- Striated

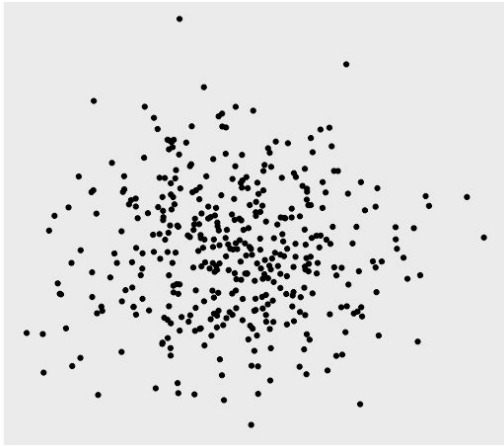
Density and Association

- Monotonic
- Outlying
- Sparse
- Skewed

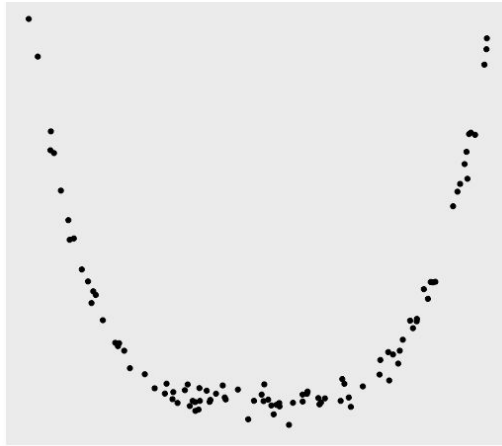
Stringy

$$C_{stringy} = \frac{\text{diameter}(T)}{\text{length}(T)}$$

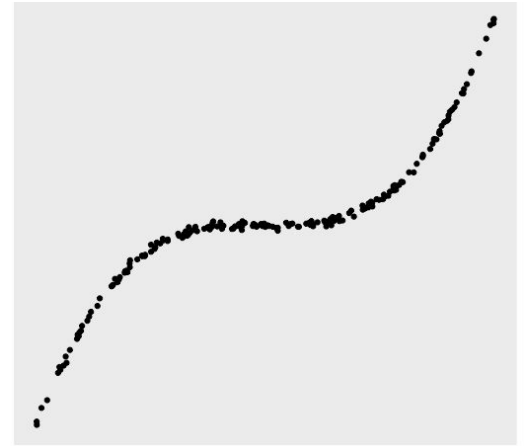
Low (0.361)



Medium (0.611)



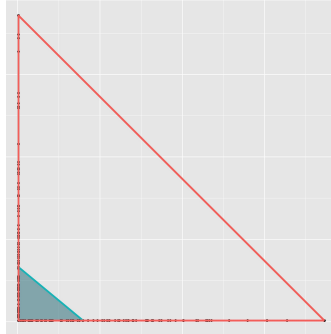
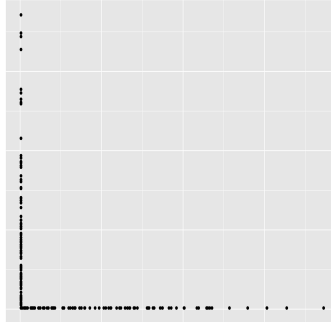
High (0.894)



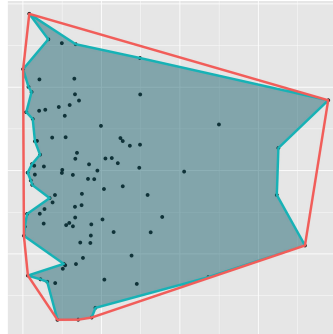
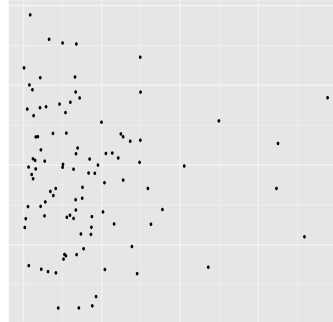
Scagnostics: Shape

$$c_{convex} = \frac{\text{area}(A)}{\text{area}(H)}$$

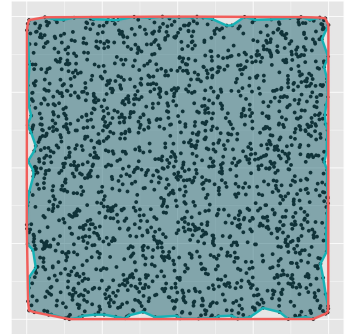
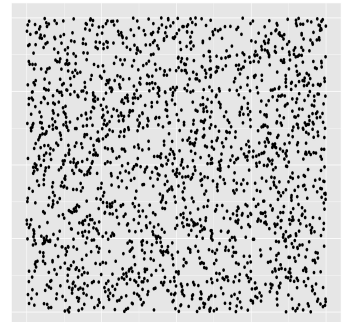
Low (0.004)



Medium (0.507)



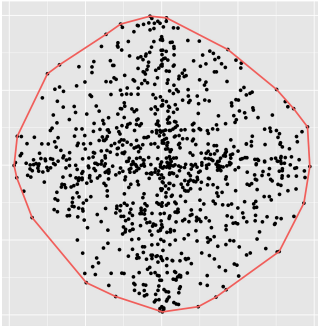
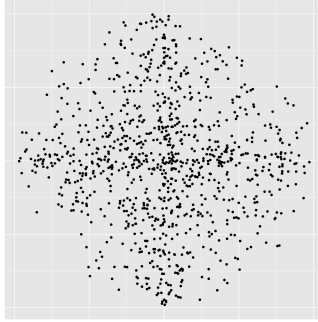
High (0.689)



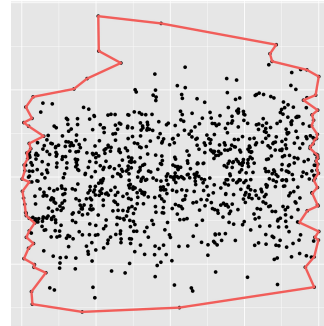
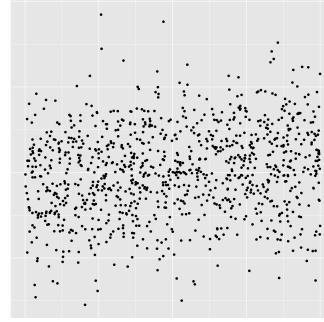
Scagnostics: Shape

$$c_{skinny} = 1 - \frac{\sqrt{4\pi area(A)}}{perimeter(A)}$$

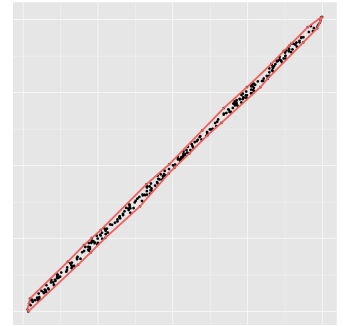
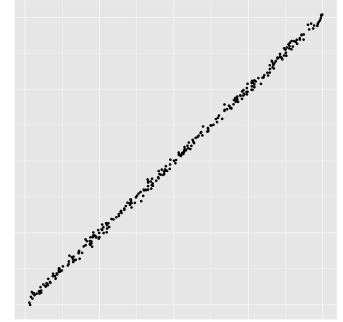
Low (0.004)



Medium (0.507)



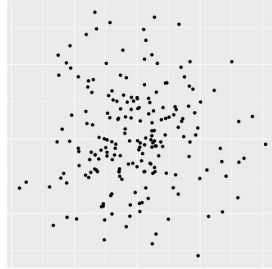
High (0.839)



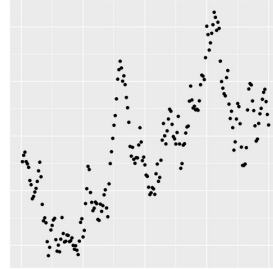
Scagnostics: Association

$$C_{monotonic} = r_{spearman}^2$$

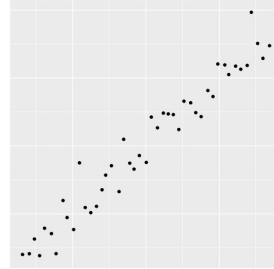
Low (0.001)



Medium (0.506)

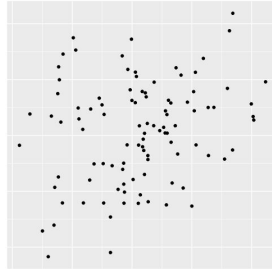


High (0.948)

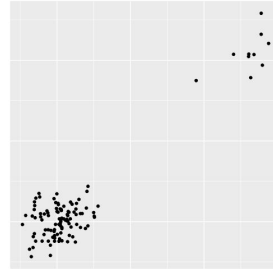


$$C_{outlying} = \frac{\text{length}(T_{outliers})}{\text{length}(T)}$$

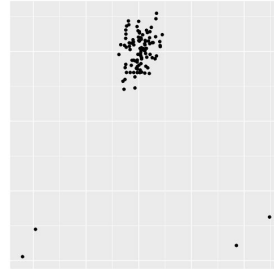
Low (0.052)



Medium (0.543)



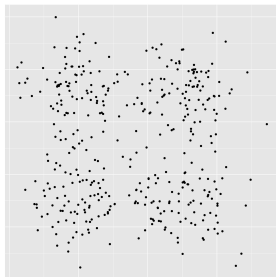
High (0.976)



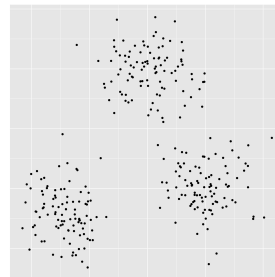
Scagnostics: Shape

$$C_{clumpy} = \max_j \left[1 - \frac{\max_k [length(e_k)]}{length(e_j)} \right]$$

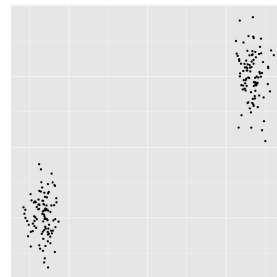
Low (0.007)



Medium (0.446)

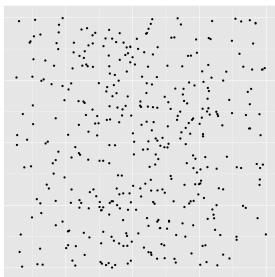


High (0.900)



$$C_{striated} = \frac{1}{|V|} \sum_{v \in V^{(2)}} I(\cos \theta_{e(v,a)e(v,b)} < -.75)$$

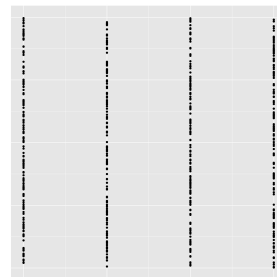
Low (0.035)



Medium (0.514)

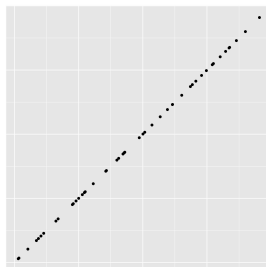


High (0.928)

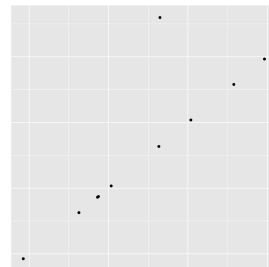


Scagnostics: Density

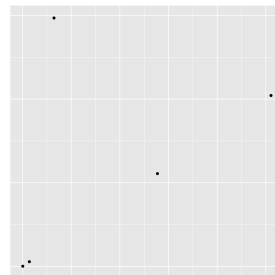
Low (0.080)



Medium (0.415)

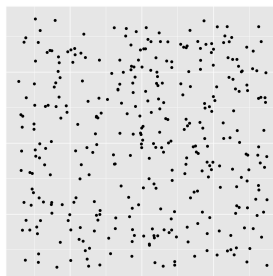


High (0.754)

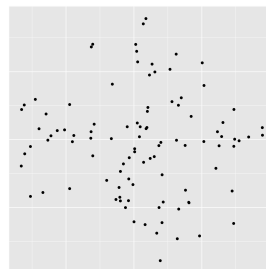


$$C_{sparse} = q_{90}(T)$$

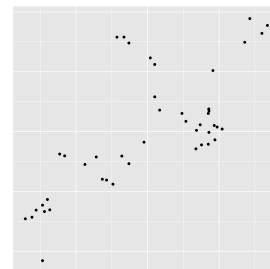
Low (0.382)



Medium (0.526)

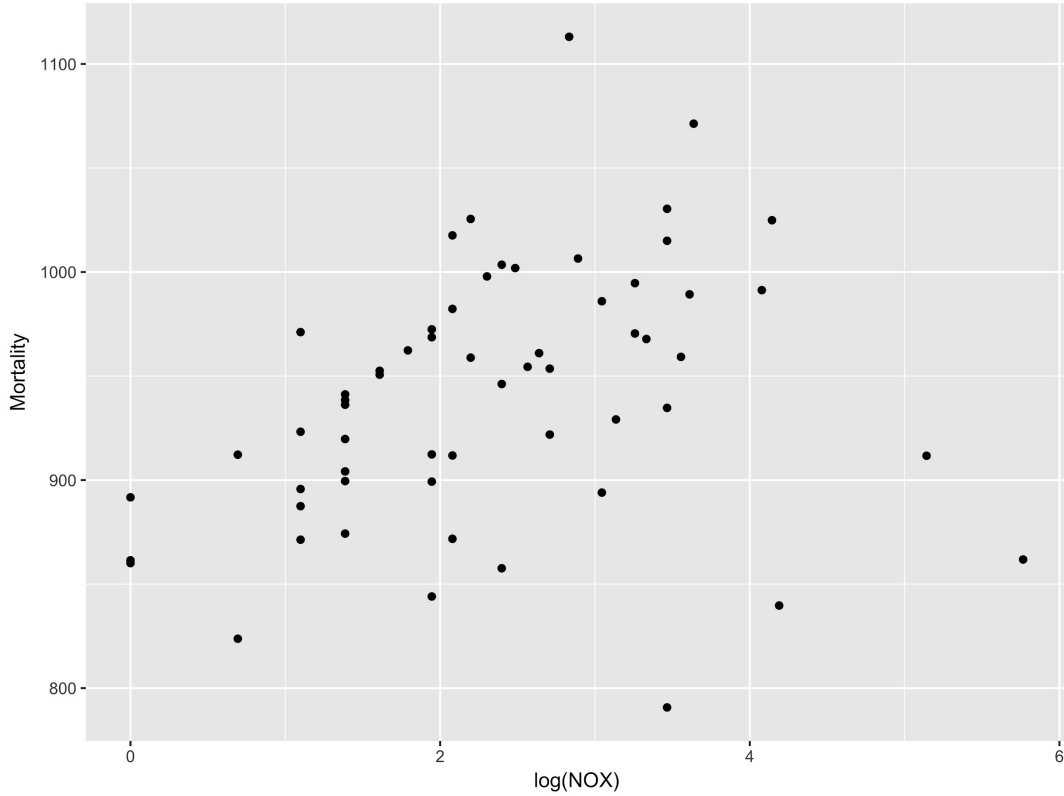


High (0.877)



$$C_{skew} = \frac{q_{90}(T) - q_{50}(T)}{q_{90}(T) - q_{10}(T)}$$

How Scagnostics Work



Outlying: 0.496

Skewed: 0.556

Clumpy: 0.038

Sparse: 0.098

Striated: 0.100

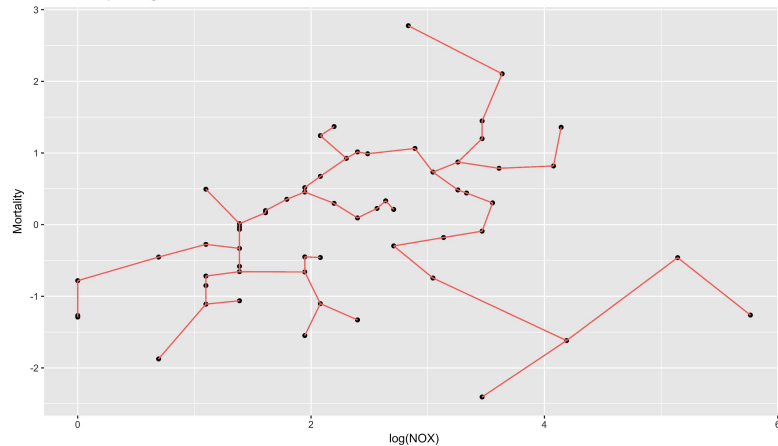
Convex: 0.718

Skinny: 0.236

Stringy: 0.521

Monotonic: 0.340

Minimal Spanning Tree



Outlying: 0.496

Skewed: 0.556

Clumpy: 0.038

Sparse: 0.098

Striated: 0.100

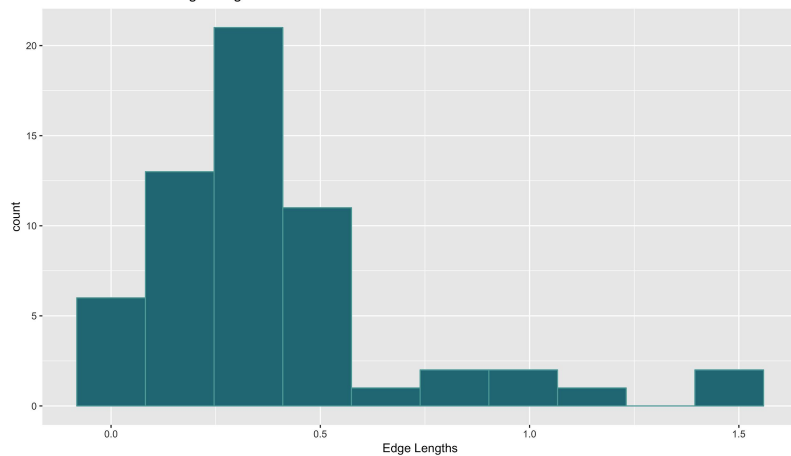
Convex: 0.718

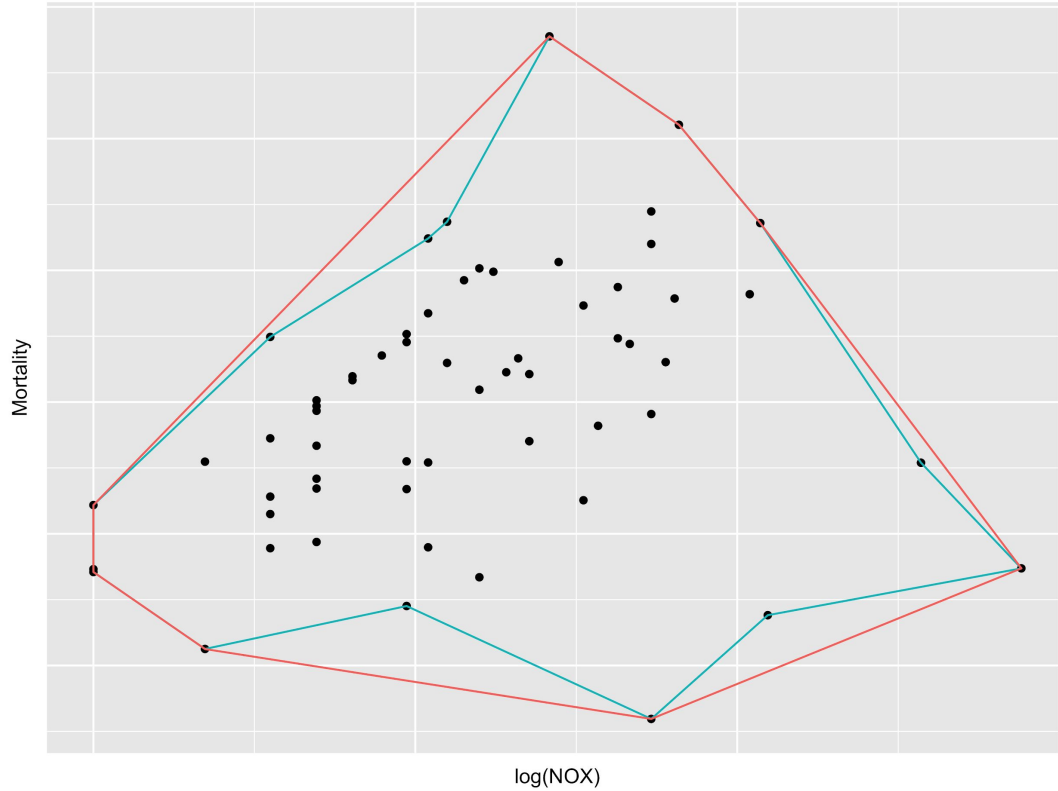
Skinny: 0.236

Stringy: 0.521

Monotonic: 0.340

Distribution of MST Edge Lengths





Outlying: 0.496

Skewed: 0.556

Clumpy: 0.038

Sparse: 0.098

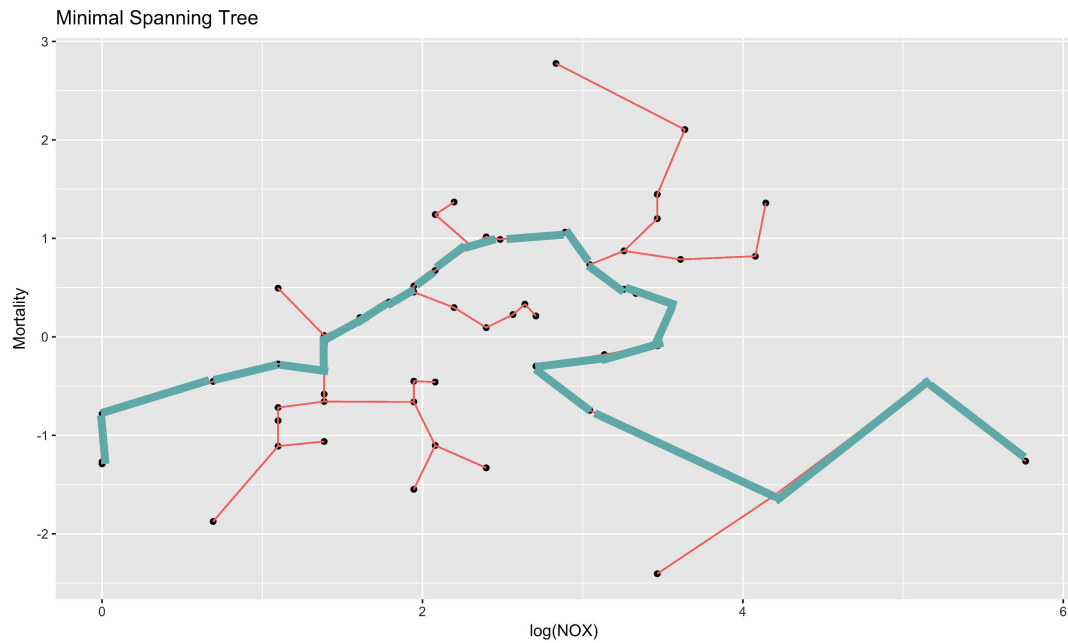
Striated: 0.100

Convex: 0.718

Skinny: 0.236

Stringy: 0.521

Monotonic: 0.340



Outlying: 0.496

Skewed: 0.556

Clumpy: 0.038

Sparse: 0.098

Striated: 0.100

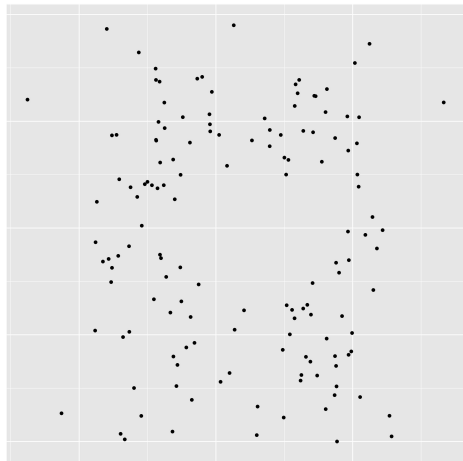
Convex: 0.718

Skinny: 0.236

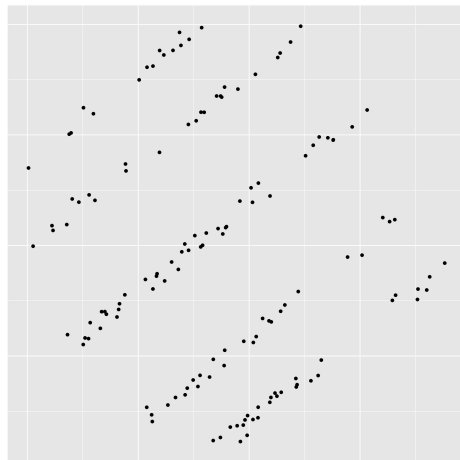
Stringy: 0.521

Monotonic: 0.340

How Scagnostics Differentiate Plots



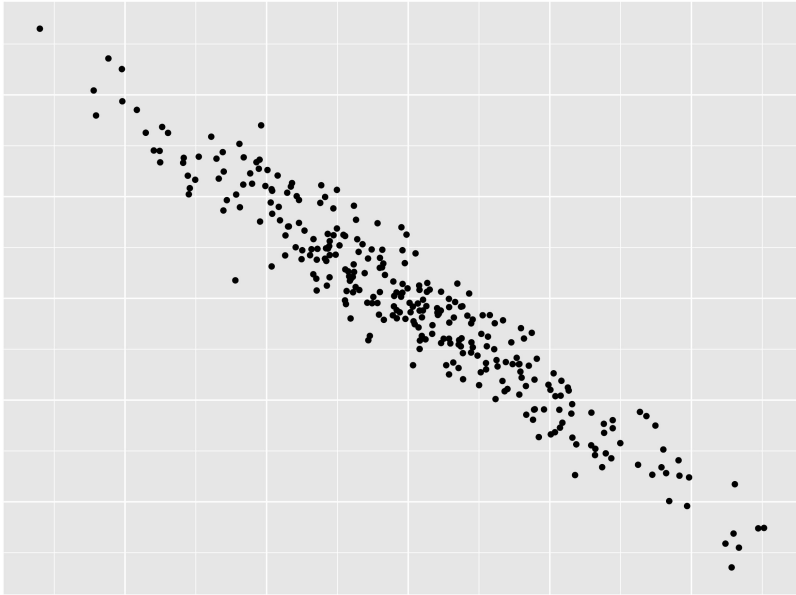
Outlying: 0.108
Skewed: 0.617
Clumpy: 0.002
Sparse: 0.078
Striated: 0.076
Convex: 0.522
Skinny: 0.571
Stringy: 0.369
Monotonic: 0.008



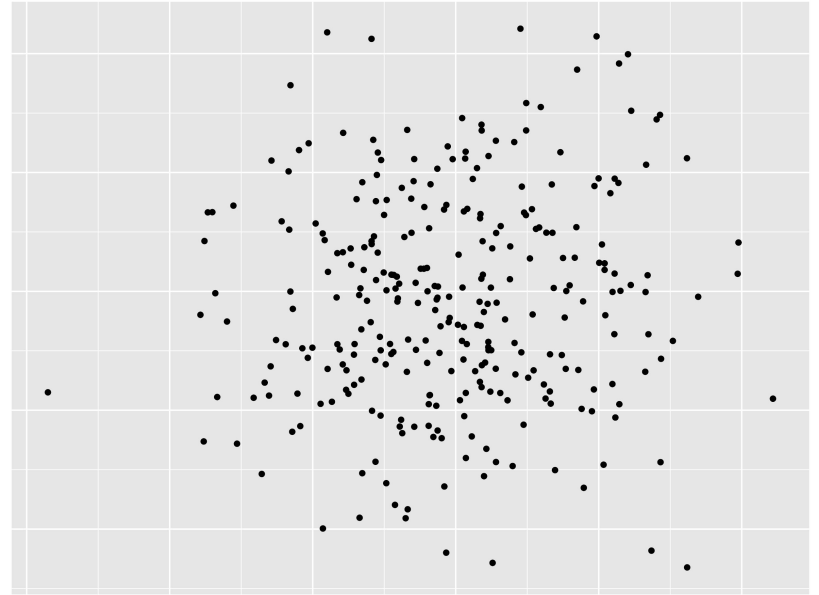
Outlying: 0.088
Skewed: 0.749
Clumpy: 0.142
Sparse: 0.067
Striated: 0.172
Convex: 0.094
Skinny: 0.838
Stringy: 0.559
Monotonic: 0.003

Building the Model

Why?



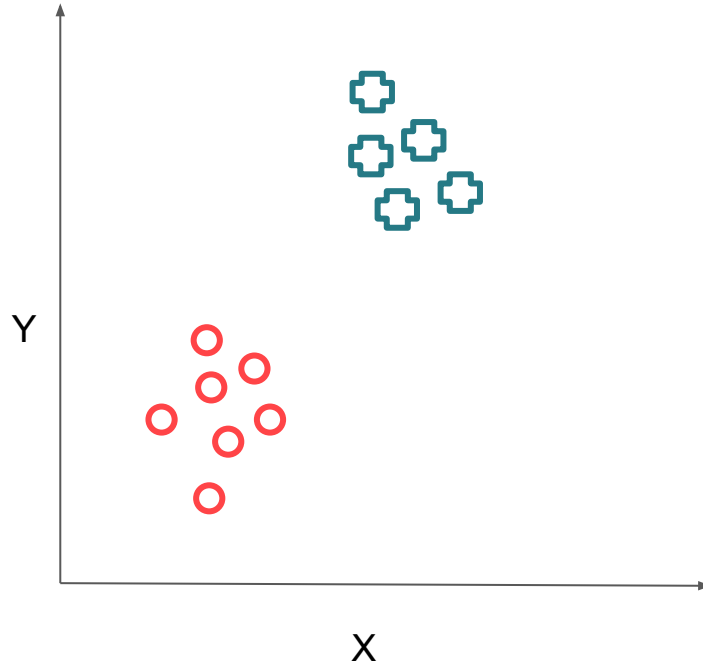
Signal



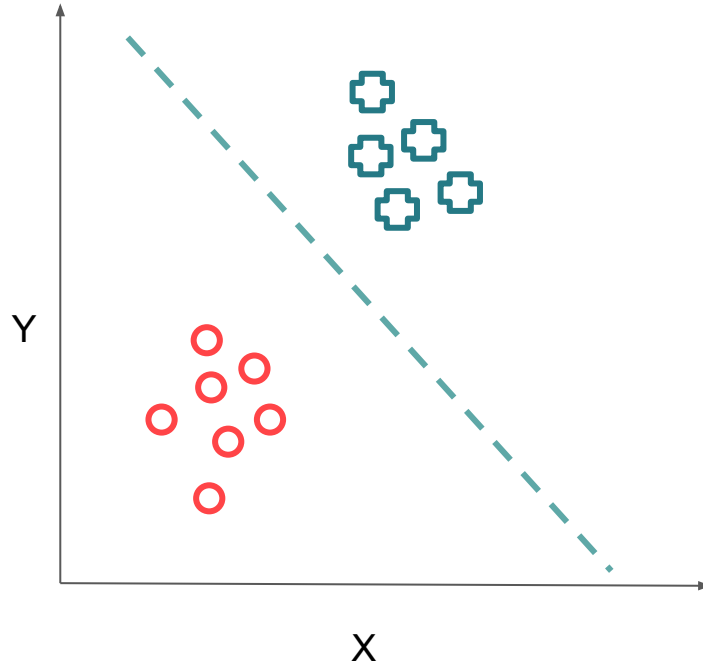
Null

Statistical Learning

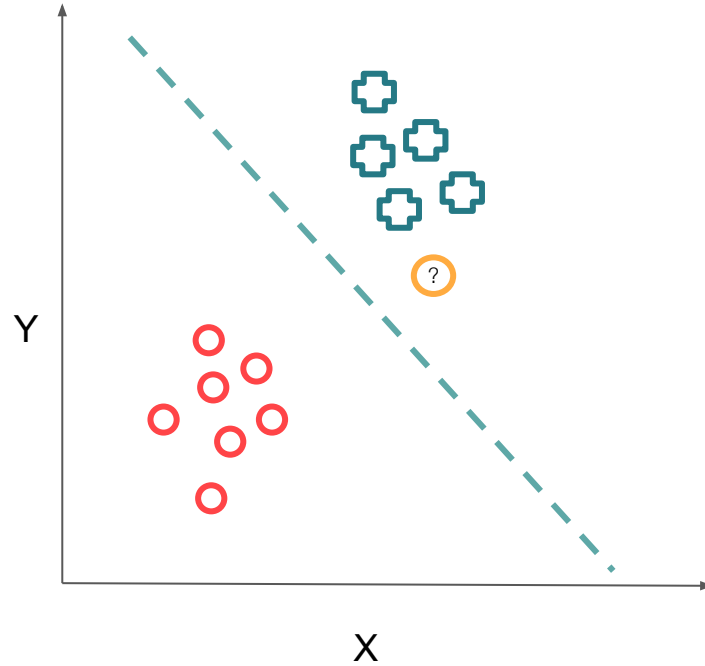
Supervised Learning



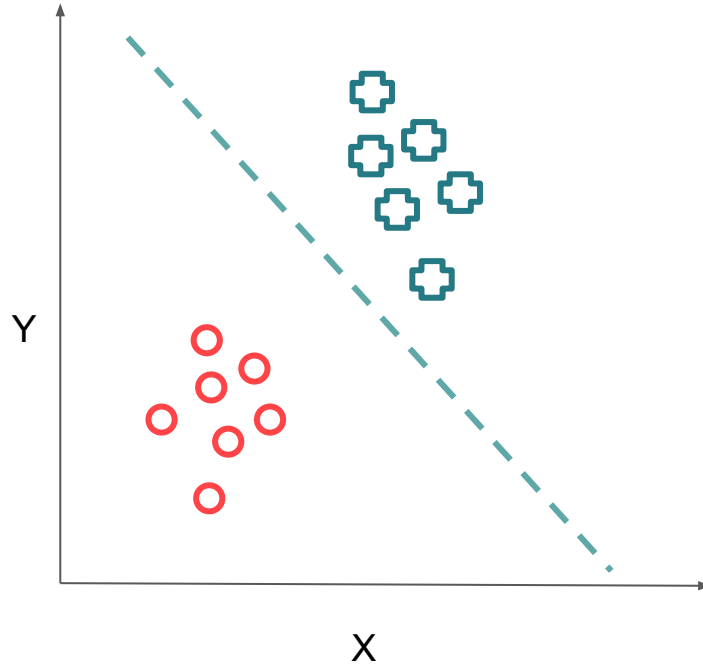
Supervised Learning



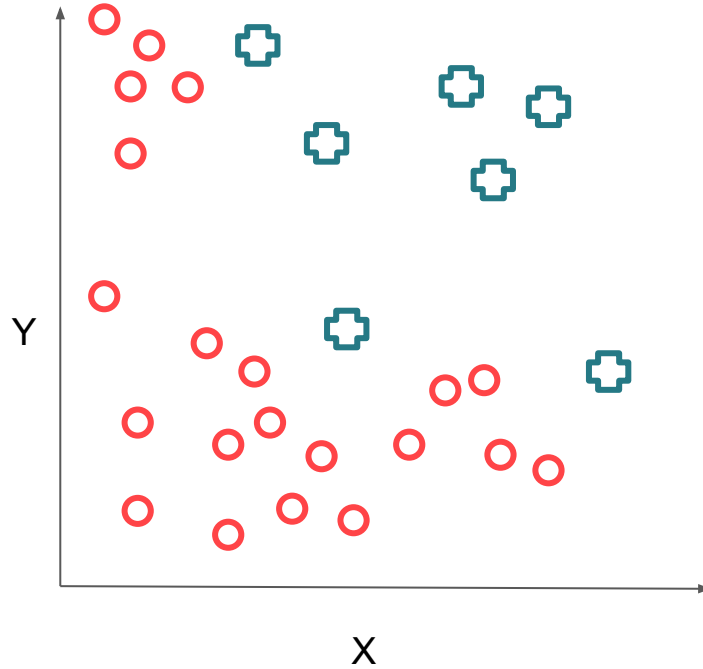
Supervised Learning



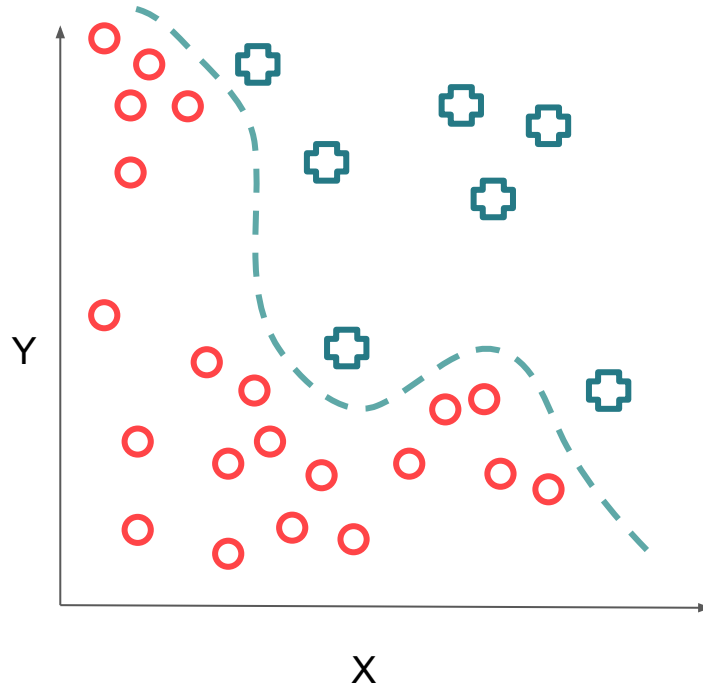
Supervised Learning



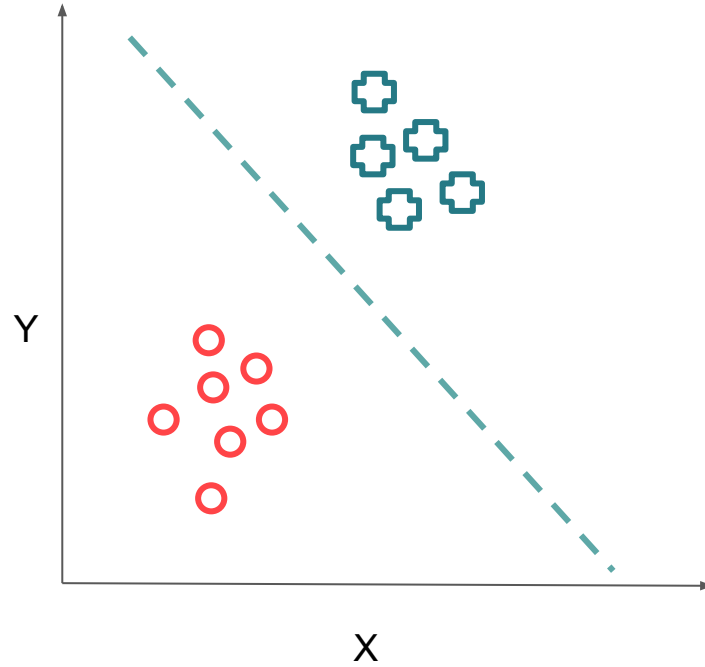
Supervised Learning



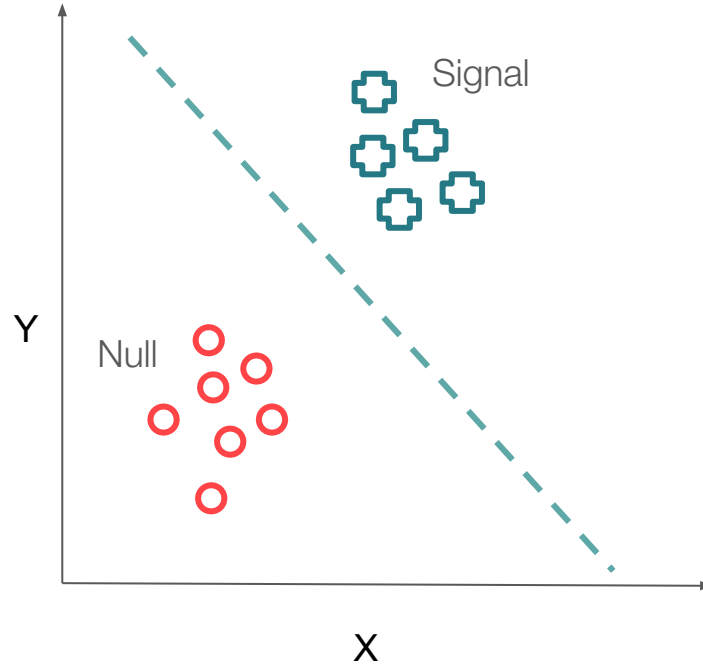
Supervised Learning



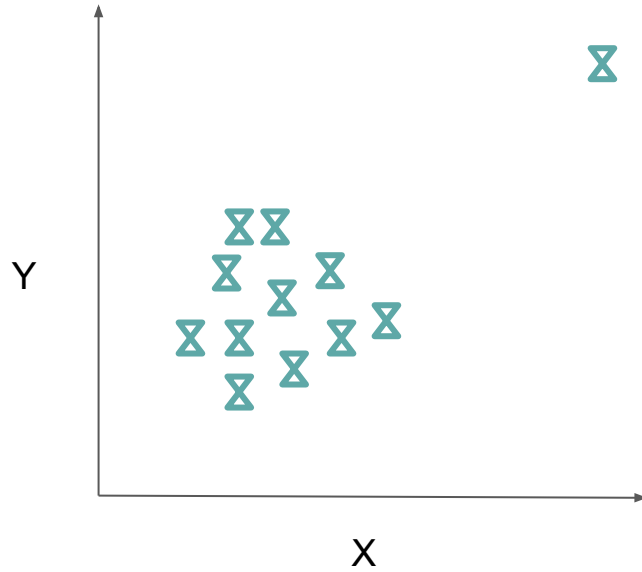
Supervised Learning



Supervised Learning

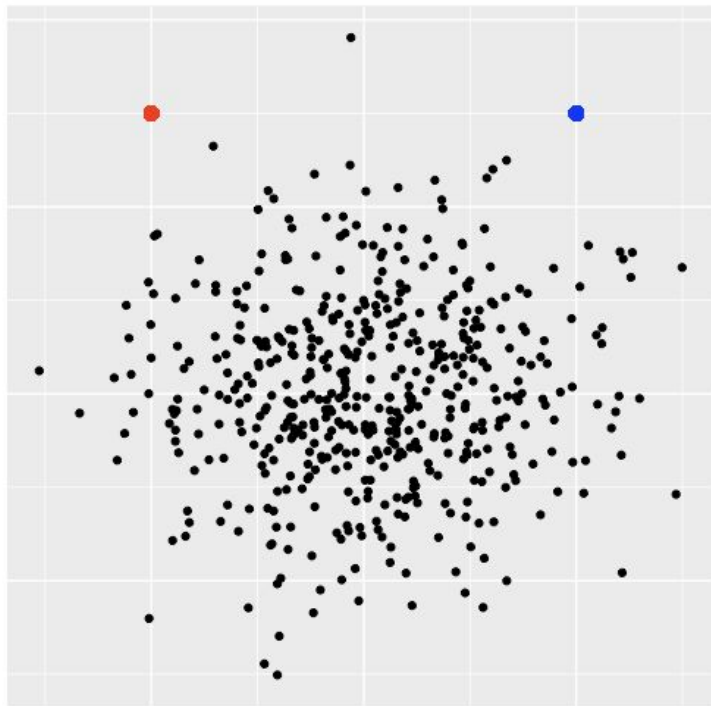


Unsupervised Learning

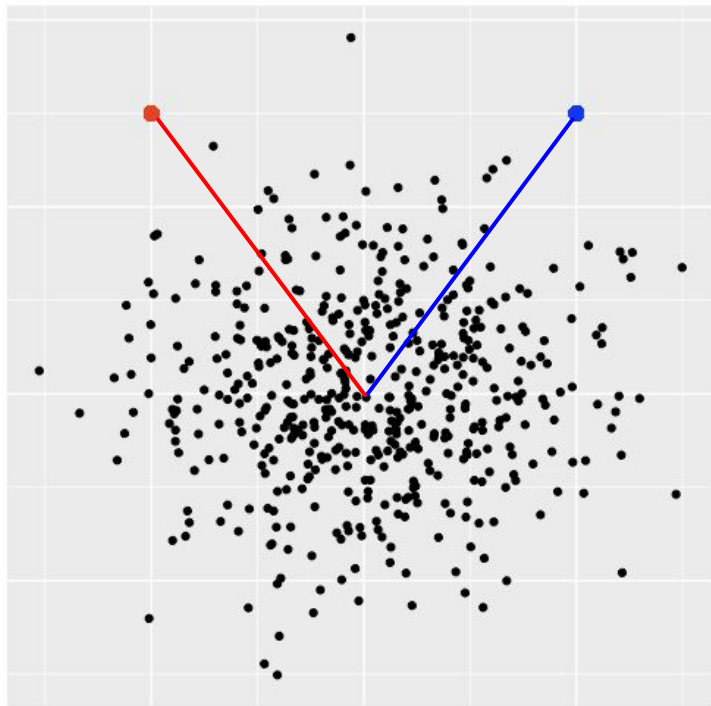


Unsupervised Method: Distance

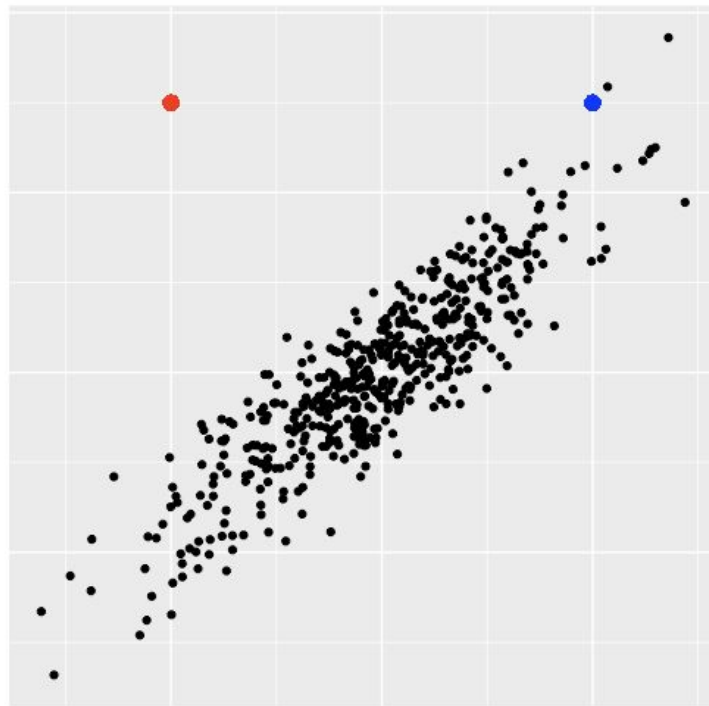
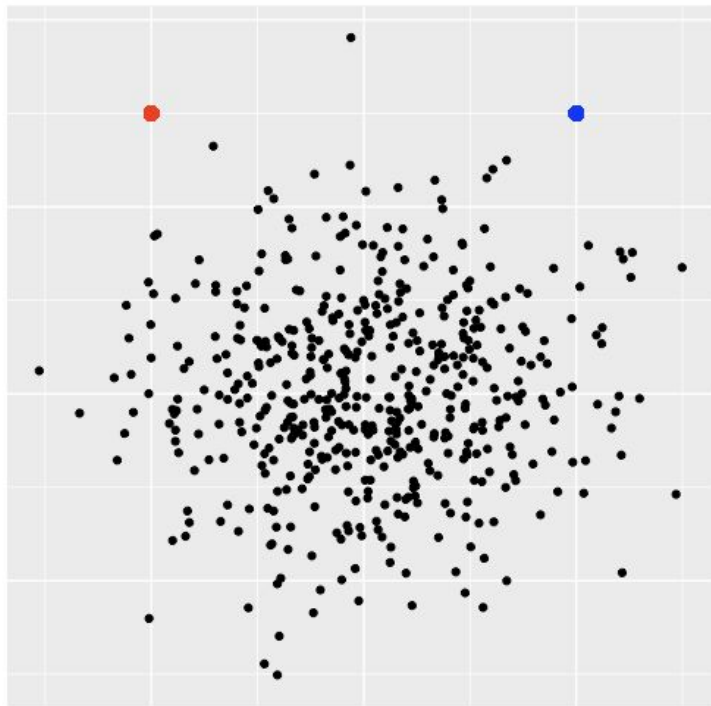
Euclidean Distance



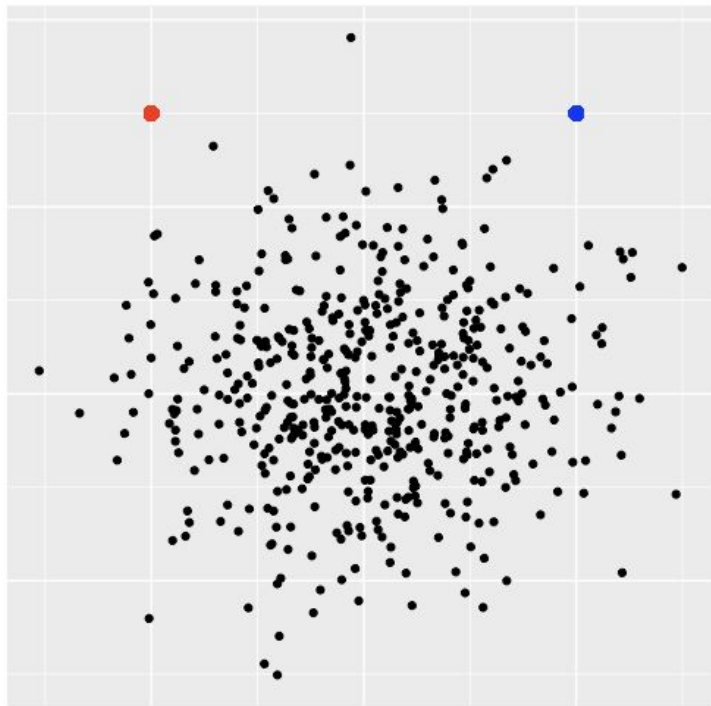
Euclidean Distance



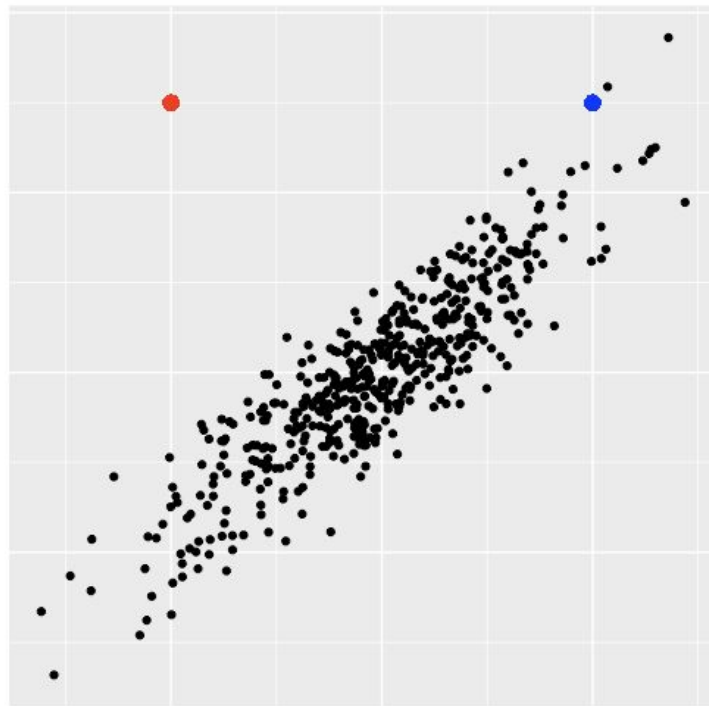
Euclidean Distance



Euclidean Distance



Mahalanobis Distance

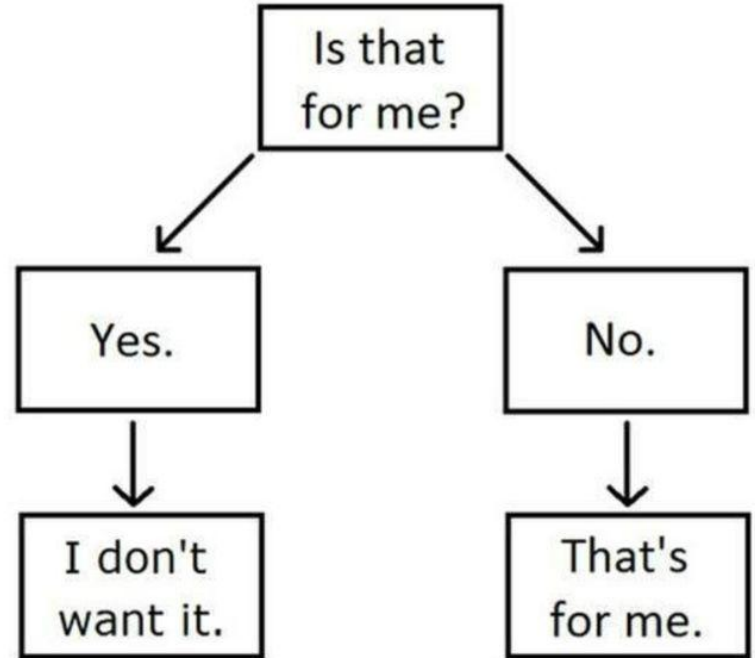


Supervised Method: Random Forest

Decision Tree

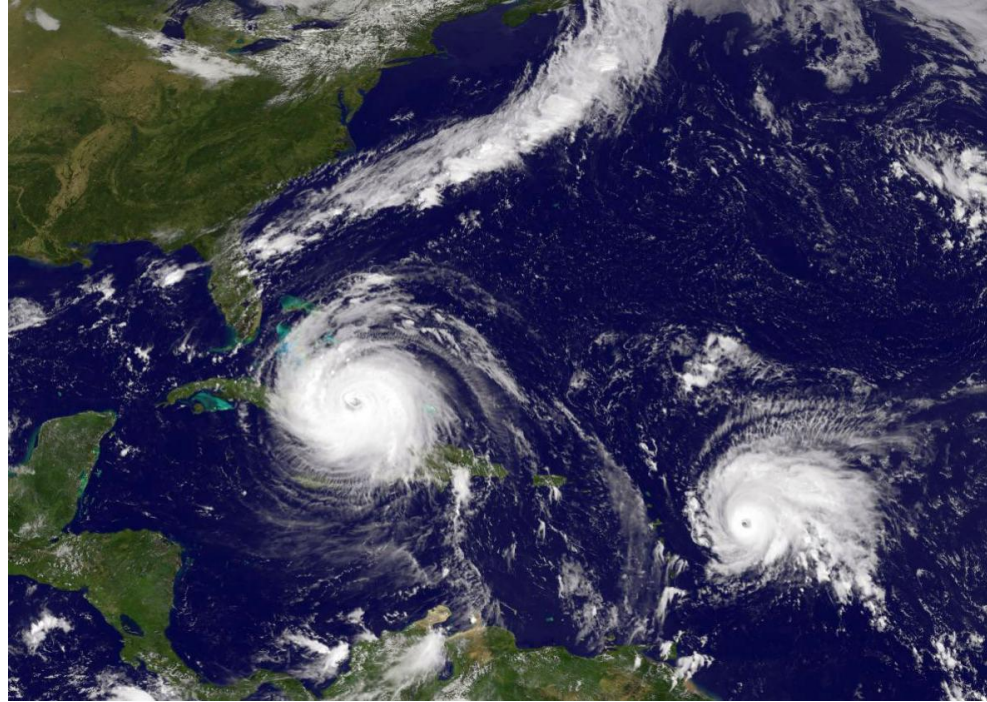


My Cat's Decision-Making Tree.

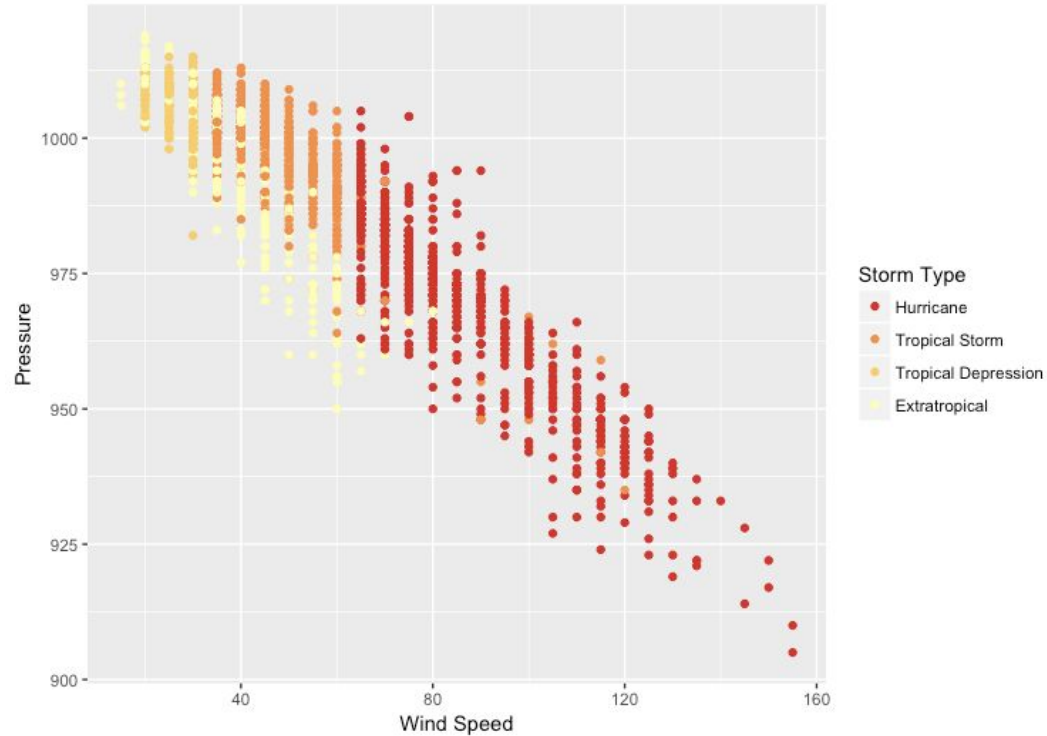


NASA Hurricane Data

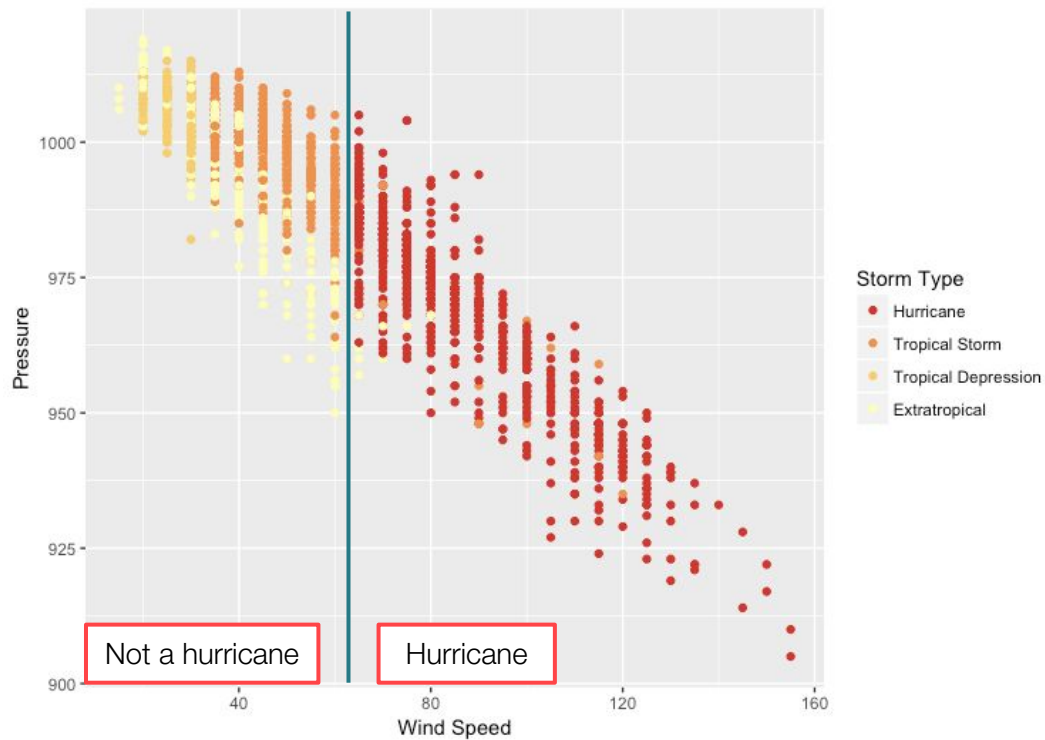
- Storm data from the National Hurricane Center's archive of Tropical Cyclone Reports (1995-2005).
- Hurricanes, tropical storms, tropical depressions, and extratropical storms were tracked through the Atlantic Ocean, Caribbean Sea and Gulf of Mexico.



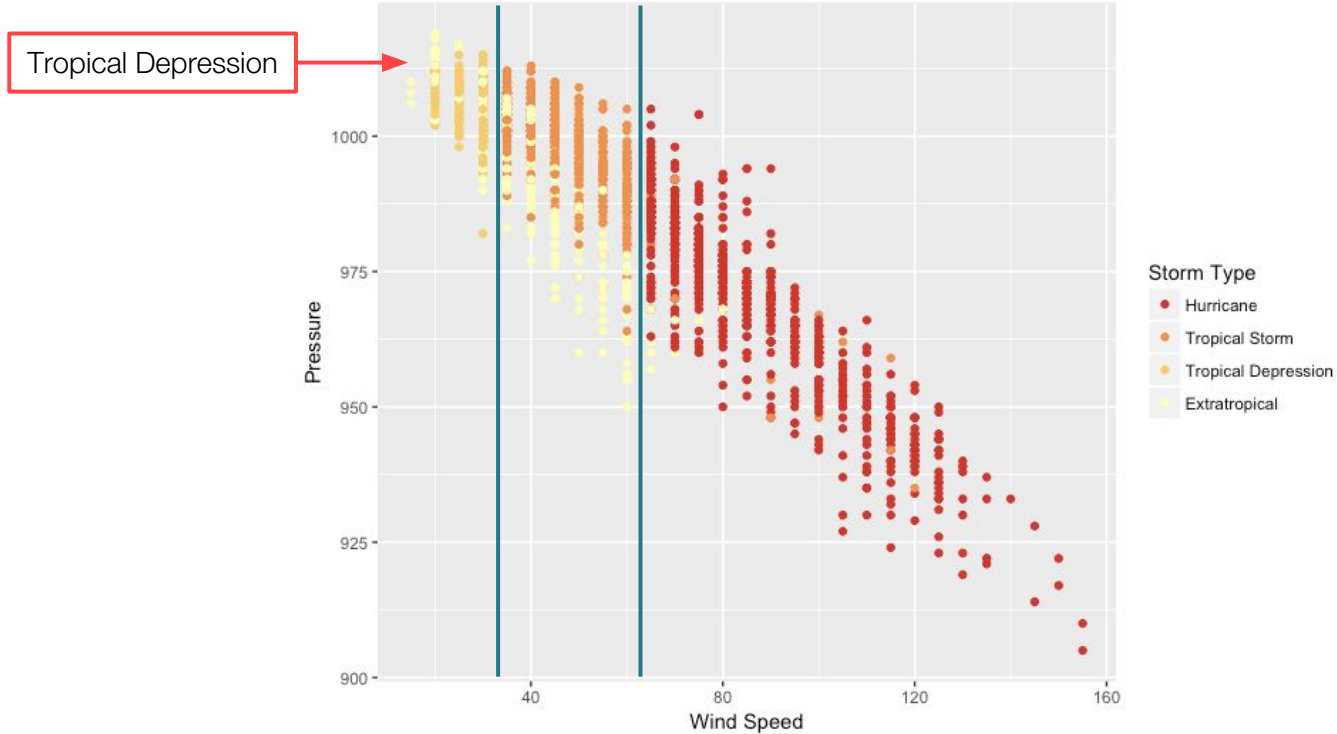
How might we split this data?



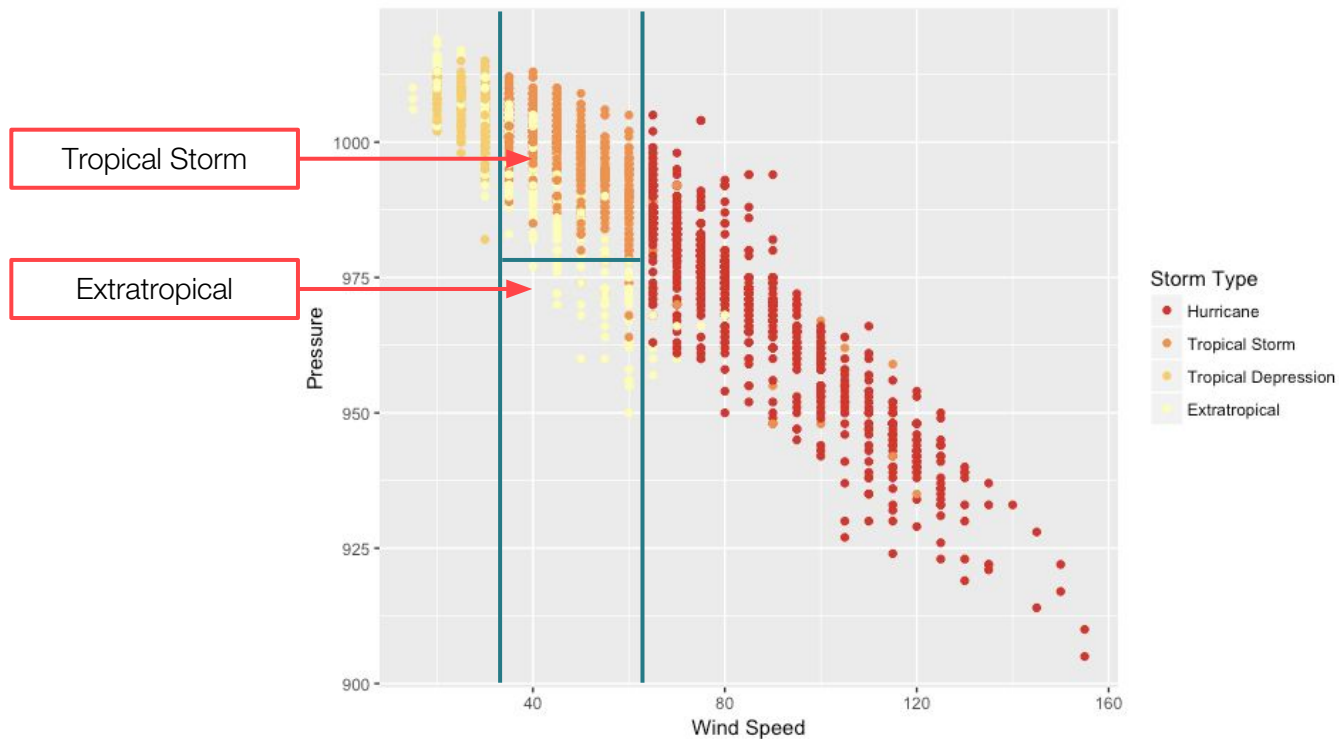
How might we split this data?



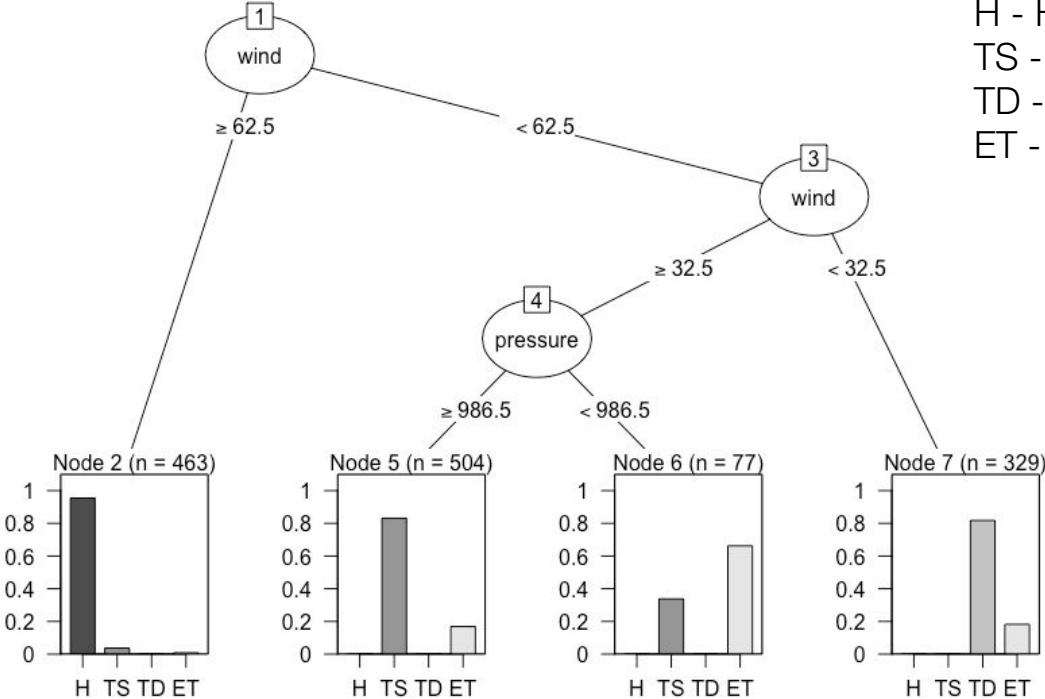
How might we split this data?



How might we split this data?

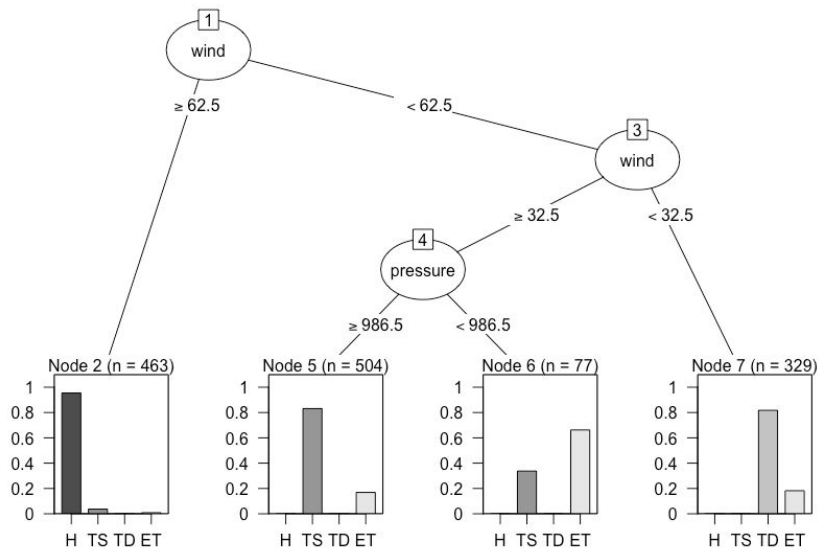


Decision Tree

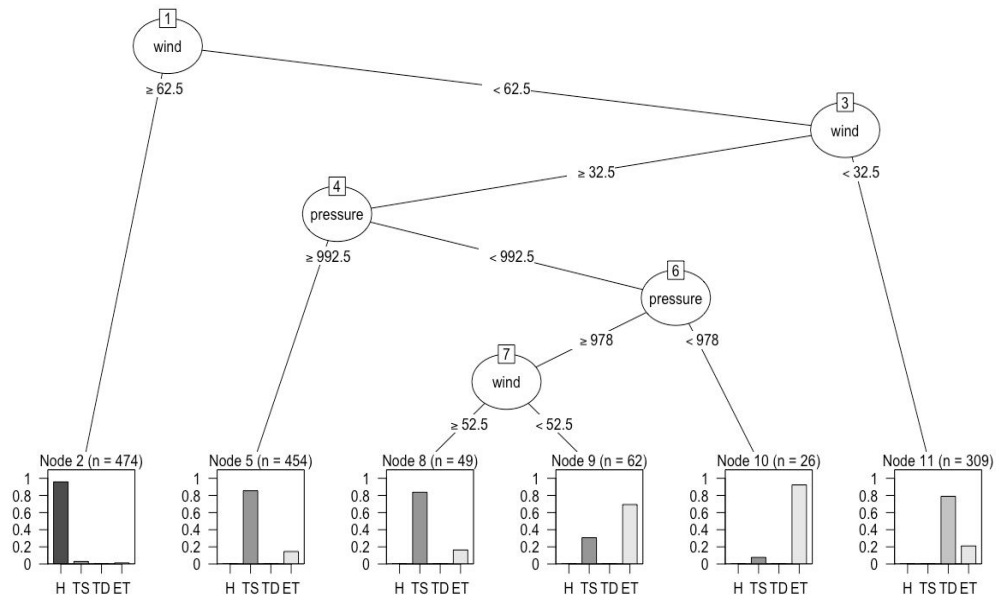


Problem: Decision trees are not very robust

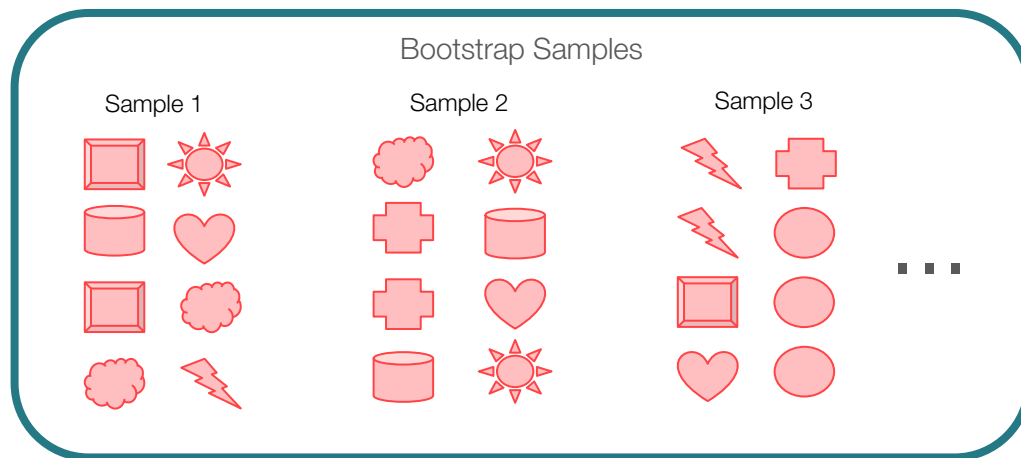
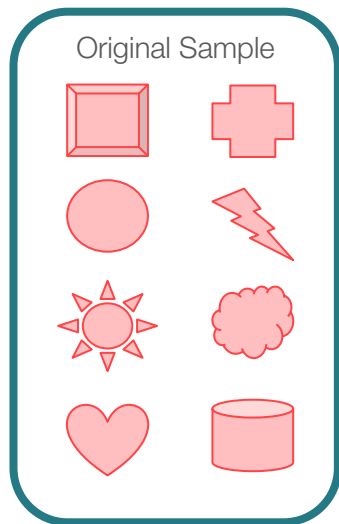
Sample 1



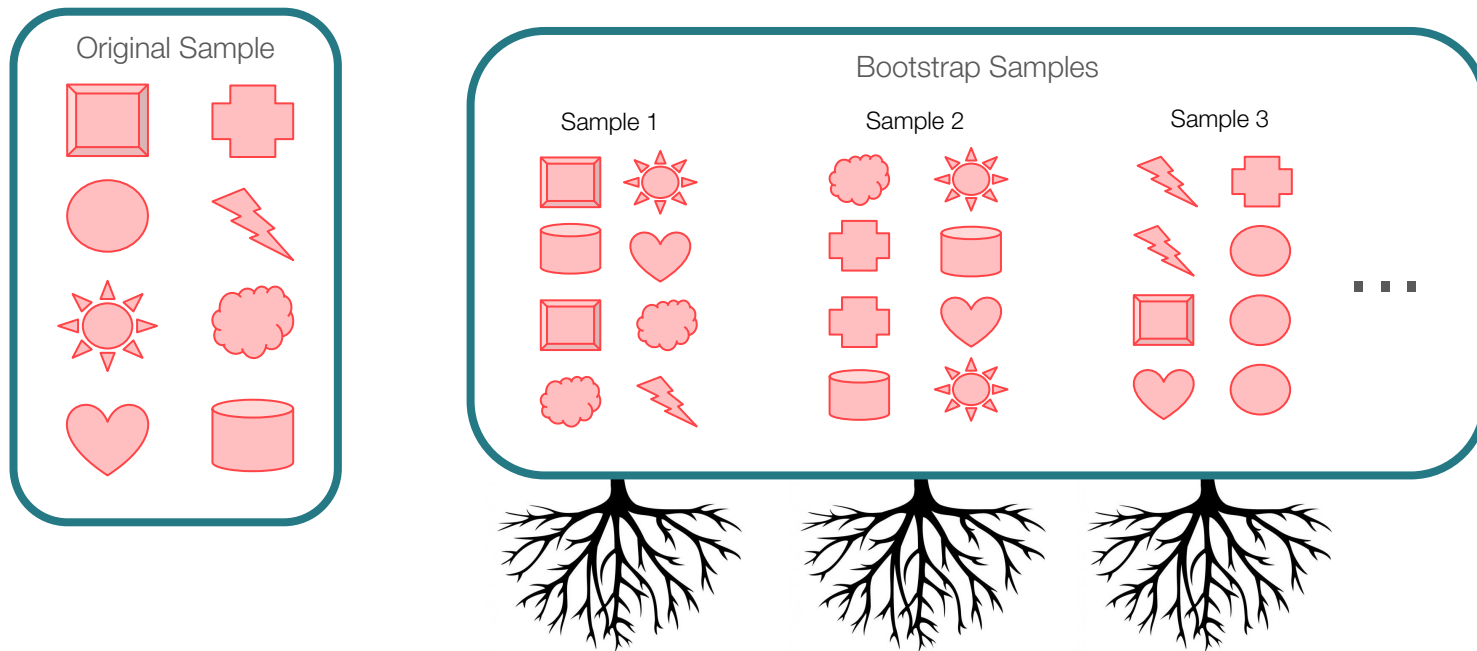
Sample 2



Bagging



Bagging

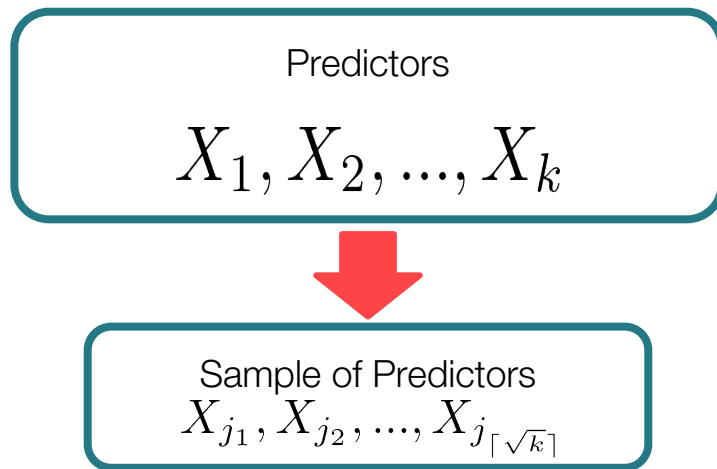


Growing a forest

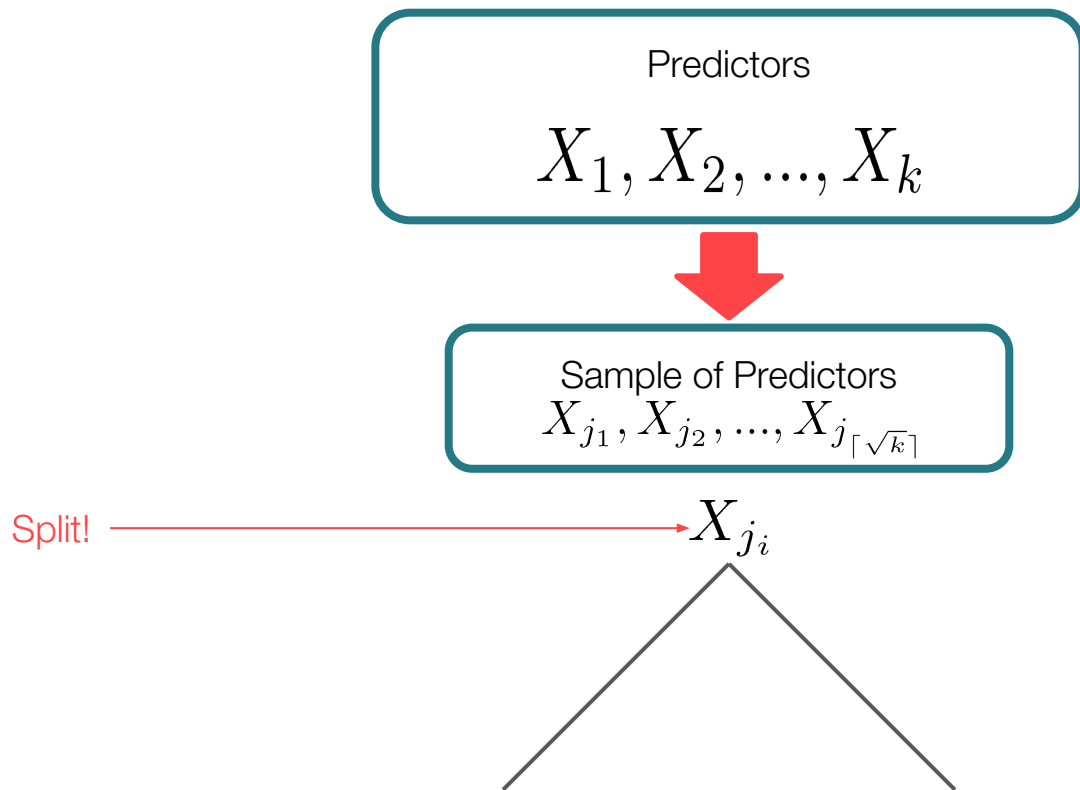
Predictors

$$X_1, X_2, \dots, X_k$$

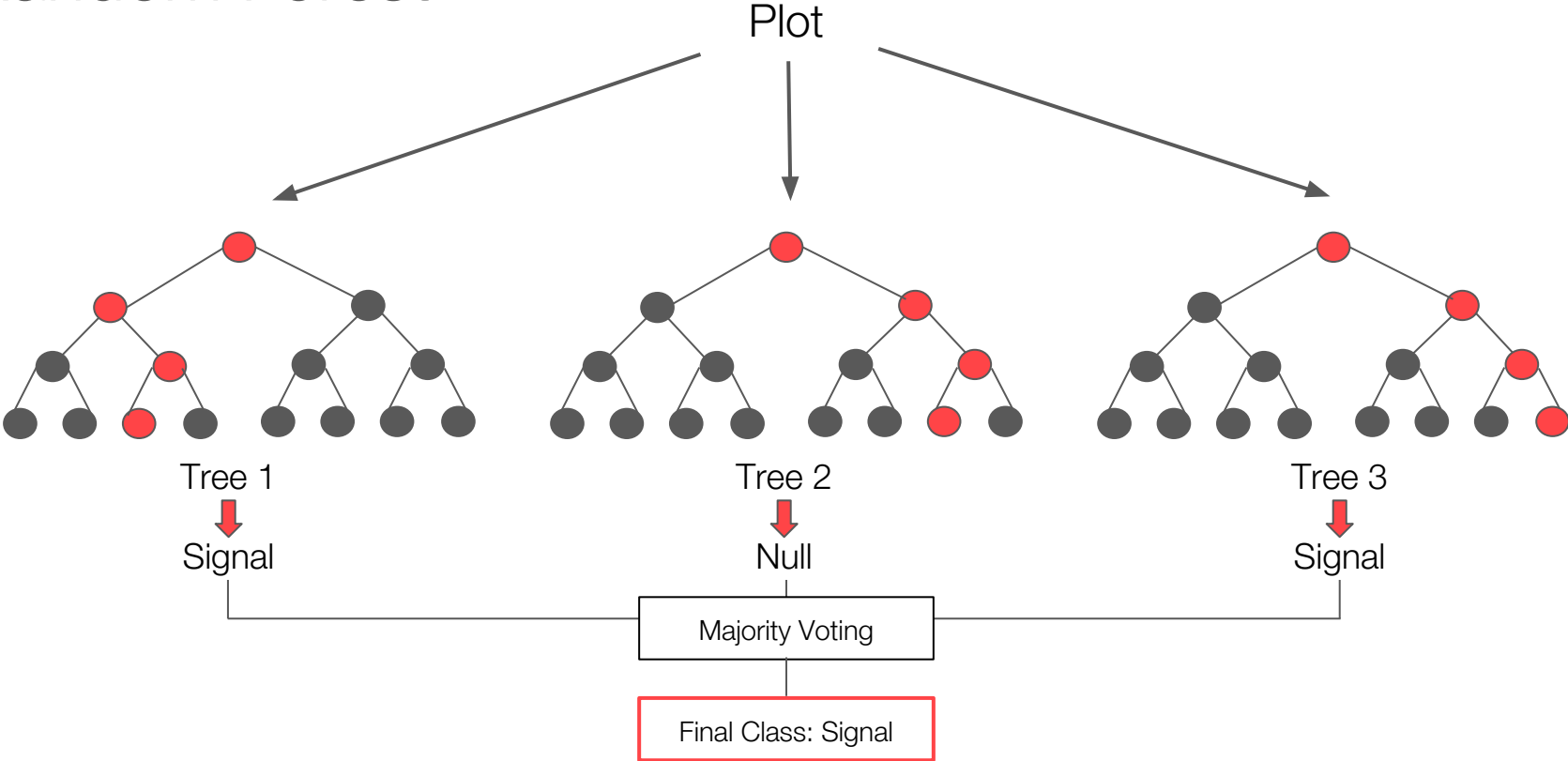
Growing a forest



Growing a forest



Random Forest



Back to hurricane data...

Accuracy of decision tree:

89%

Accuracy of random forest:

96%



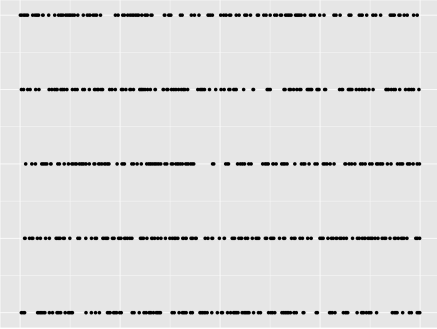
Training Data

Primary Family Data

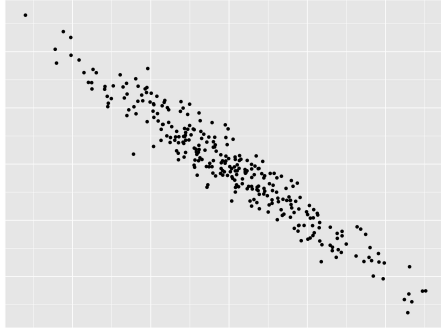
- Striated
- Linear
- Cluster
- Funnel
- Exponential
- Quadratic
- 14865 signal plots
- 14865 null plots

Primary Family Data

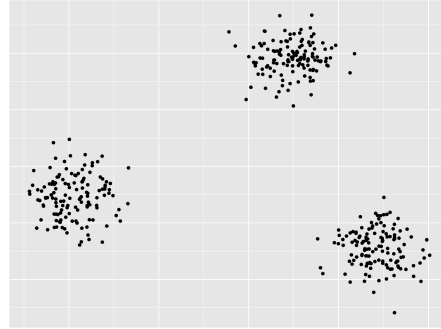
Striated



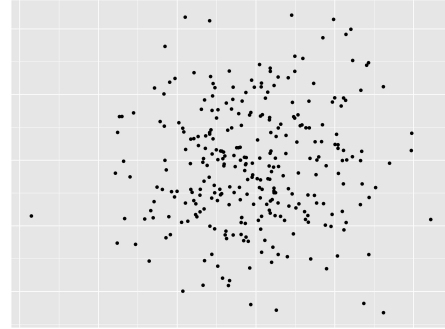
Linear



Cluster

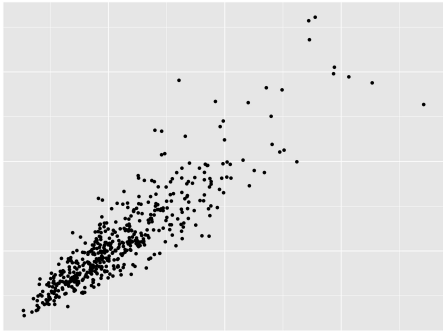


Null

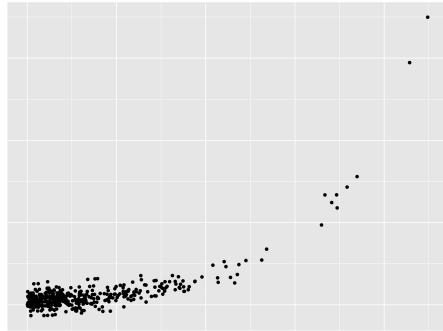


Primary Family Data

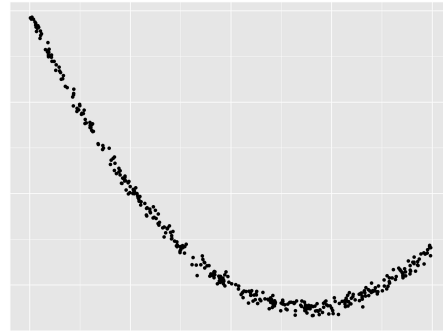
Funnel



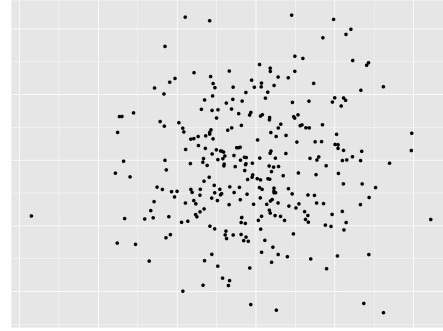
Exponential



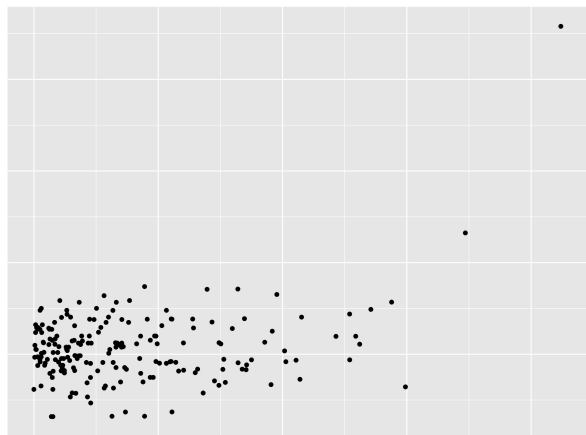
Quadratic



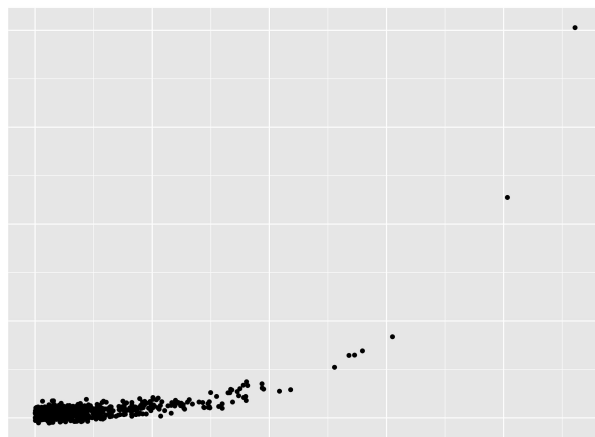
Null



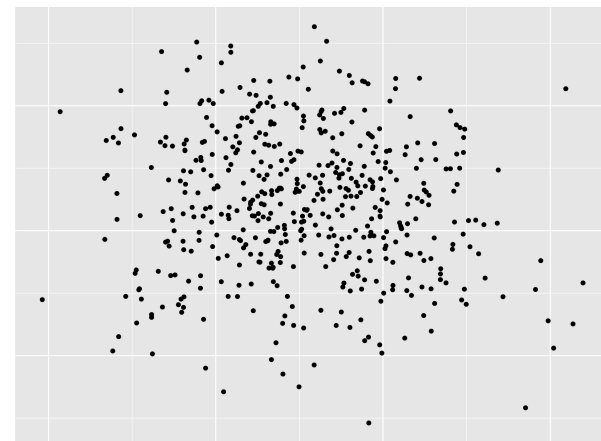
Training Data: Exponential



Signal

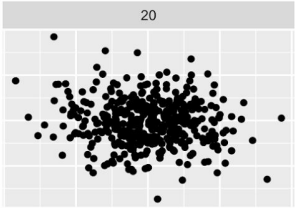
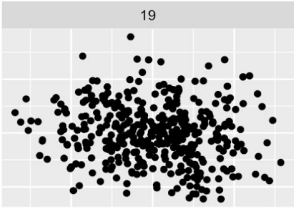
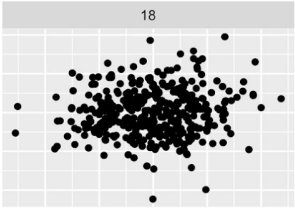
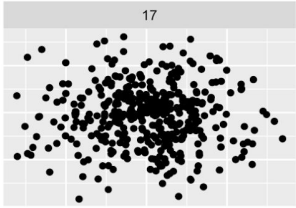
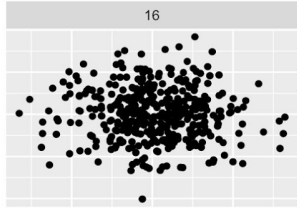
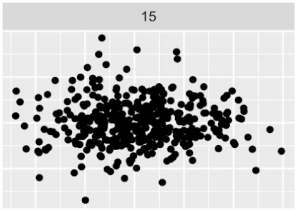
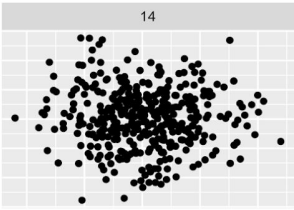
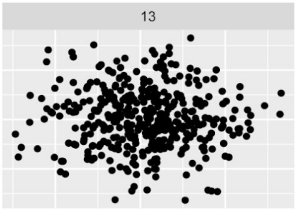
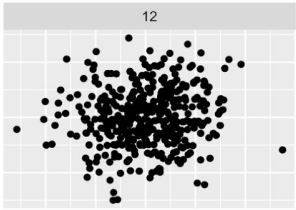
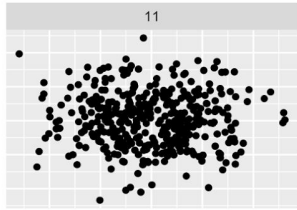
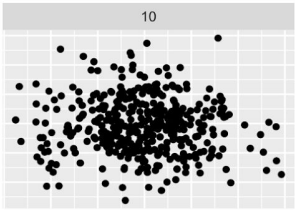
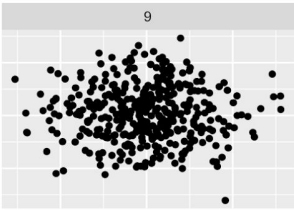
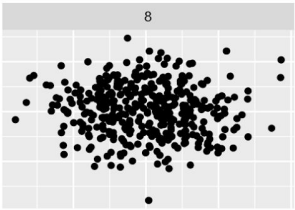
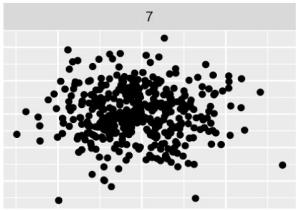
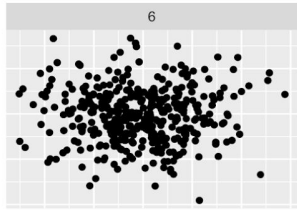
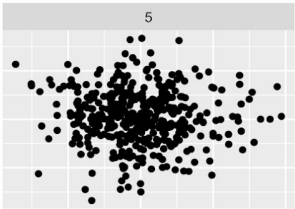
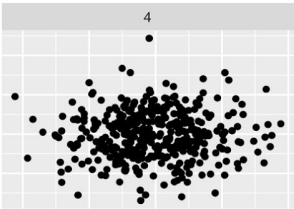
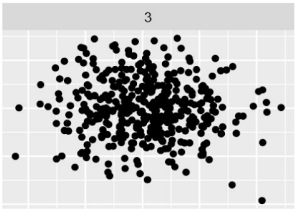
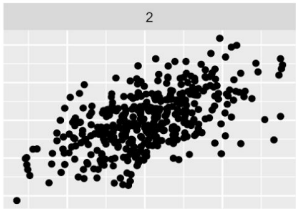
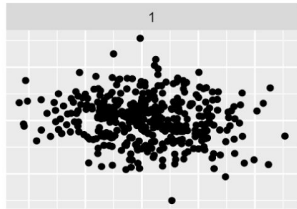


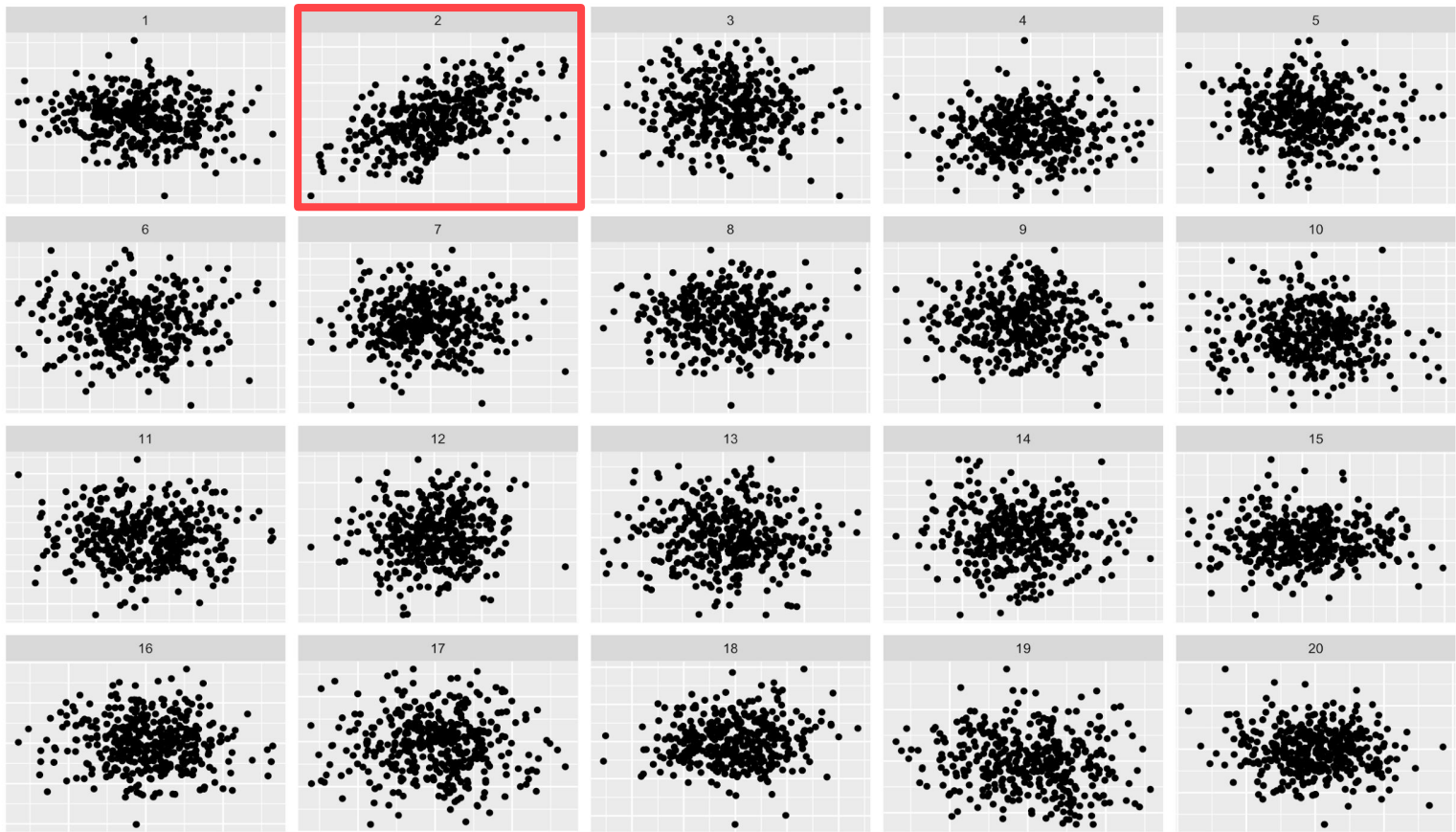
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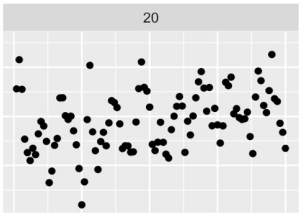
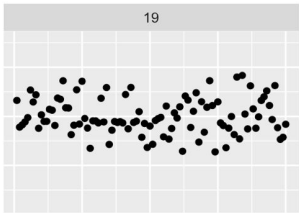
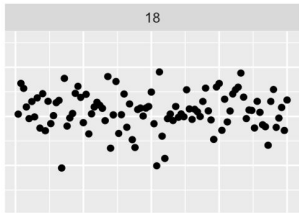
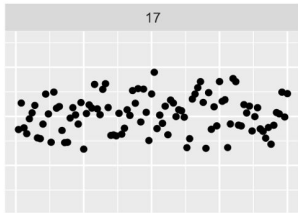
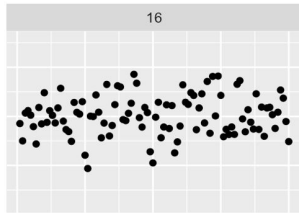
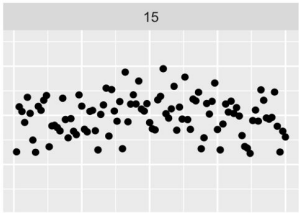
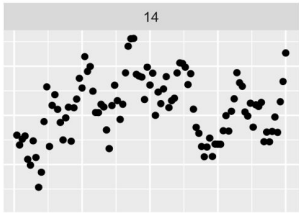
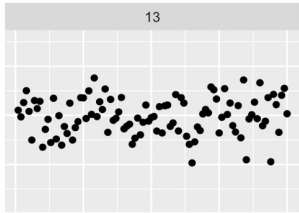
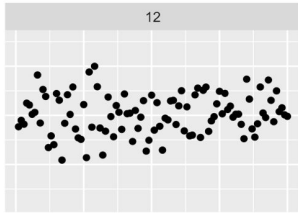
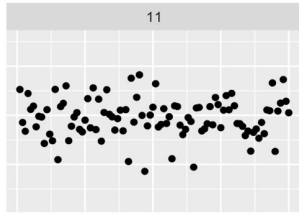
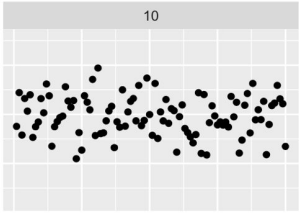
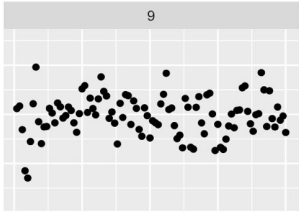
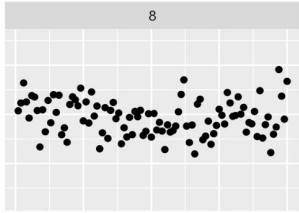
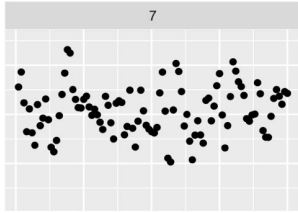
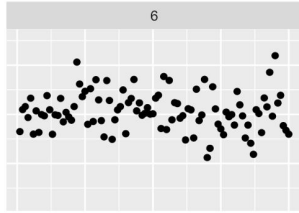
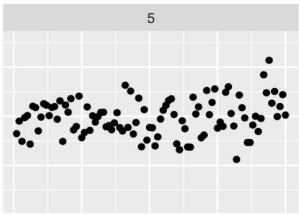
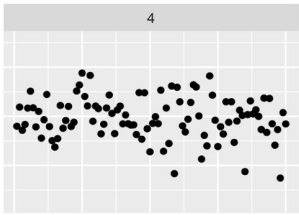
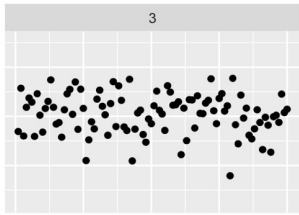
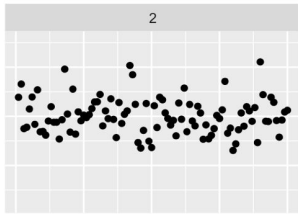
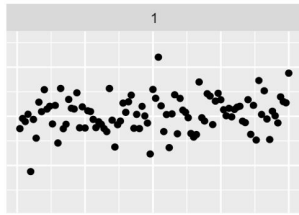


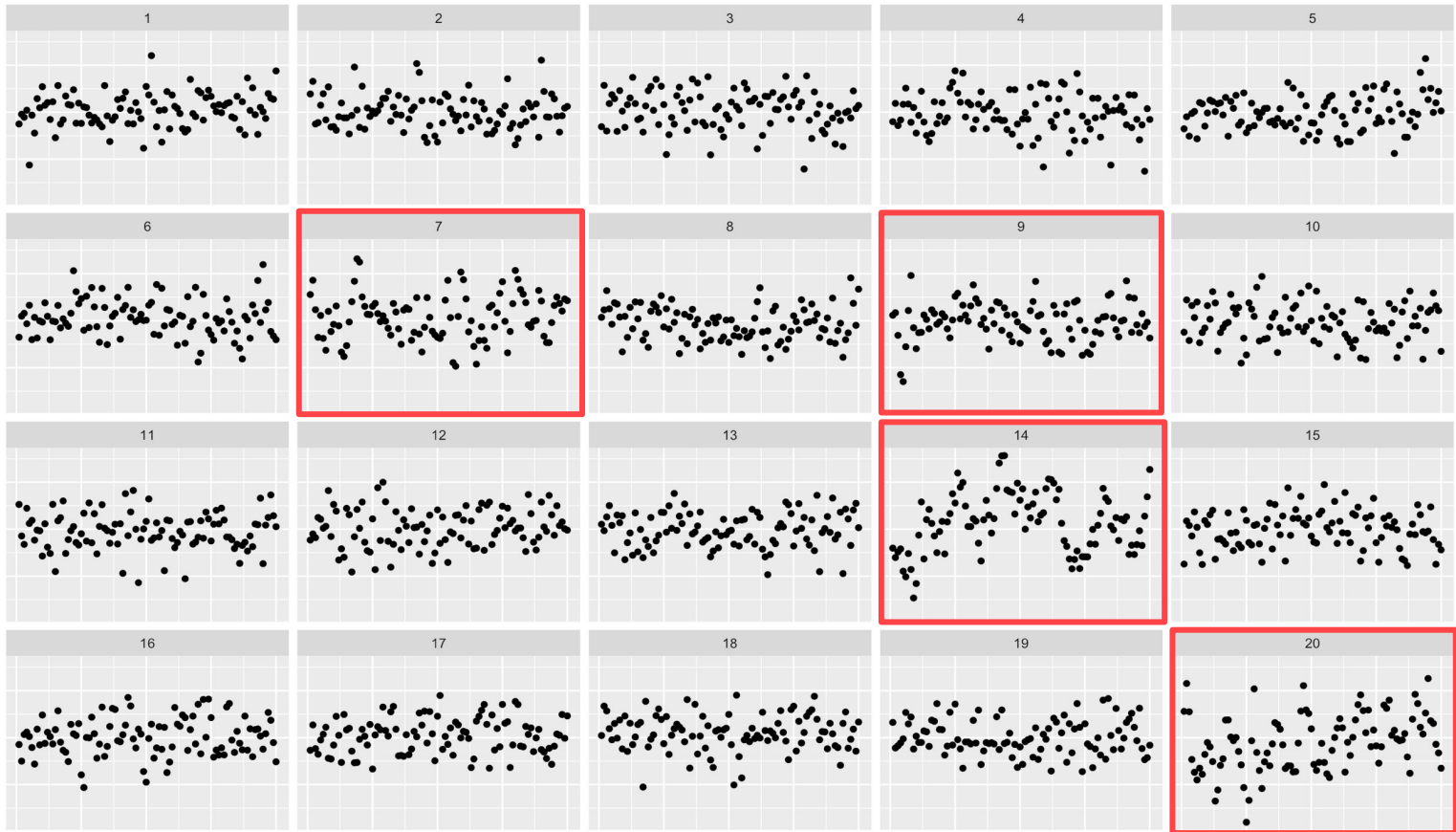
Null

Scatterplot Lineups: Testing the Model









Lineups: Model Accuracy

<i>One Signal Plot</i>	Mahalanobis Accuracy	Random Forest Accuracy
Linear Trend	.857	.992
Primary Family	.952	.972
<i>Unknown Signal Plots</i>		
Linear Trend	.628 (.372)	.932 (.053)
Primary Family	.722 (.278)	.979 (.030)
Lineups Per Dataset	1000	

Note: Rate of false positives is given in parentheses

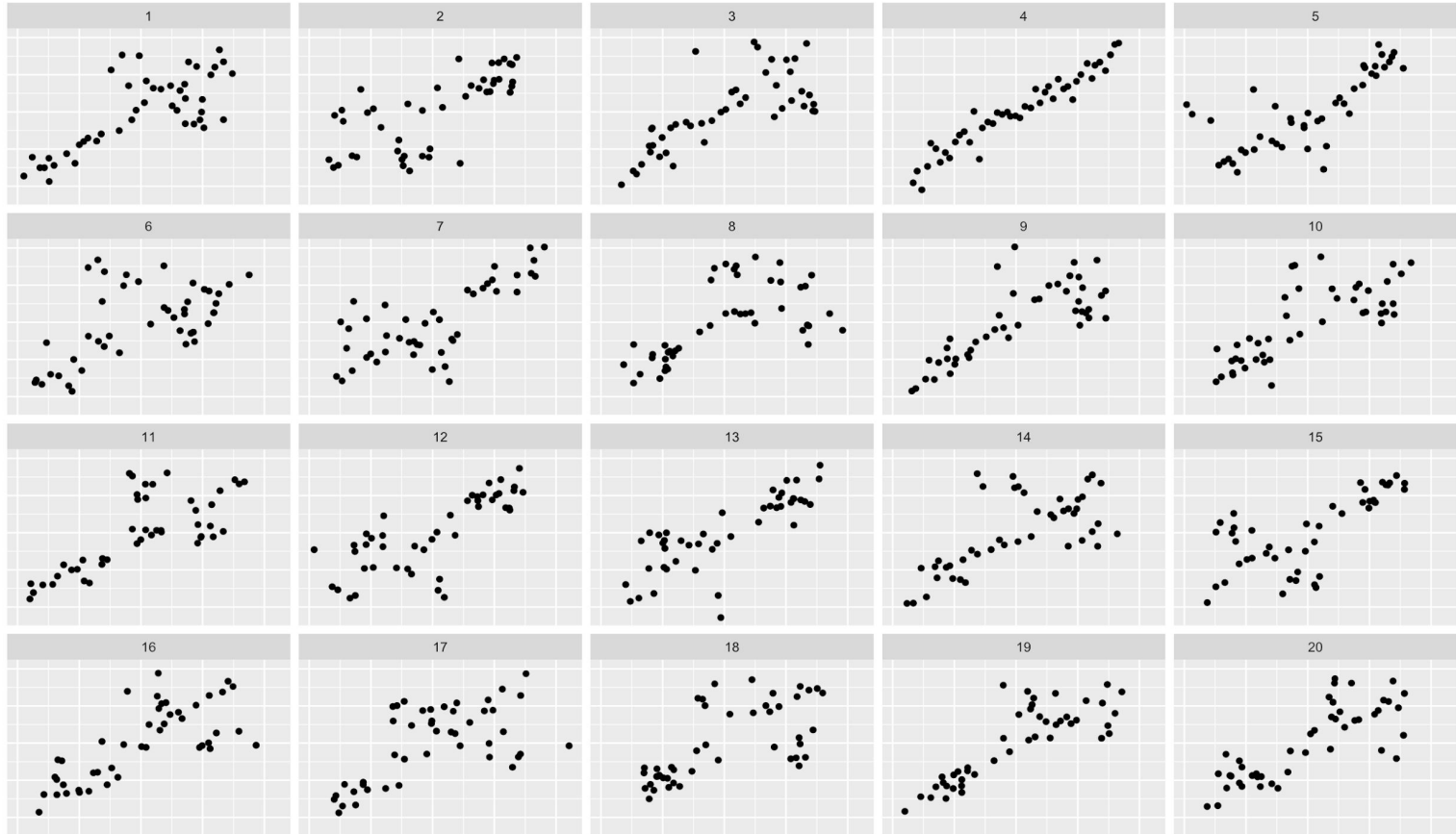
ISU Data

Lineup perception study from Iowa State

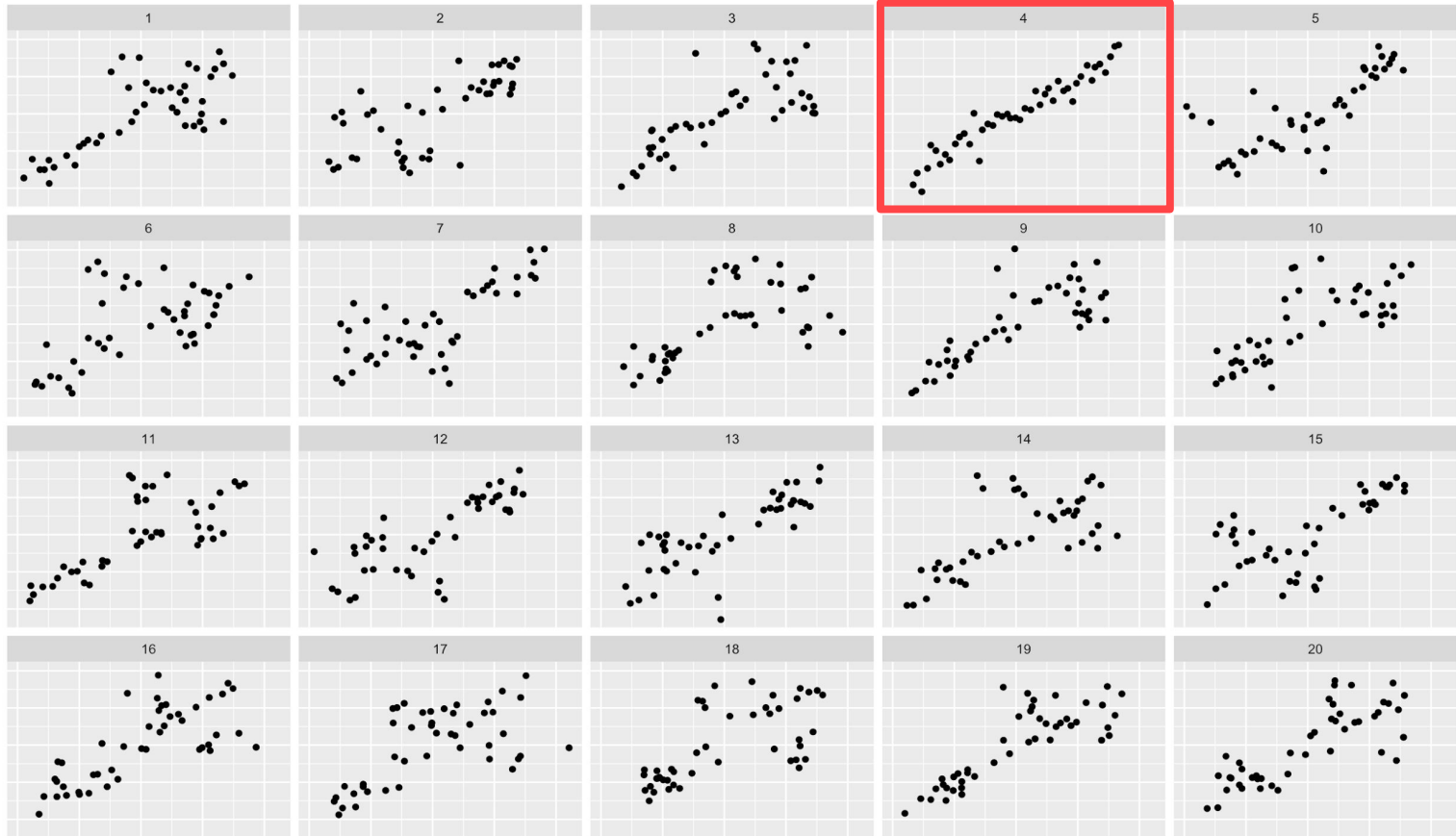
Hybrid linear + cluster plots

- 20 One-Signal Lineups
- 27 Multiple-Signal Lineups

ISU Data



ISU Data



ISU Data: Model Accuracy

	Single Signal Plot	Unknown Signal Plots
Mahalanobis Accuracy	.600	.537 (.433)
Random Forest Accuracy	1.000	.926 (.077)
Total Number of Lineups	20	27

Note: Rate of false positives is given in parentheses

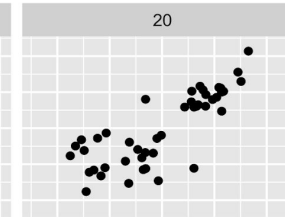
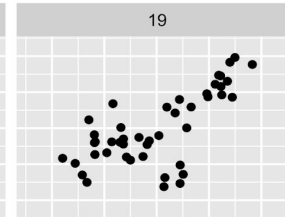
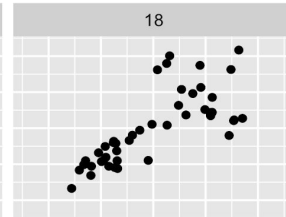
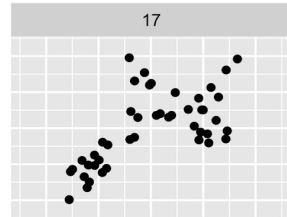
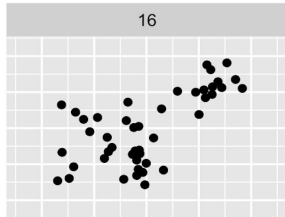
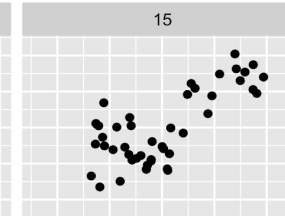
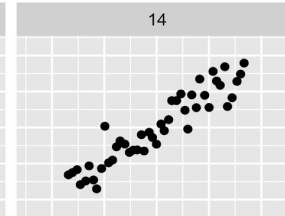
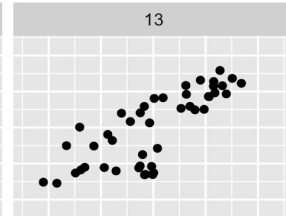
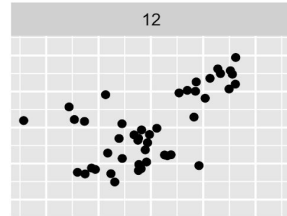
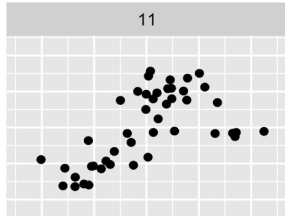
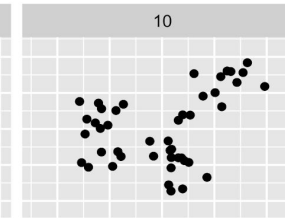
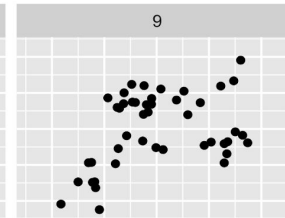
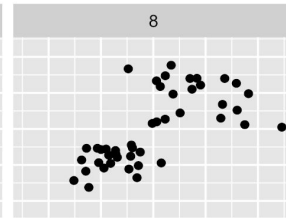
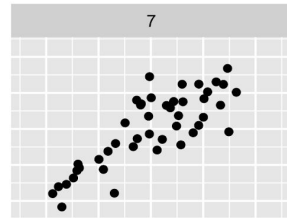
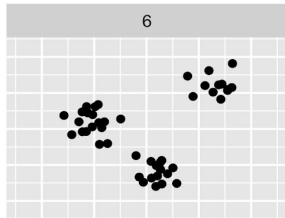
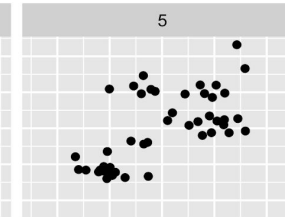
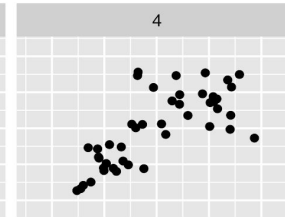
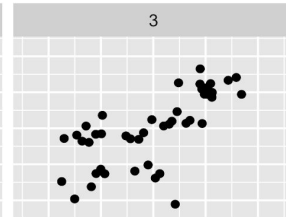
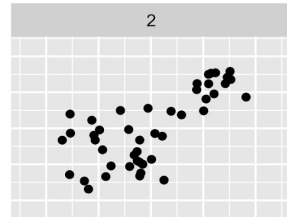
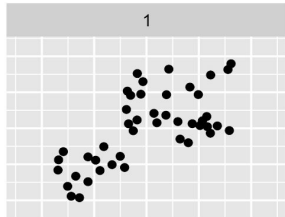
Carleton Study

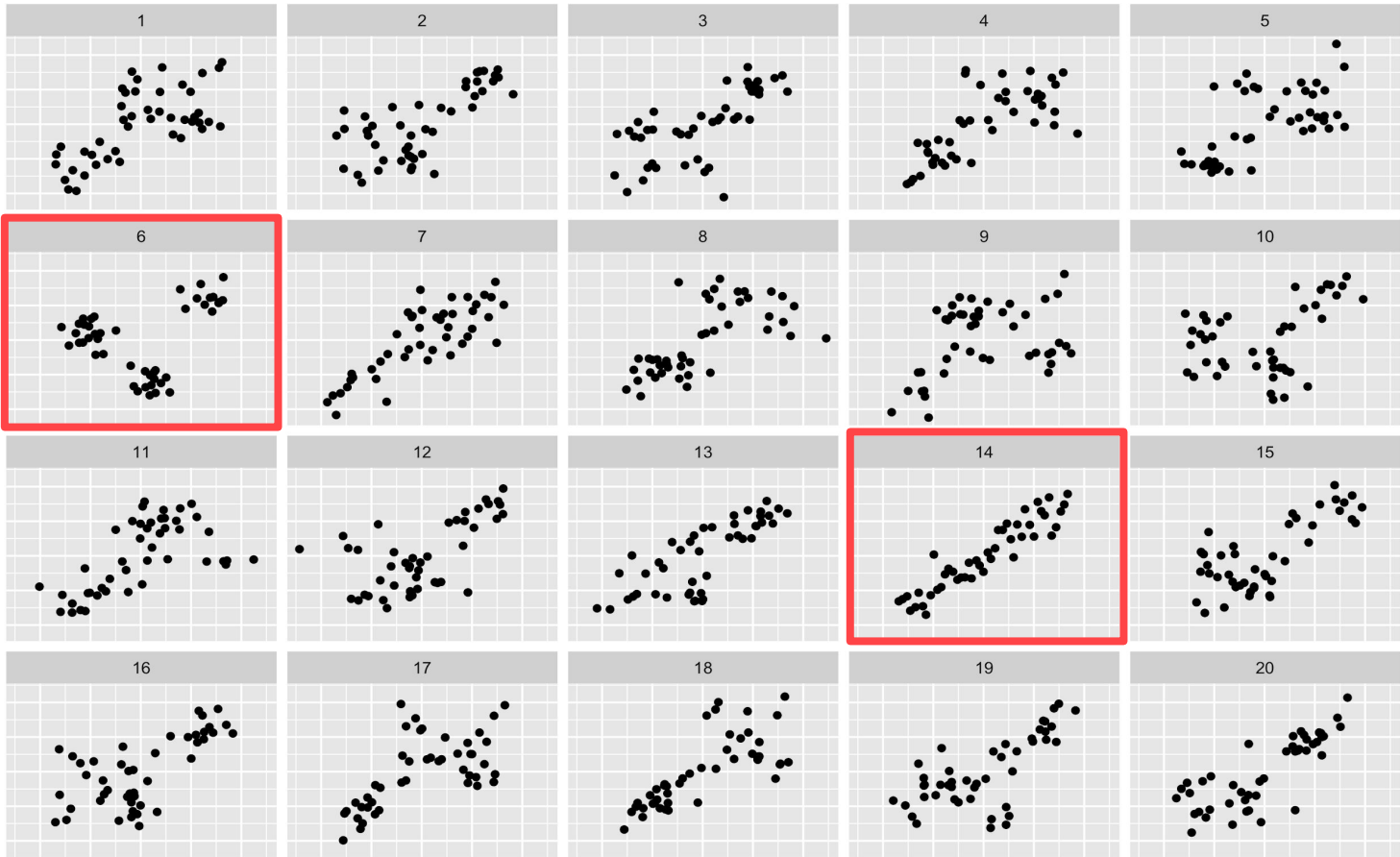
Comparison to Human Perception

Participants: 50 Carleton students

Procedure: 9 lineups shown to each person

- 6 lineups had 1 target plot
- 3 lineups had unknown number of target plots





Results

	Single Signal Plot	Unknown Signal Plots
Participant Accuracy	.805	.720 (.105)
Mahalanobis Accuracy	.750	.628 (.291)
Random Forest Accuracy	.917	.917 (.083)

Note: Rate of false positives is given in parentheses

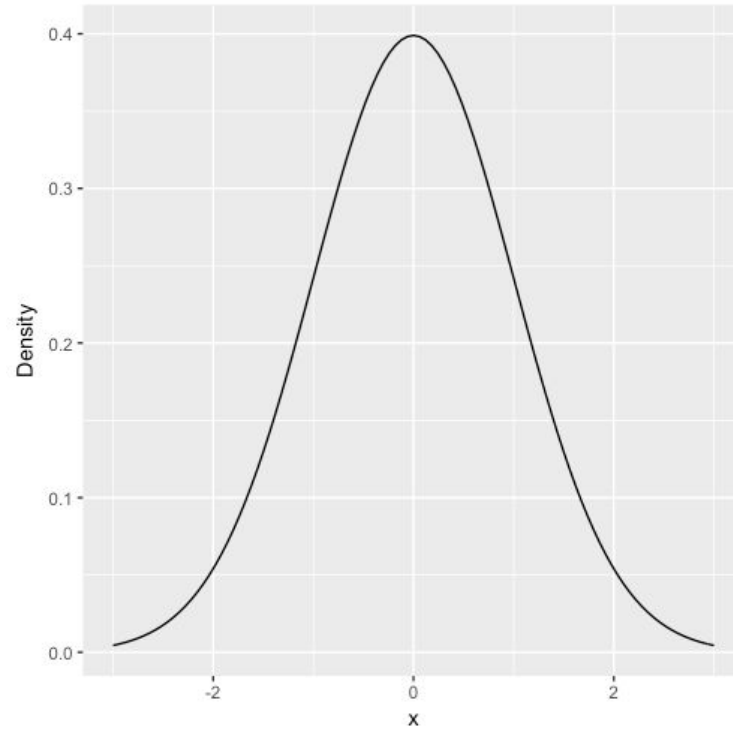
Lineups: Model Accuracy

<i>One Signal Plot</i>	Mahalanobis Accuracy	Random Forest Accuracy
Time Series	.248	.425
QQ Plots	.210	.500
<i>Unknown Signal Plots</i>		
Time Series	.579 (.421)	.566 (.464)
QQ Plots	.589 (.411)	.761 (.248)
Lineups Per Dataset	1000	

Note: Rate of false positives is given in parentheses

Can scagnostics help with
other types of plots?

Assessing normality



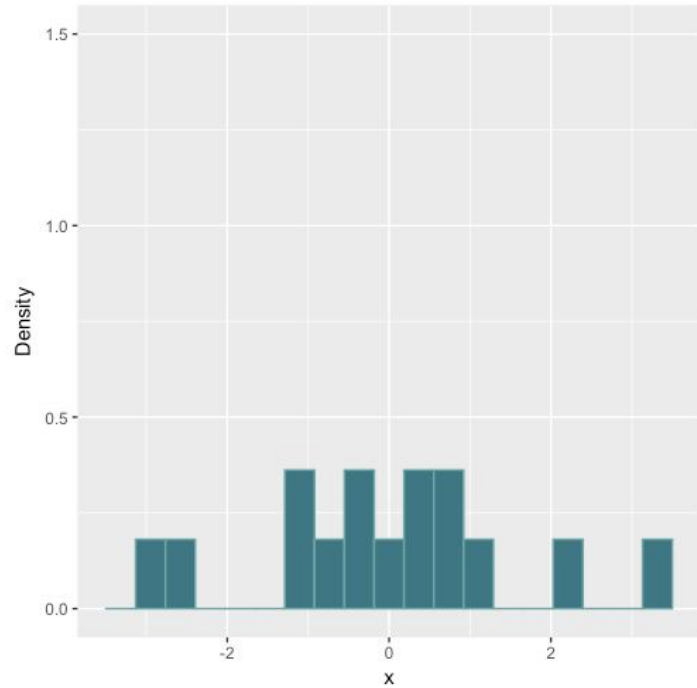
Assessing normality

Some data



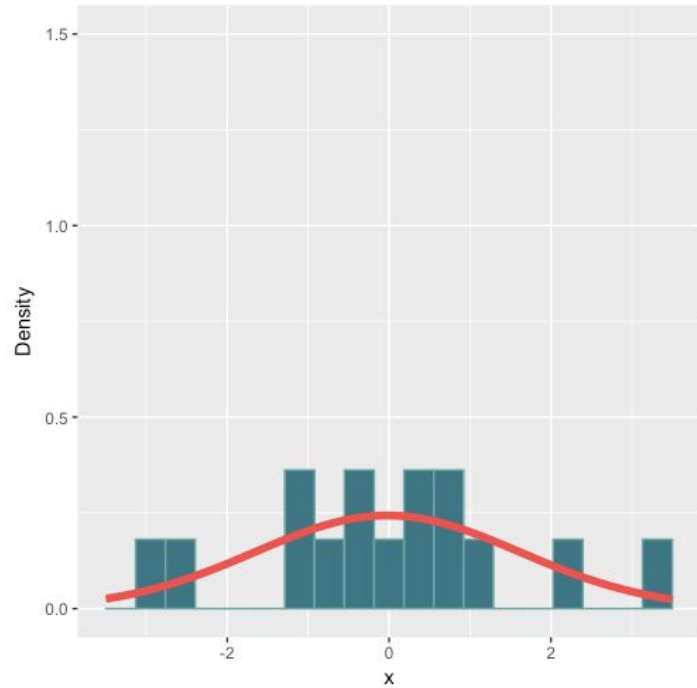
Assessing normality

Histogram



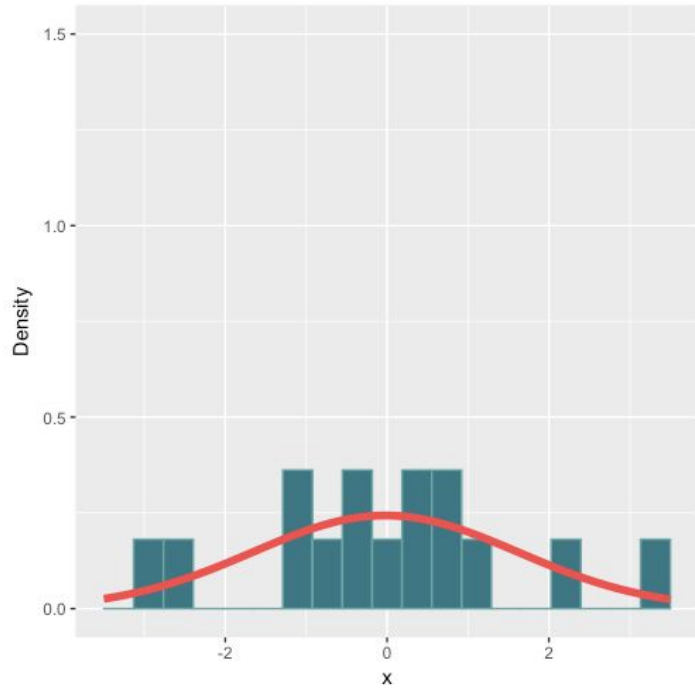
Assessing normality

Histogram

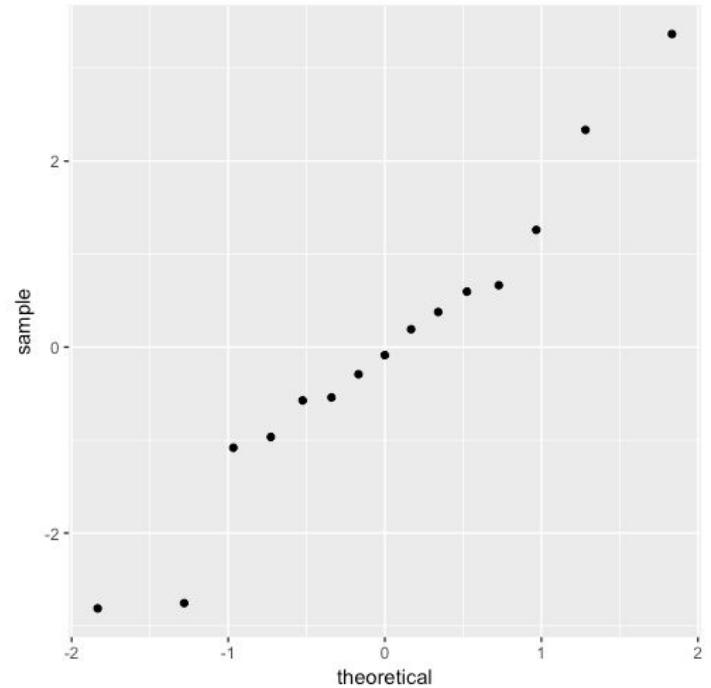


Assessing normality

Histogram

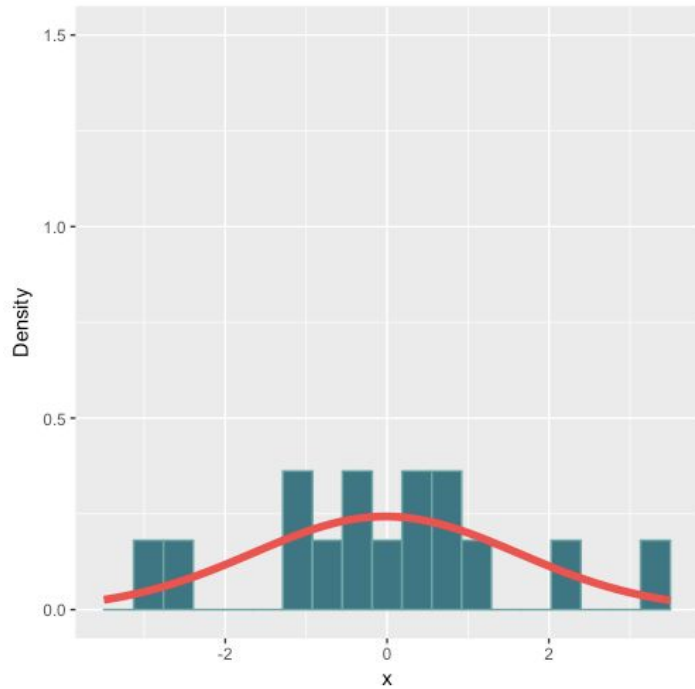


QQ Plot

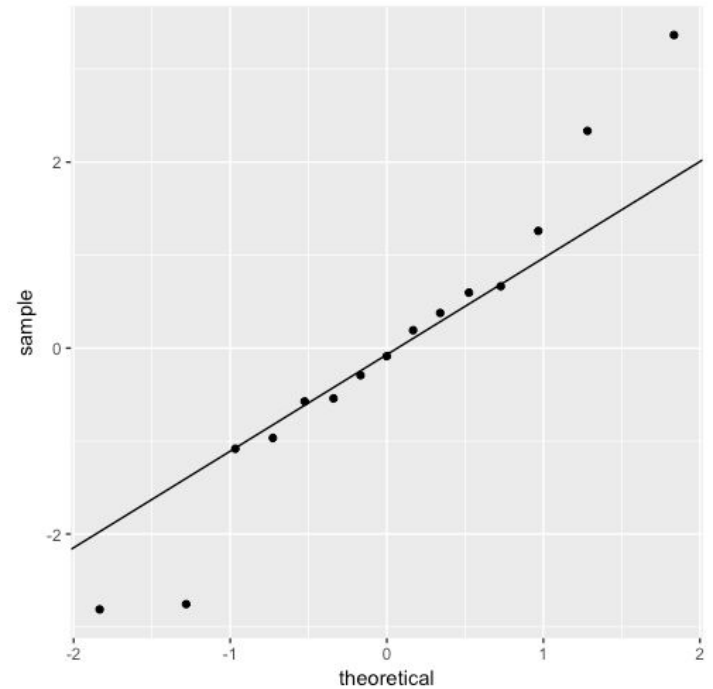


Assessing normality

Histogram

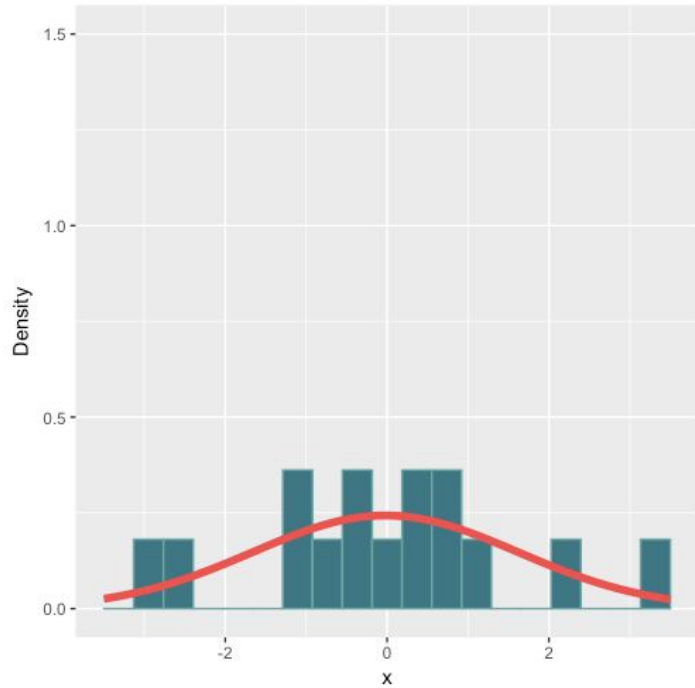


QQ Plot

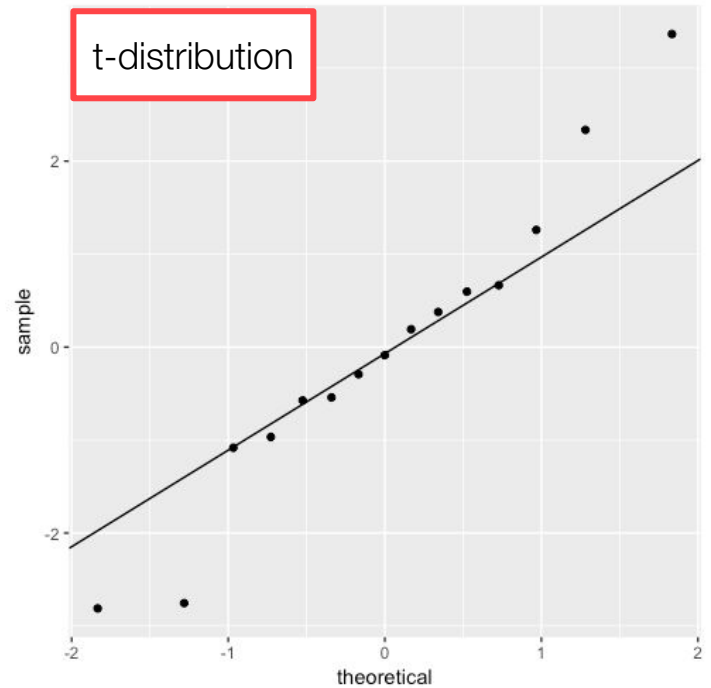


Assessing normality

Histogram

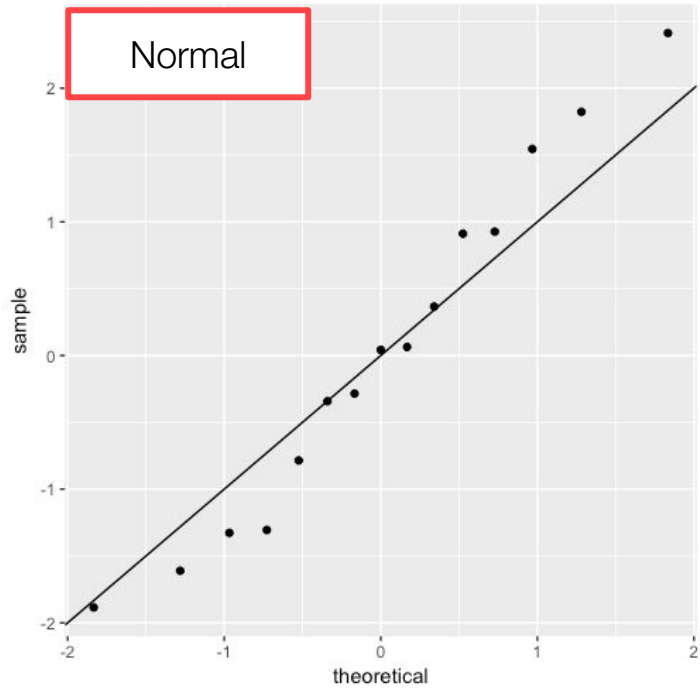


QQ Plot

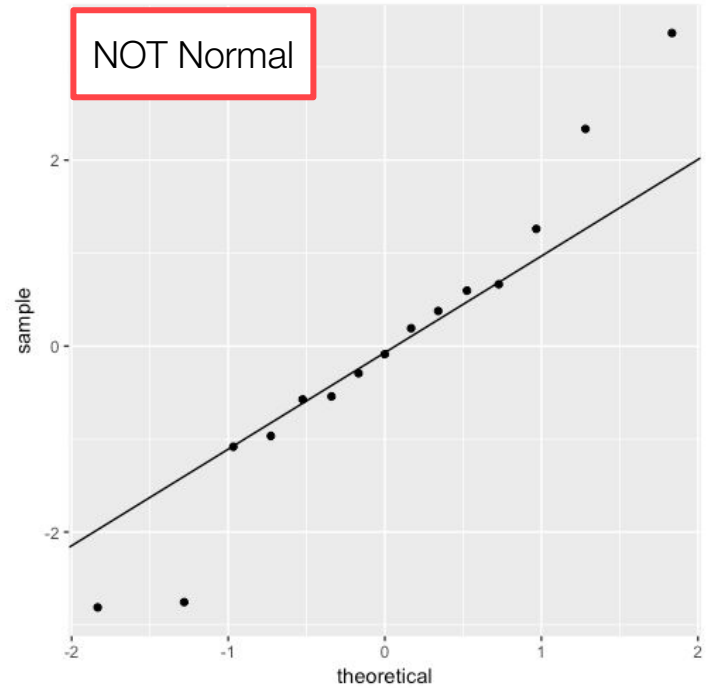


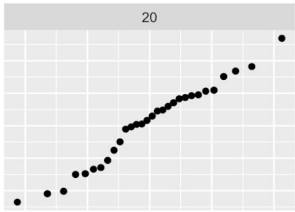
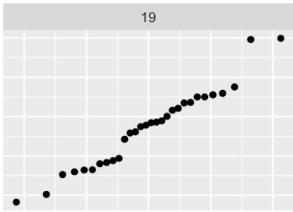
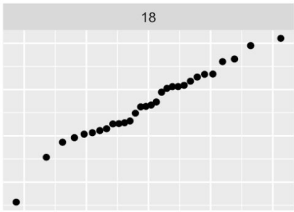
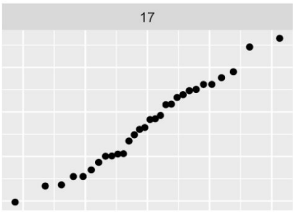
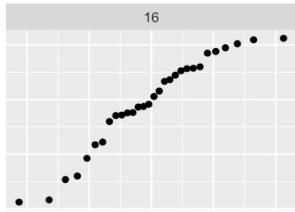
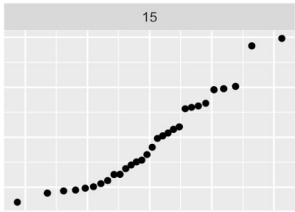
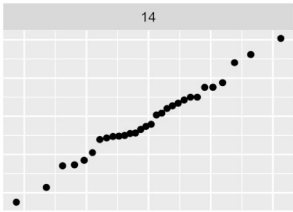
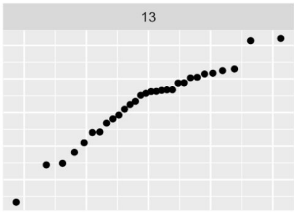
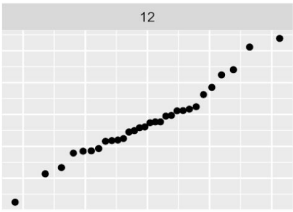
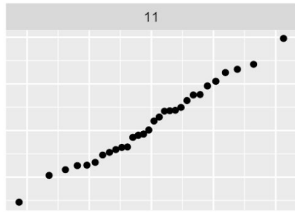
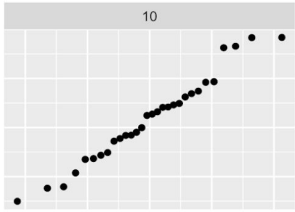
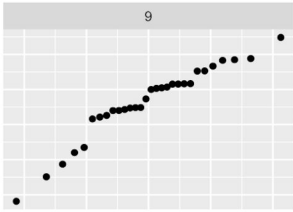
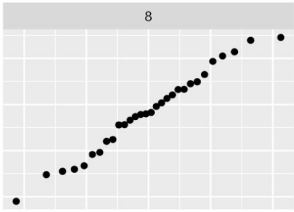
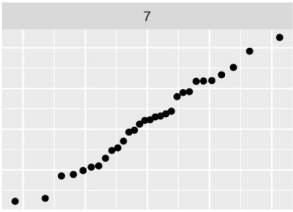
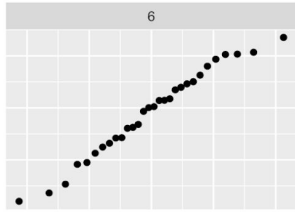
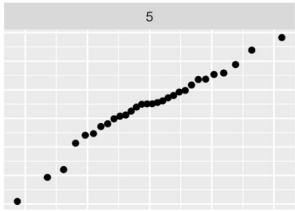
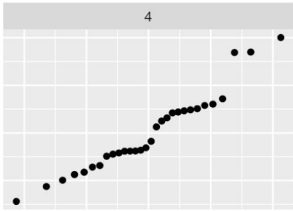
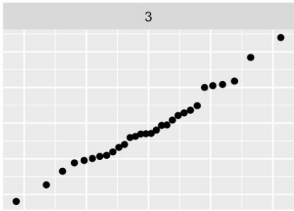
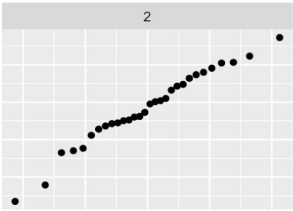
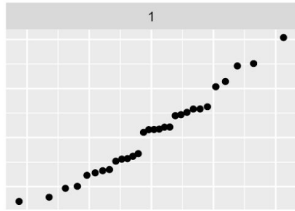
Assessing normality

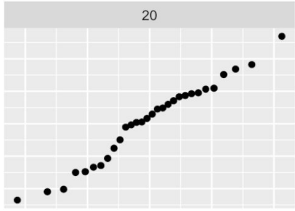
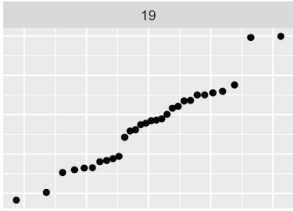
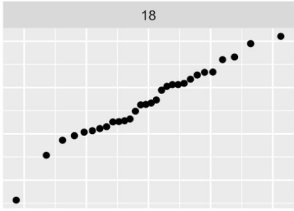
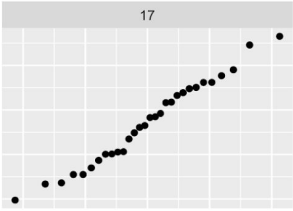
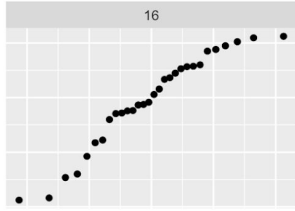
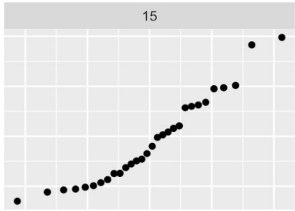
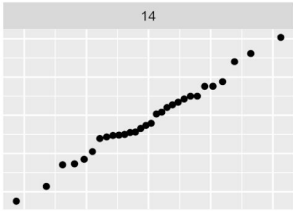
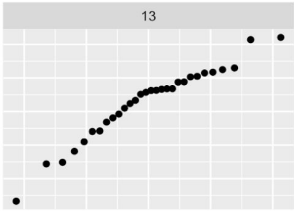
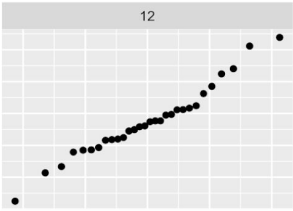
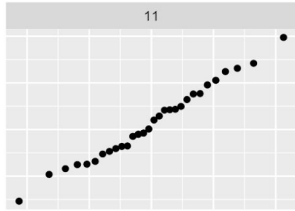
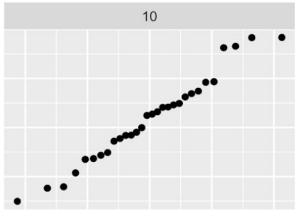
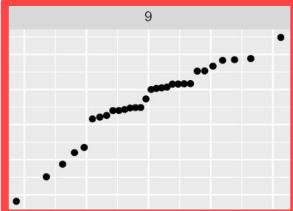
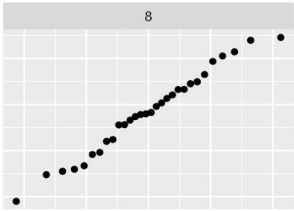
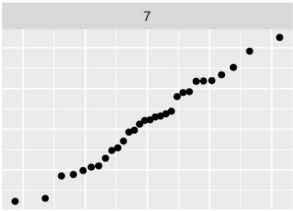
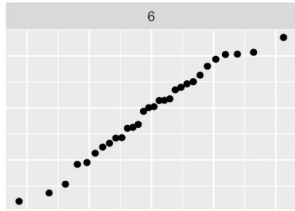
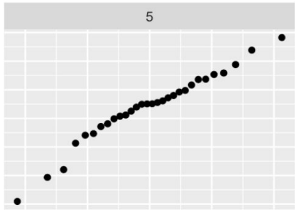
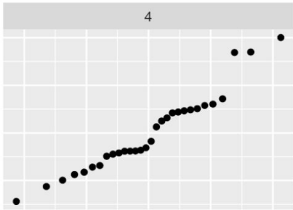
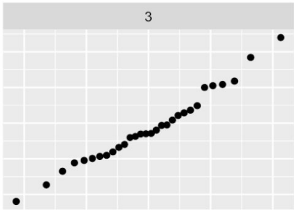
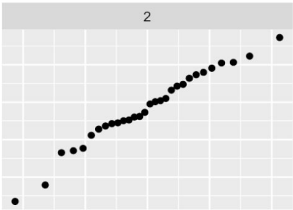
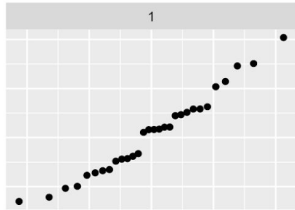
QQ Plot



QQ Plot







Can scagnostics predict non-normality?



Can scagnostics predict non-normality?

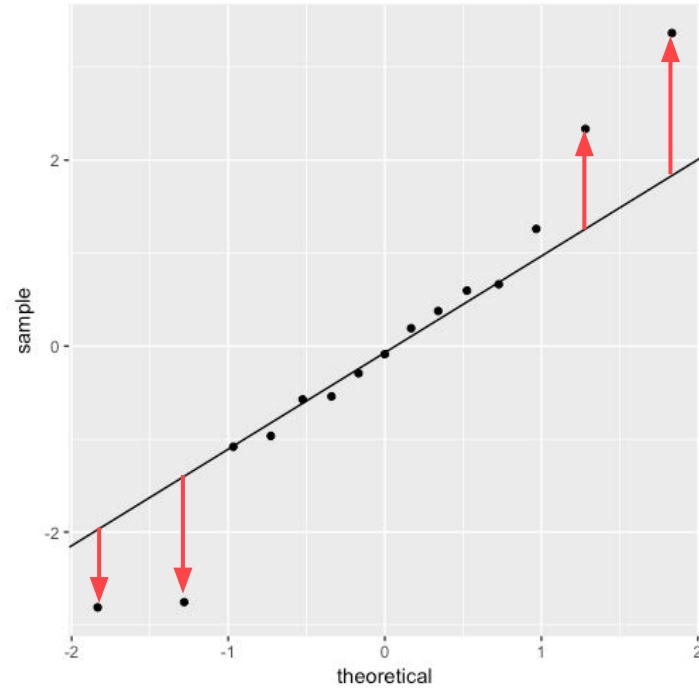
Shape

- Stringy
- Convex
- Skinny
- Clumpy
- Striated

Density and Association

- Monotonic
- Outlying
- Sparse
- Skewed

Can scagnostics predict non-normality?



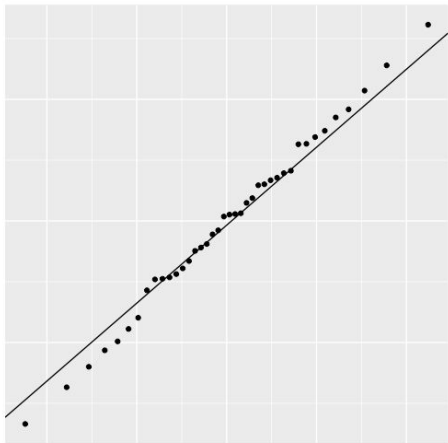
A new scagnostic

$$C_{deviation} = \frac{1}{n} \sum_{i=1}^k ((x_i^2 + 1)(y_i - x_i)^2)$$

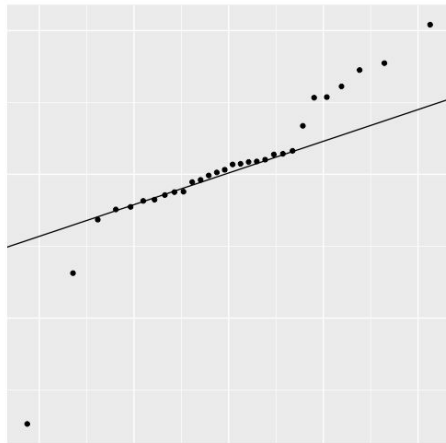
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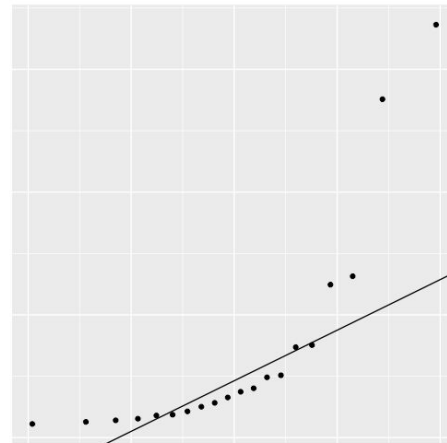
Low (0.007)



Medium (0.549)



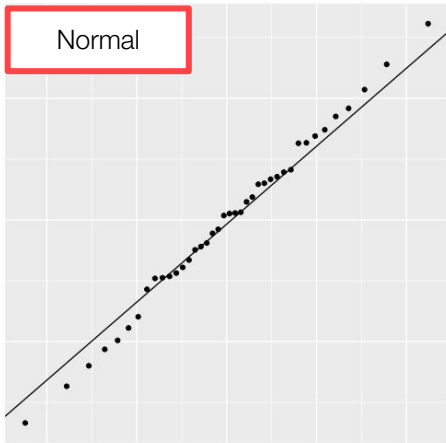
High (1.11)



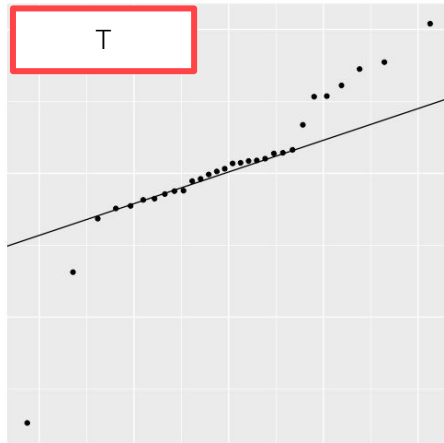
A new scagnostic

$$C_{deviation} = \frac{1}{n} \sum_{i=1}^k ((x_i^2 + 1)(y_i - x_i)^2)$$

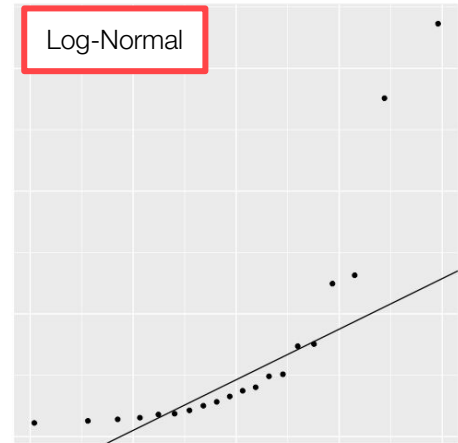
Low (0.007)



Medium (0.549)



High (1.11)



Performance

16,000 QQPlots were generated from a variety of distributions (normal, t, log-normal, exponential, and Chi-Squared).



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Anderson-Darling
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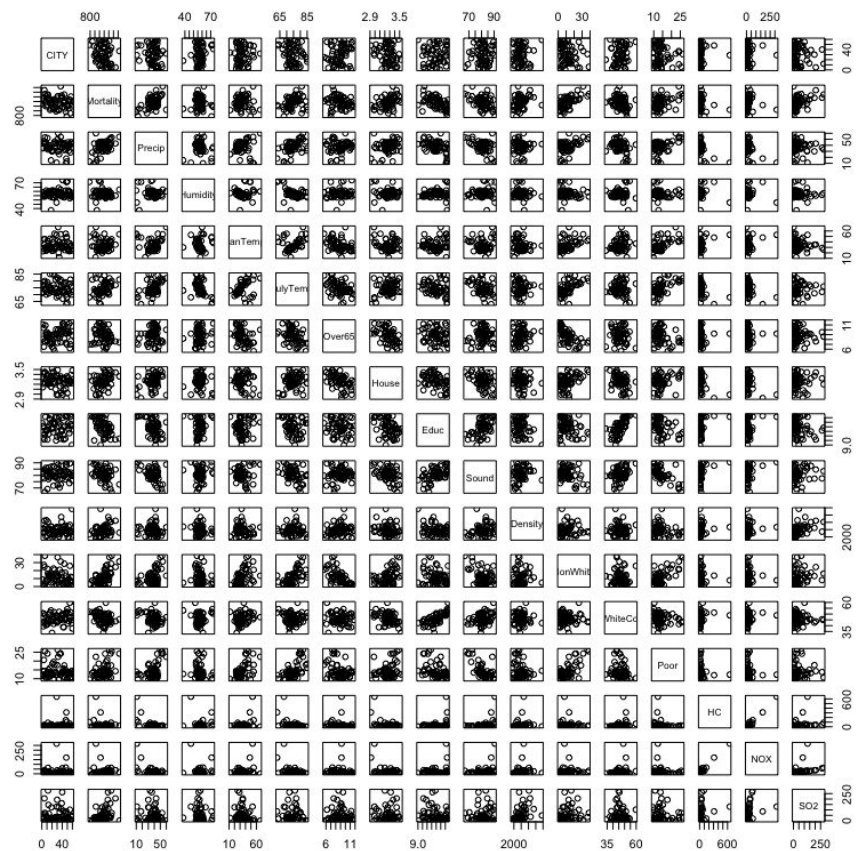
78.6%

Accuracy:
Model with Deviation
Scagnostic

84.0%

Conclusions

Applications



Our App

Looking at Pairwise Relationships

Choose CSV File

Browse... No file selected

Header

Separator

Comma

Semicolon

Tab

Begin

Choose a dataset to analyze!

Our App

Looking at Pairwise Relationships

Choose CSV File

Browse... pollution2.csv

Upload complete

Header

Separator

Comma

Semicolon

Tab

Plot Type:

exponential

funnel

linear trend

null

quadratic

null

Relationship

logNOX vs Precip

logNOX vs JanTemp

logNOX vs JulyTemp

logNOX vs Over65

logNOX vs House

logNOX vs Educ

logNOX vs NonWhite

logNOX vs WhiteCol

logNOX vs Poor

Mortality vs Humidity

Mortality vs JanTemp

Mortality vs JulyTemp

Mortality vs Over65

Mortality vs Sound

Mortality vs Density

Precip vs Humidity

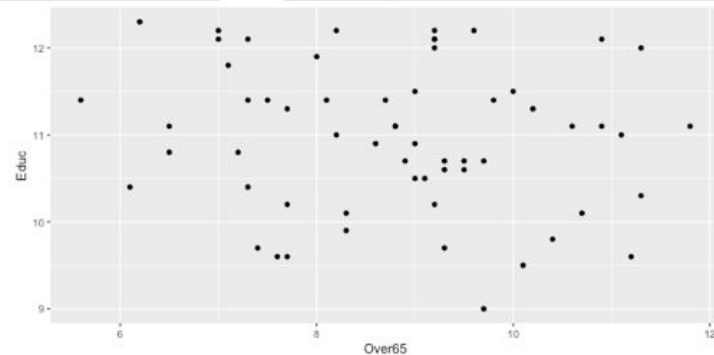
Precip vs JanTemp

Precip vs JulyTemp

Precip vs Over65

Precip vs House

Precip vs Density



Select relationship to view!

Over65 vs Educ

Our App

Looking at Pairwise Relationships

Choose CSV File

Browse... pollution2.csv

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Header

Separator

Comma

Semicolon

Tab

Plot Type: exponential

funnel

linear trend

null

quadratic

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Relationship

logNOX vs Mortality

logNOX vs Humidity

logNOX vs Density

logNOX vs NOX

logNOX vs SO2

Mortality vs NonWhite

Mortality vs Poor

Mortality vs HC

Mortality vs NOX

Mortality vs SO2

Precip vs NonWhite

Humidity vs JulyTemp

Humidity vs Educ

Humidity vs WhiteCol

JanTemp vs NonWhite

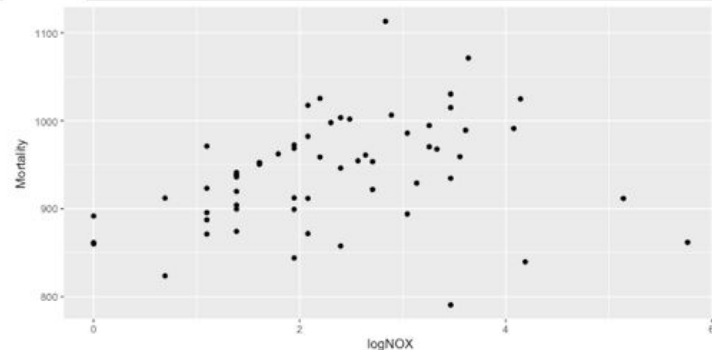
JulyTemp vs HC

Sound vs Poor

Sound vs HC

Density vs HC

Density vs NOX



Select relationship to view!

logNOX vs Mortality

Acknowledgements

Thank you to Adam Loy, the Carleton Math & Statistics Department Faculty, our classmates, and our families.

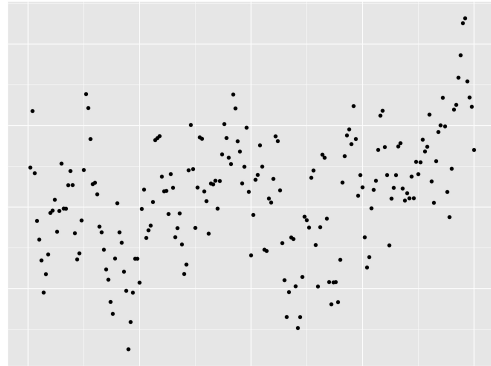


Primary Family Models

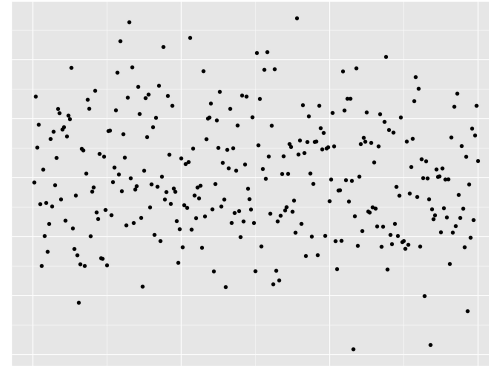
Model	Accuracy
K-Nearest Neighbors	69.6%
Linear Discriminant Analysis	93.9%
Support Vector Machine	97.3%
Logistic Regression	97.4%
Quadratic Discriminant Analysis	98.1%
Random Forest	98.6%

QQ Plots and Time Series

Time Series

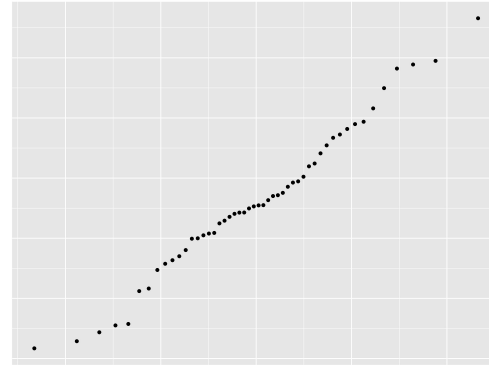
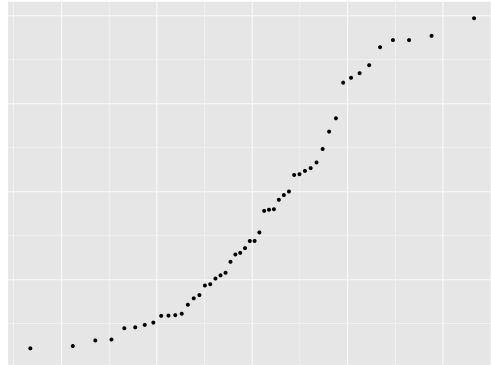


Signal



Null

QQ Plots



#5ea8a7

#ff4447

#257985